



Universität  
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# Energy Frontier: Collider experiments

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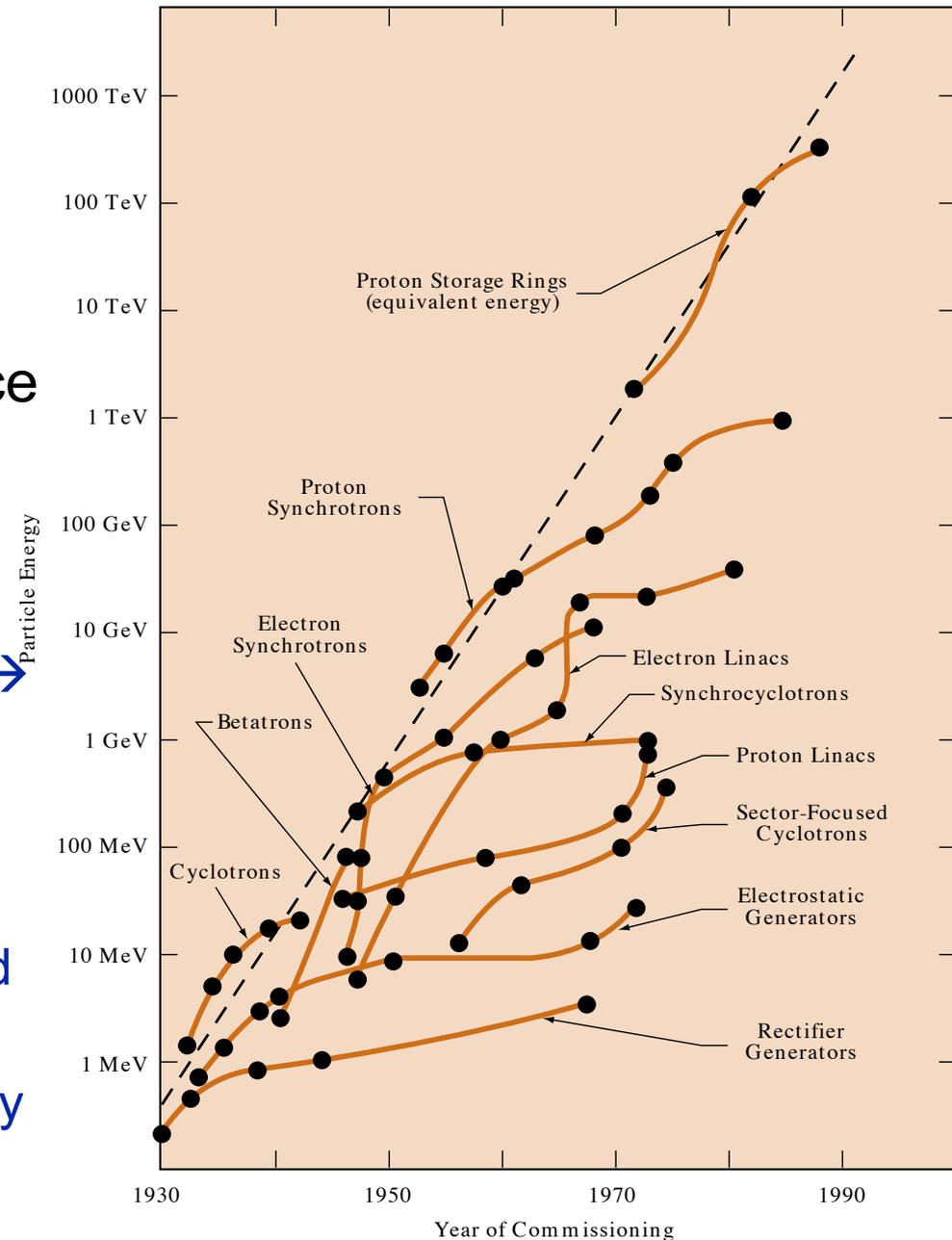
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# Overview

- History of particle accelerators and colliders
- Complementarity of hadron and lepton colliders
- Probing the Standard Model at colliders
  - SLC
  - LEP
  - HERA
  - Tevatron
  - LHC

# History

- 1924/28: First linear accelerator by Gustav Ising and Rolf Wideröe
- 1930: Cyclotron invented and built by Ernest Lawrence
- From 1950: Accelerators used in particle physics
  - Discovery of neutral pion, vector mesons, anti-proton → appearance of particle zoo
- 1970: First colliders
  - More particles discovered
  - Organization in the Standard Model
  - Towards modern high-energy physics



# Electromagnetic acceleration

Configuration	Static acceleration	Resonant acceleration	Inductive acceleration
Linear 	DC gun Cockcroft Walton Van de Graaf	RF linac <ul style="list-style-type: none"> <li>standing wave (= drift tube linac, DTL)</li> <li>travelling wave</li> </ul>	Induction linac
Circular 		Cyclotron Iso-Cyclotron Synchro-Cyclotron Microtron Synchrotron	Betatron

# Acceleration and beams

- Two key themes in particle physics for accelerator physics and technology
- High center-of-mass energy
  - Stimulated the transition from fixed target devices to devices with colliding beams
  - Stimulates the invention of new methods of acceleration and new technologies
- High event rate: high luminosity
  - Stimulates the physics of particle beams

$$\frac{dR}{dt} = \mathcal{L} \cdot \sigma$$

$$\mathcal{L} = \frac{N_1 N_2 f N_b}{4\pi \sigma_x \sigma_y}$$

$$\mathcal{L}_{\text{int}} = \int_0^T \mathcal{L}(t') dt'$$

Event rate proportional to instantaneous luminosity and cross section

$\mathcal{L}$  : instantaneous luminosity [ $\text{cm}^{-2}\text{s}^{-1}$ ]

$N_1, N_2$ : number of particles per bunch

$N_b$ : number of bunches

$f$ : revolution frequency

$\sigma_x, \sigma_y$ : transverse beam dimension

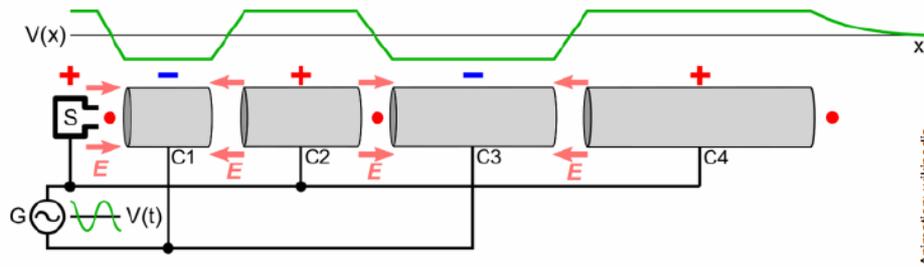
$\mathcal{L}_{\text{int}}$ : integrated luminosity [ $\text{pb}^{-1}, \text{fb}^{-1}, \text{ab}^{-1}$ ]

# High center-of-mass energy

- Linear acceleration (Linac)
  - High acceleration gradient  $G$  (MV/m)
  - One-pass acceleration of particles
  - Dimension given by desired energy and gradient
    - $L \sim E_{\text{cm}}/G$
- Circular acceleration
  - Accelerate particles in one or few locations and bend particles back to those locations
  - Dimension given by momentum and magnetic field
    - $R \sim P_{\text{cm}}/B$
- $E_{\text{cm}}$  is given by particle physics goal
- $L$  is given by money, politics, available space
- $G, B$  are given by technology (and money)

# High center-of-mass energy

- Linear acceleration: High gradient
  - Cylindrical electrodes with alternating field, length matched to particle velocity



$$\frac{dp}{dt} = eE$$

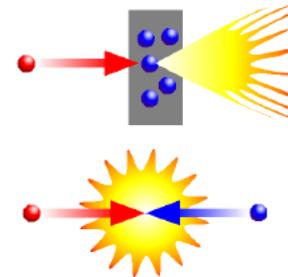
- Circular acceleration: High magnetic field
  - Achieved with superconducting magnets

- Fixed target vs collider

- Fixed target:  $E_{cm} = \sqrt{2E_b m_t c^2}$

- Collider:  $E_{cm} = 2E_b$

- Getting over  $\sqrt{E_b}$  dependence has significant consequences for the required beam quality

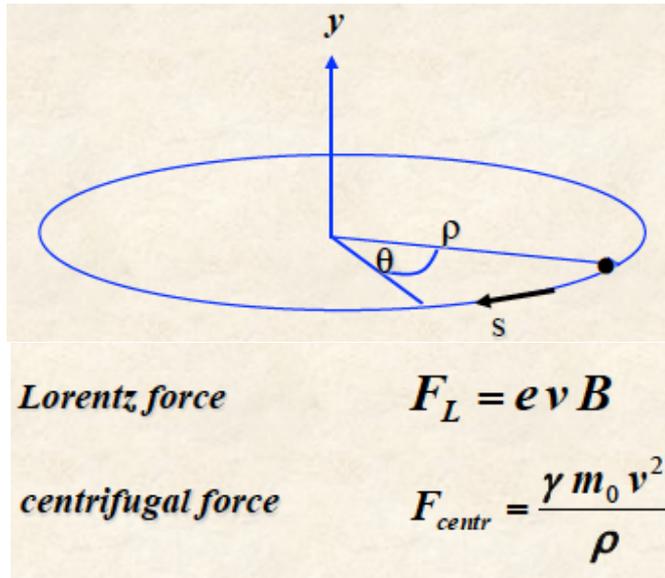


# High luminosity

- Formation of beams of particles is needed for acceleration within accelerator
  - In the past, motivated by keeping the particles inside the accelerator
  - For fixed target experiments, the event rate does not depend on the beam size, just that it hits the target in roughly the right location
  - For colliders, the beam structure and size has a large influence on the luminosity
- Accelerator design begins with the concept of a design orbit (circular accelerator) or trajectory (Linac)
- The beam needs to be near this orbit or trajectory all the time and throughout the length of the device
  - Beam size should be small
  - Angular and transverse momentum divergence should be small
  - Timing matters → bunch structure
  - Energy spread should be small

# Transverse motion

- A set of particles can be formed into a beam in the neighborhood of some design orbit or trajectory by having external fields confining all particles to that neighborhood
- For relativistic particles magnetic fields are used to do the bending

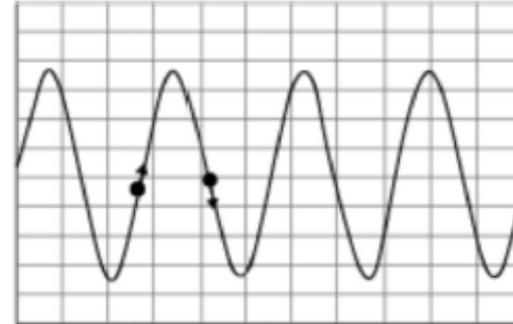
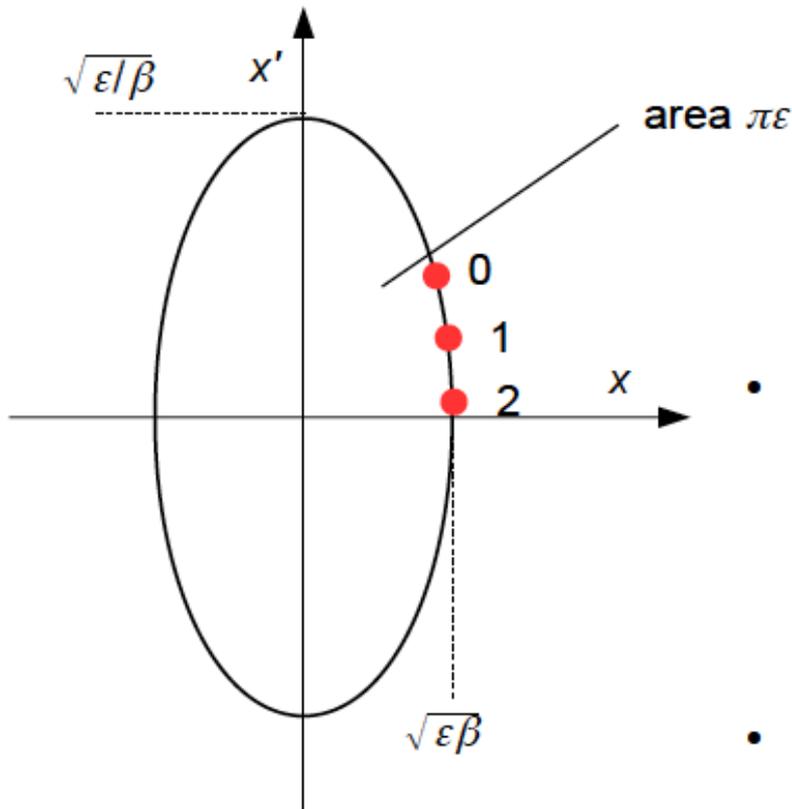


$$\frac{p}{e} = B \rho$$

: **magnetic rigidity**  
describes the  
resistance of a particle  
for being reflected

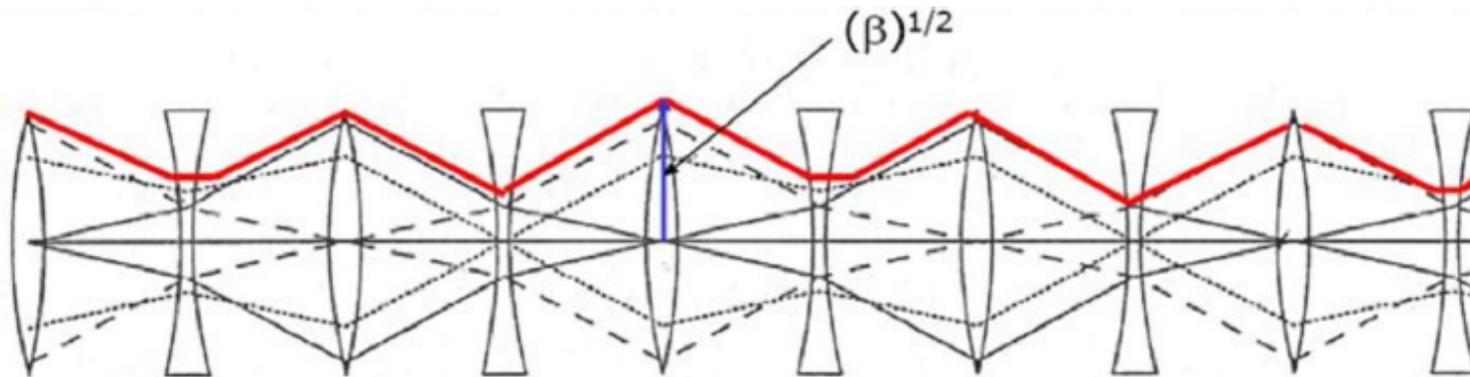
- Example: LHC
  - $B=8.3\text{T}$ ,  $p=7000\text{ GeV}/c$
  - $\rho = 2.83\text{ km}$ ,  $2\pi\rho = 18\text{ km} \sim 66\%$  of machine circumference

# Phase space ellipse



- A single particle undergoing betatron oscillations describes an ellipse in phase space, when measured turn after turn at the same position in the ring
  - periodically going from maximum position  $x$  to maximum divergence angle  $x' = dx/ds$  and back
- The area  $A = \pi\epsilon$  of the ellipse is a measure of how much the particle departs from the reference trajectory.
- The quantity  $\epsilon$  is called the **emittance**. (Single-particle emittance in case of one particle)
- The area in phase space occupied by all particles of a beam (modulo  $\pi$ ) is called the **beam emittance**.
- Emittance is a property of the beam

# $\beta$ -function



from: Mei Bai, BND School 2015 (original?)

- Depending on the initial conditions, different particles may follow very different trajectories along the accelerator
- The envelop of all trajectories is described by a periodic function, the  $\beta$ -function
- **The  $\beta$ -function is a property of the accelerator!**
- The beam size is defined by both, the emittance and the  $\beta$ -function

$$\sigma(s) = \sqrt{\epsilon \cdot \beta(s)}$$

- $\beta^*$  is the value of the  $\beta$ -function at the interaction point

# Synchrotron radiation

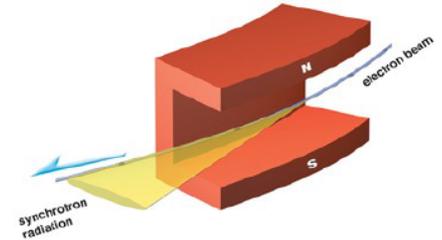
- The choice of accelerator type is strongly influenced by the particle type
- The power radiated off in circular motion is:

$$P_y = \frac{e^2 c}{6 \pi \epsilon_0} \left( \frac{E}{mc^2} \right)^4 \frac{\beta^4}{\rho^2} \longrightarrow \text{Energy loss per turn: } U_0 = P_y \cdot t_{\text{turn}} = P_y \frac{2 \pi \rho}{c}$$

In practical units ( $\beta \approx 1$ ):

$$U_0(\text{keV}) = 10^{33} \frac{e}{3 \epsilon_0} \left( \frac{e}{mc^2} \right)^4 \frac{[E(\text{GeV})]^4}{\rho(\text{m})}$$

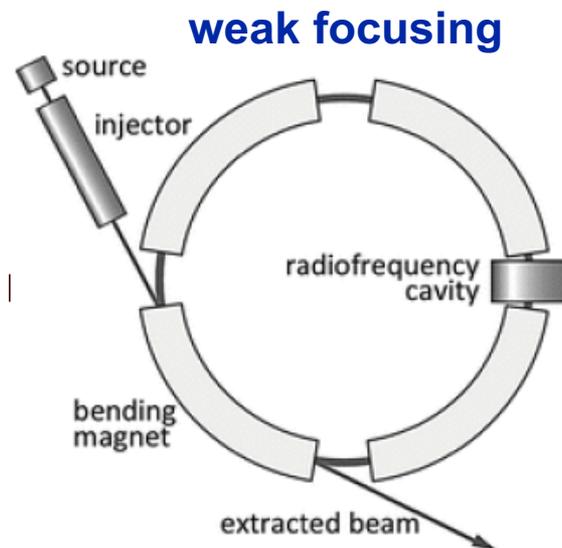
$\approx 88.5$  (electrons)  
 $\approx 4.84 \times 10^{-8}$  (muons)  
 $\approx 7.79 \times 10^{-12}$  (protons)



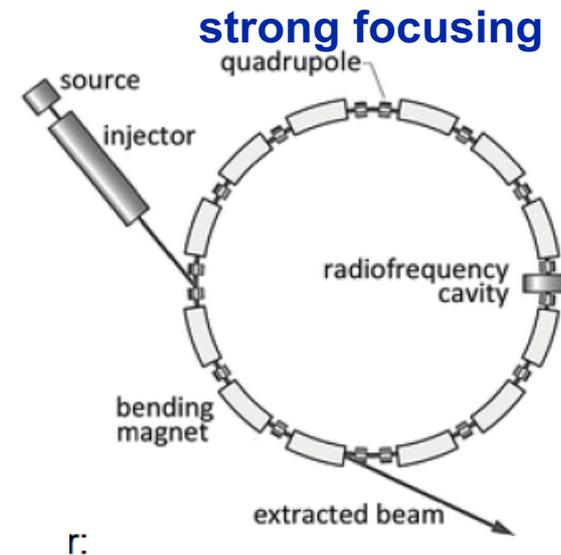
- In practice, using size ( $\rho$ ) to compensate the increase in synchrotron radiation for electrons works only up to a certain point
- If the energy loss per turn gets too large, might as well use a Linac to reach higher energies
- Note: on the positive side, synchrotron radiation today is the reason why most electron accelerators are built

# Synchrotron

- **Cyclotron:** constant magnetic field, constant-frequency electric field, varying orbit
- **Synchrotron:** Constant orbit with varying magnetic and electric fields → synchronization between particle revolution frequency, accelerating and bending field
- Dipole magnets need large aperture to accommodate particle oscillations
- Invention of strong focusing as breakthrough



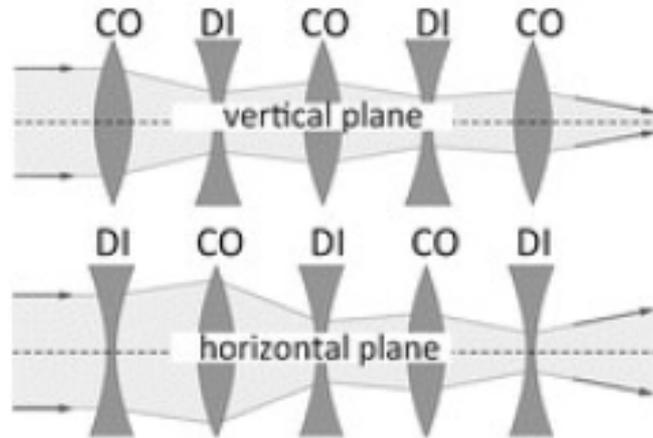
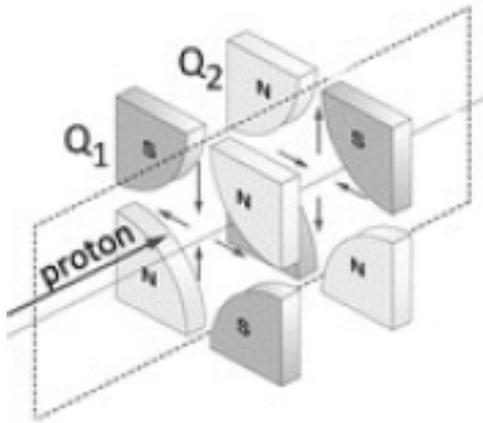
U. Amaldi, "Particle Accelerators: from Big Bang Physics to Hadron Therapy", Springer 2014



U. Amaldi, "Small Accelerators Grow", Springer 2014

# Strong focusing

- Combination of focusing and defocusing magnets has an overall focusing effect (as with optical lenses)
- First time empirically tried by E.D Courant, S. Livingston and H.S. Snyder in 1952 at the Cosmotron (BNL)



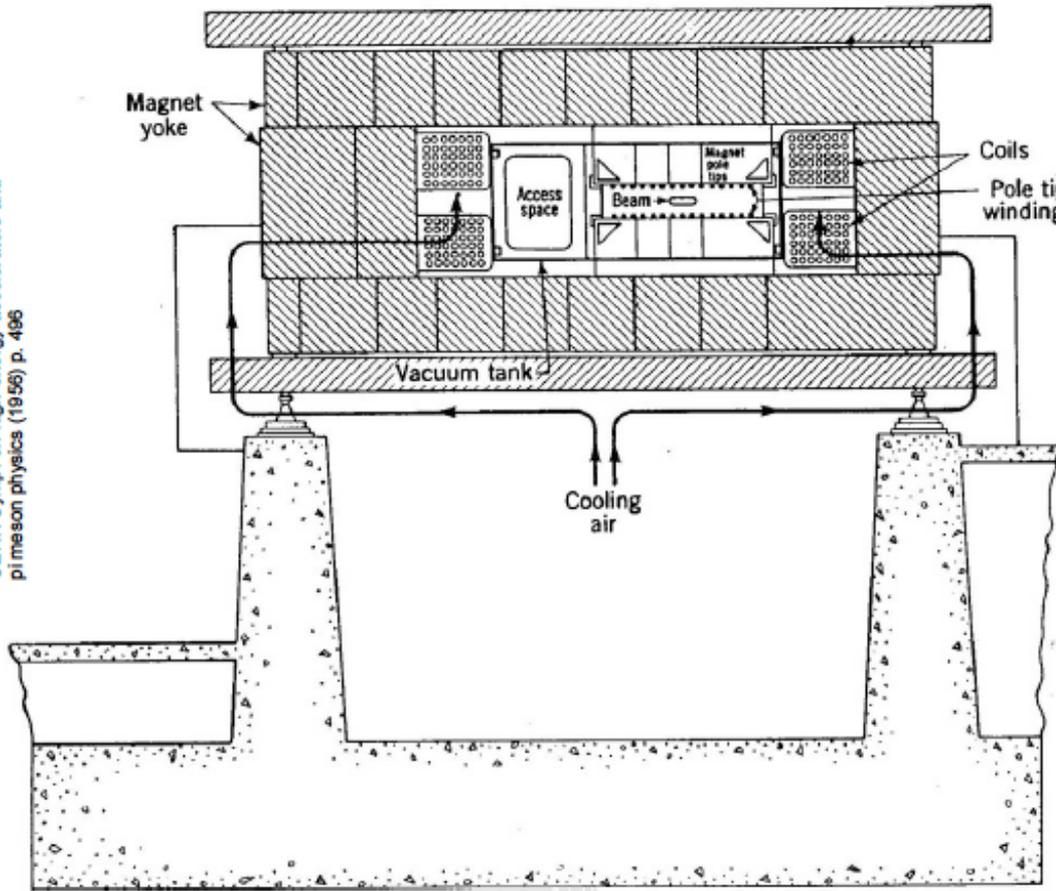
*Sequences of converging (CO) and diverging (DI) focusing magnets have a net focusing effect!*



U. Amaldi, "Particle Accelerators: from Big Bang Physics to Hadron Therapy", Springer 2014

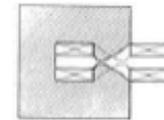
# Strong focusing revolution

E.J. Lofgren: *Bevatron operational experiences*  
CERN Symp. on high-energy accelerators and  
pionon physics (1958) p. 496



**6-GeV Bevatron (Berkeley)**

to scale!

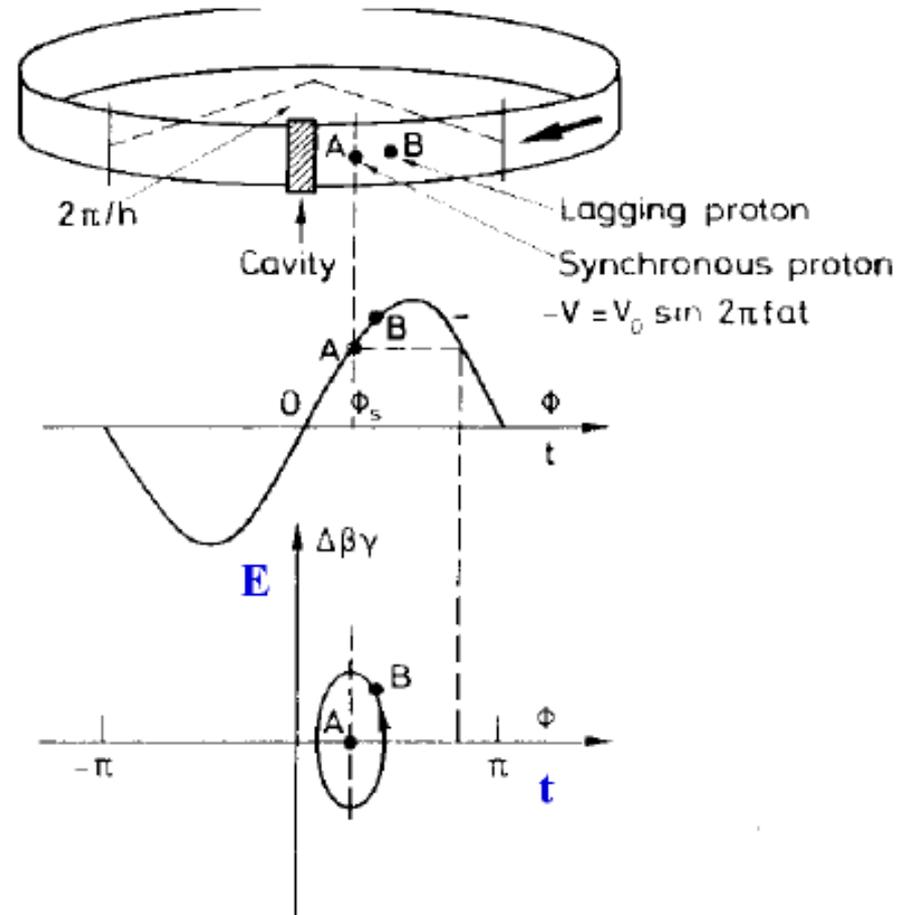


**33-GeV AGS  
(Brookhaven)**

# Phase stability

- Second key prerequisite for modern synchrotrons is concept of phase stability
  - Particles are only accelerated if they have the correct phase w.r.t. RF field
  - Particles with too much energy arrive at a phase to get less
  - Particles with too little energy arrive at the phase to get more
- Formation of particle bunches

## Phase stability



# First modern synchrotrons

- Built in 1959, both still in use today

PS at CERN 28 GeV



- 628m circumference
- 245 dipole magnets ( $B^{\text{dipole}}=1.2\text{T}$ )
- First used for fixed-target experiments
- Later for pre-acceleration for ISR, SPS, LEP, LHC

AGS at BNL 33 GeV



- 807m circumference
- 240 dipole magnets ( $B^{\text{dipole}}=1.2\text{T}$ )
- First used for fixed-target experiments
  - 1962: Discovery of  $\nu_{\mu}$
  - 1976: Discovery of  $J/\psi$
  - 1980: CP violation in the kaon system
- Later for pre-acceleration for RHIC

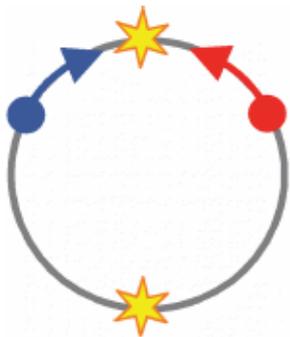


# Storage ring collider

- Next step from synchrotron is the storage ring collider
  - Circular collider: one or two storage rings with opposite beams
  - Energy frontier: acceleration mode (synchrotron) followed by storage mode (in the same ring)
- Single ring can be used for particle-antiparticle collider → need to make sure that no unwanted collisions happen → use different orbits
- Decrease beam size at interaction point to increase density and hence luminosity

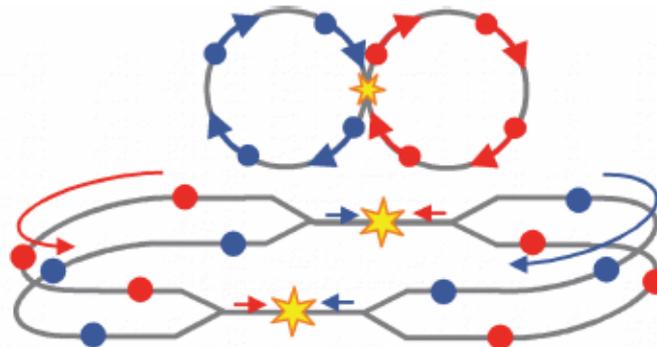
## Collider schemes:

single ring



$\bullet = \bar{\bullet} \quad E = \bar{E}$

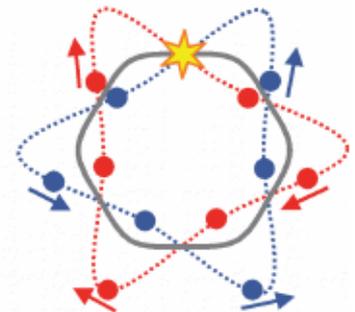
double rings



avoid parasitic collisions  
or close encounters

allows  $\bullet \neq \bar{\bullet} \quad E \neq \bar{E}$

“brezel” scheme

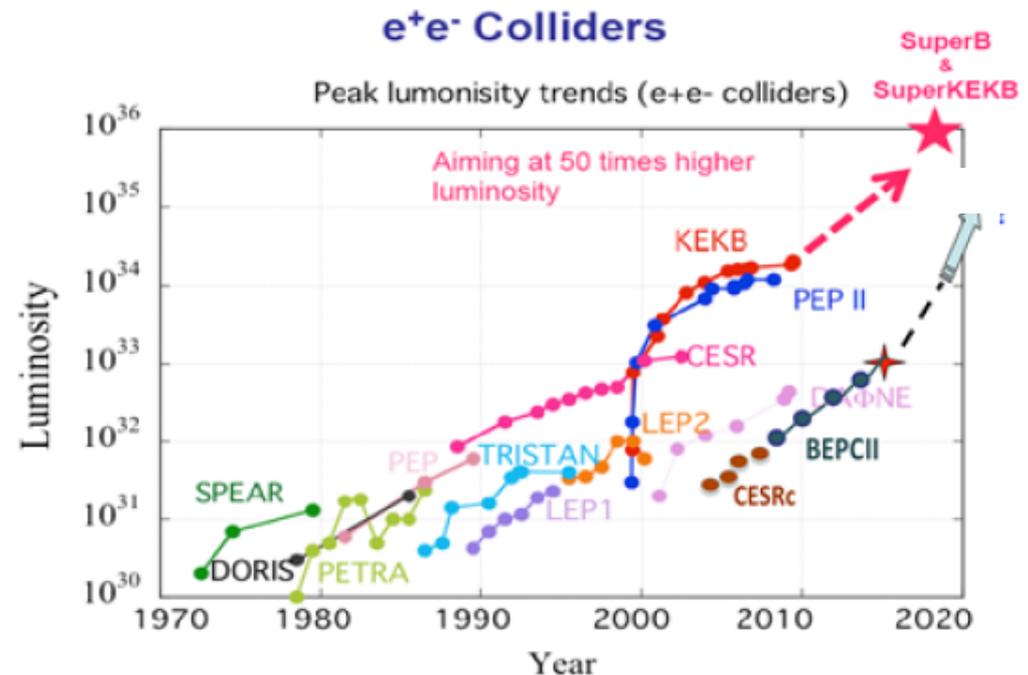
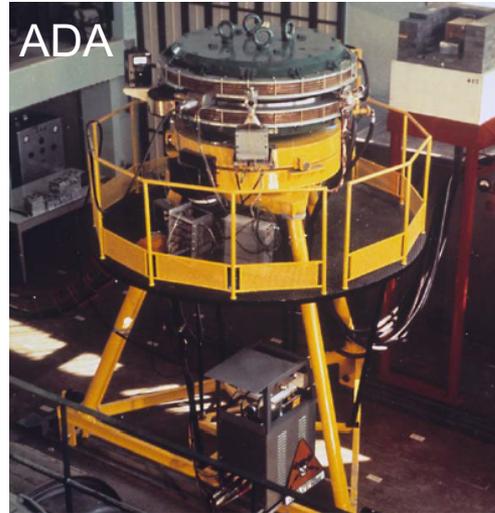


orbit oscillations to avoid  
parasitic collisions

$\bullet = \bar{\bullet} \quad E = \bar{E}$

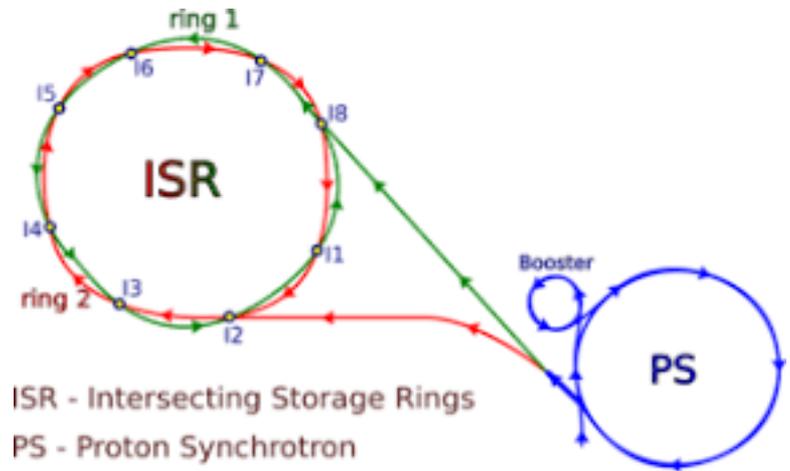
# $e^+e^-$ Colliders

- 1961: ADA, first electron-positron collider at Frascati, Italy
  - Proved technology
  - 4m circumference
  - $E_{cm} = 500$  MeV
- 1969-1993: ADONE
  - Used for particle physics
  - Circumference of 105m
  - $E_{cm} = 3.1$  GeV (initially 3.0 GeV  $\rightarrow$  just missed  $J/\psi$  in 1974)
- Followed by many others all around the world
- Electron beams can be focused on very small spot  $\rightarrow$  reach highest luminosities



# Proton colliders

- 1971: Added storage ring to CERN PS → first proton-proton collider – intersecting storage rings (**ISR**)
  - Two rings with 300m circumference
  - $E_{cm} = 62 \text{ GeV}$

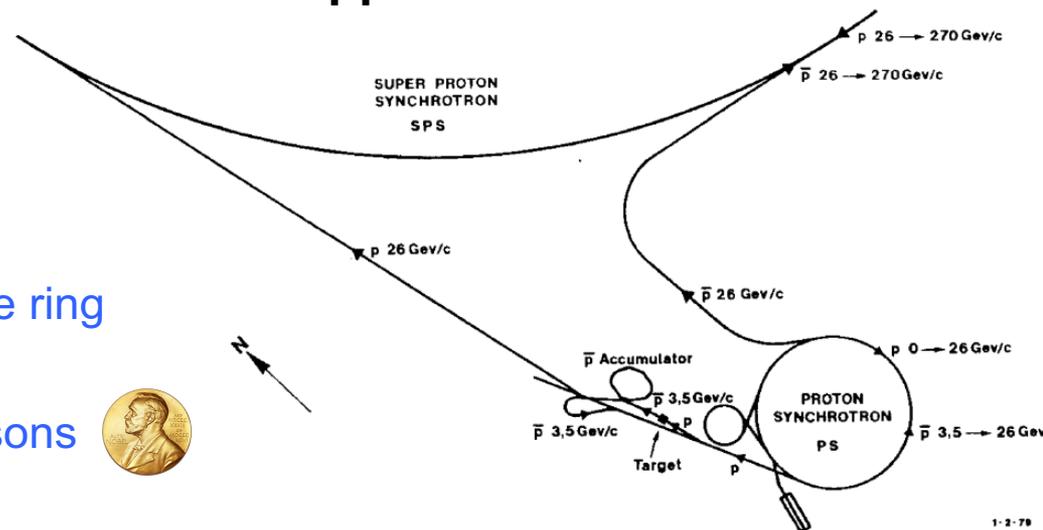


- 1976: **SPS**
  - Circumference of 6.9km
  - 1425 magnets ( $B^{\text{dipole}}=2.0\text{T}$ )
  - $E_{\text{beam}} = 450 \text{ GeV}$

- 1981-1990: **Spp̄S**
  - Operation as  $p\bar{p}$  collider in single ring
  - $E_{cm}=546 \text{ GeV}$
  - 1984: Discovery of W and Z bosons
  - $L_{\text{inst}}^{\text{max}} = 3 \times 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$

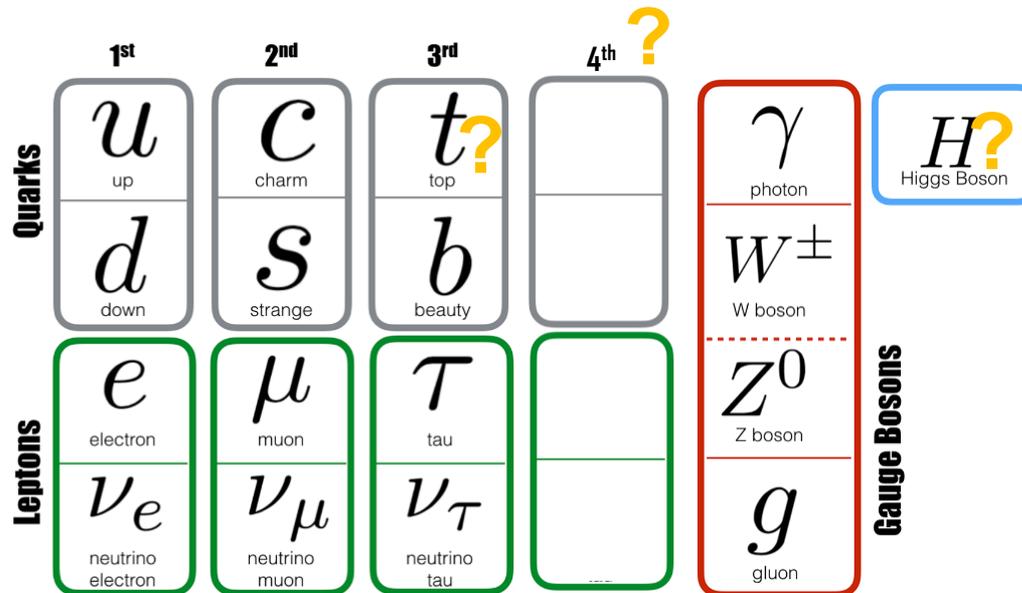


## SPS Spp̄S

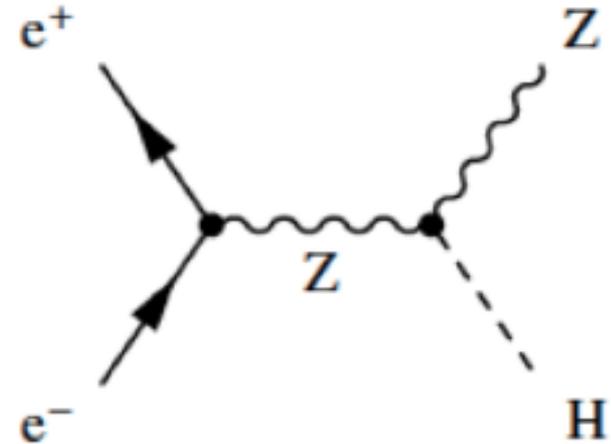
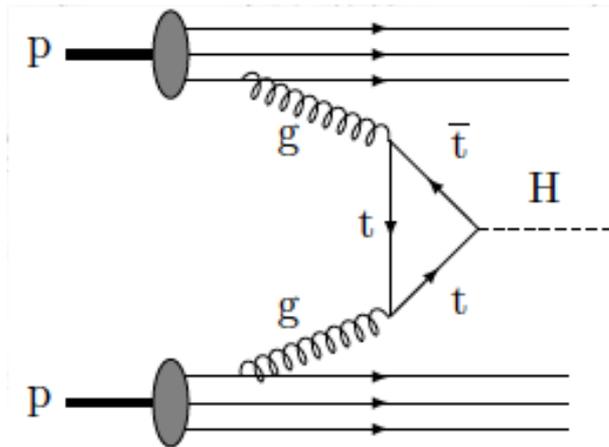


# The Standard Model mid-1980

- Discovery of  $W$  and  $Z$  boson with predicted masses was spectacular confirmation of theory of electroweak unification by Glashow, Salam and Weinberg
- Still missing particles in the Standard Model: top quark, Higgs boson, additional families?
- In need of experiments reaching higher energies to explore new phase space and strive for discoveries

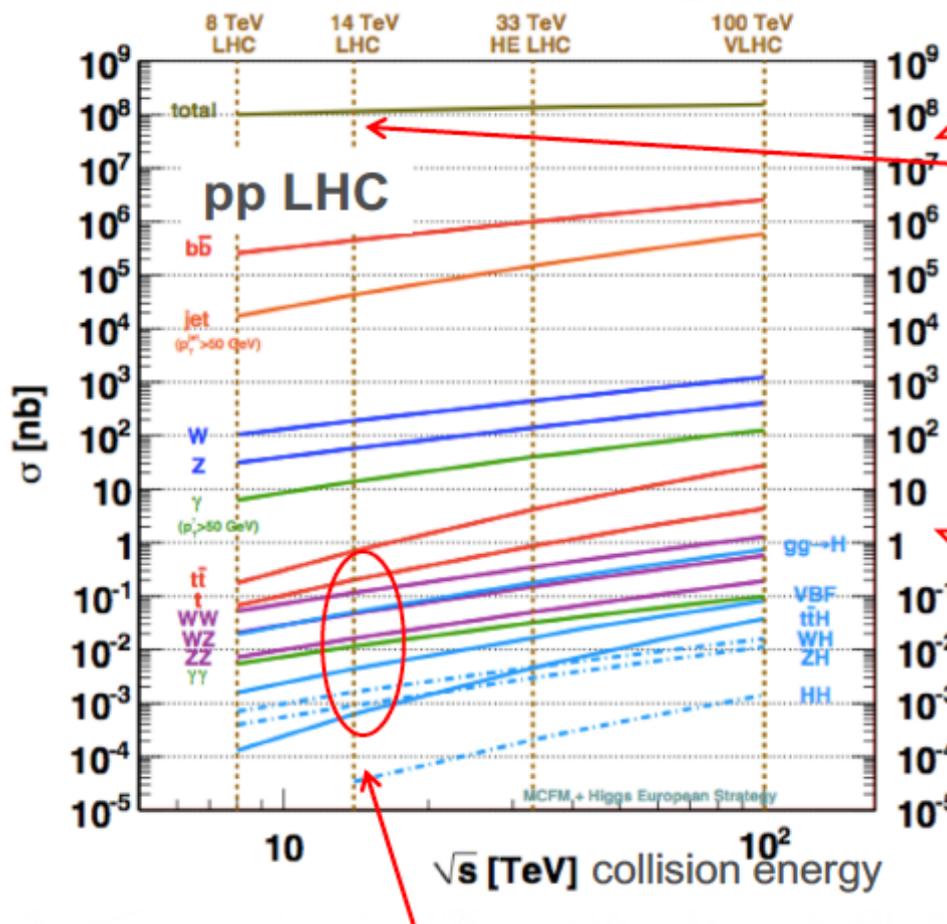


# pp collisions vs $e^+e^-$ collisions



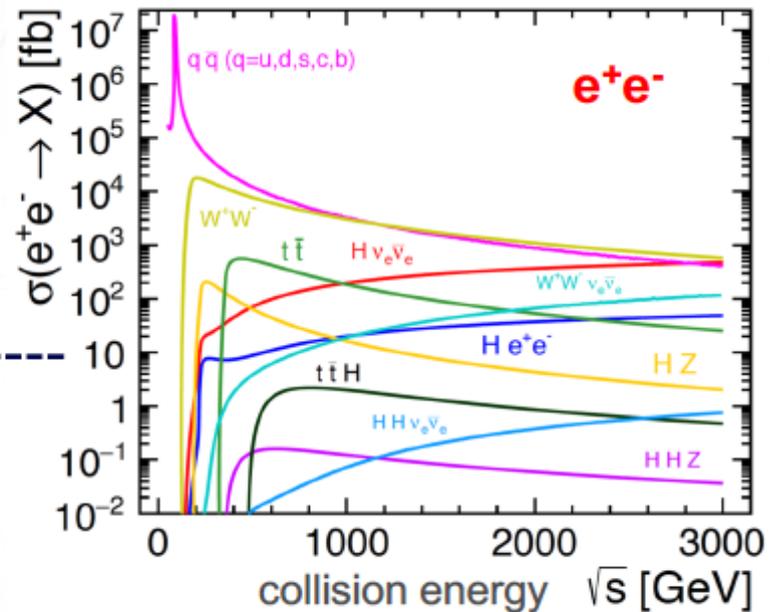
p-p collisions	$e^+e^-$ collisions
<p><b>Proton is compound object</b></p> <ul style="list-style-type: none"> <li>→ Initial state not known event-by-event</li> <li>→ Limits achievable precision</li> </ul>	<p><b><math>e^+/e^-</math> are point-like</b></p> <ul style="list-style-type: none"> <li>→ Initial state well defined (<math>E, p</math>)</li> <li>→ High-precision measurements</li> </ul>
<p><b>High rates of QCD backgrounds</b></p> <ul style="list-style-type: none"> <li>→ Complex triggering schemes</li> <li>→ High levels of radiation</li> </ul>	<p><b>Clean experimental environment</b></p> <ul style="list-style-type: none"> <li>→ Trigger-less readout</li> <li>→ Low radiation levels</li> </ul>
High cross-sections for <b>colored-states</b>	Superior sensitivity for <b>electro-weak states</b>
High-energy <b>circular</b> pp colliders feasible	<ul style="list-style-type: none"> <li>- At lower energies (<math>\lesssim 350</math> GeV), <b>circular</b> <math>e^+e^-</math> colliders can deliver <b>very large luminosities</b>.</li> <li>- Higher energy <math>e^+e^-</math> requires <b>linear</b> collider.</li> </ul>

# pp collisions vs e<sup>+</sup>e<sup>-</sup> collisions



LHC total cross section factor > 100 million !!

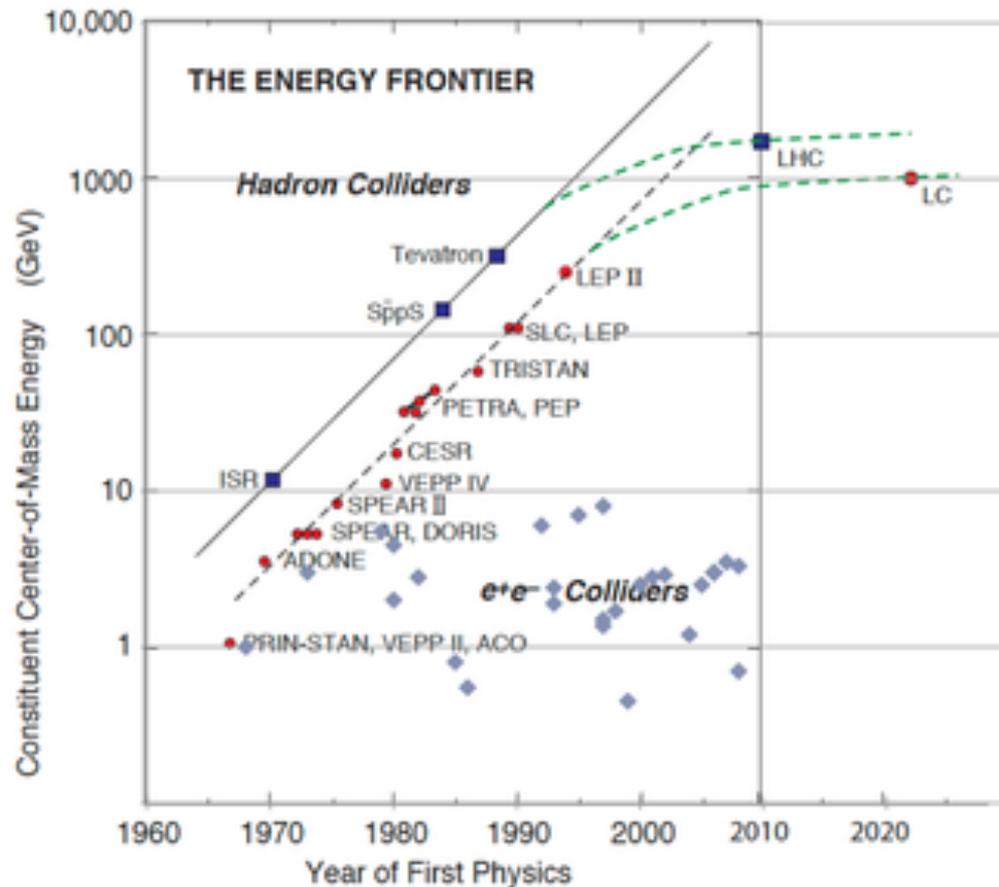
At LHC, much of the interesting physics needs to be found among a huge number of collisions



e<sup>+</sup>e<sup>-</sup> events are "clean"

# Followed both paths....

- Precision tests of the Standard Model at lepton colliders with  $\sqrt{s} \sim 100 \text{ GeV} \rightarrow \text{LEP and SLC}$
- Pushing toward highest energies with hadron colliders with  $\sqrt{s} \sim 1\text{-}10 \text{ TeV} \rightarrow \text{Tevatron and LHC}$



# Lepton colliders

# Linear or circular?

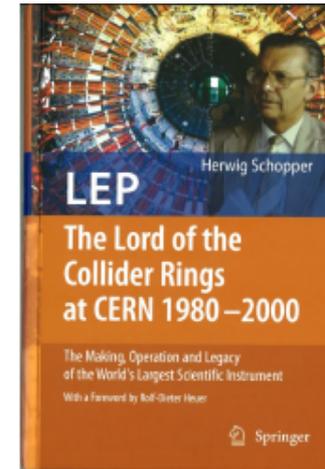
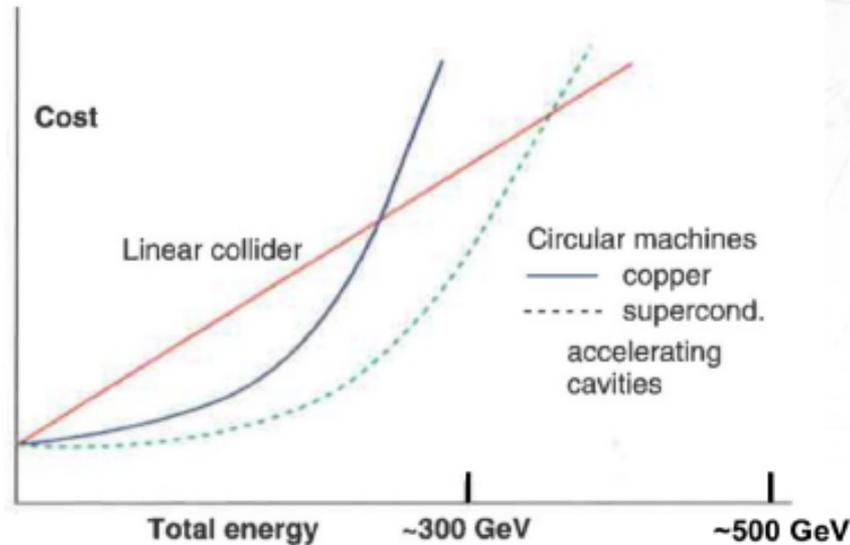
- Acceleration of electrons in circular machines limited by Synchrotron radiation

– Energy loss per turn grows like

$$\Delta E \propto \frac{1}{R} \left( \frac{E}{m} \right)^4$$

– Must compensate with R and accelerating cavities

→ cost also grows like  $E^4$

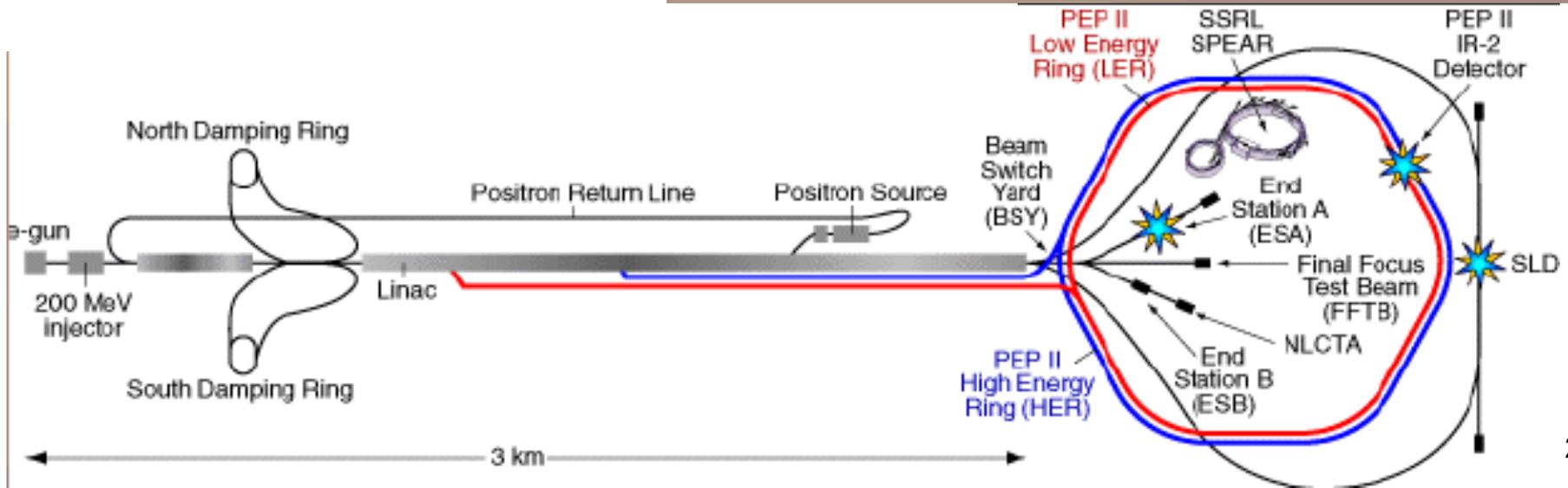
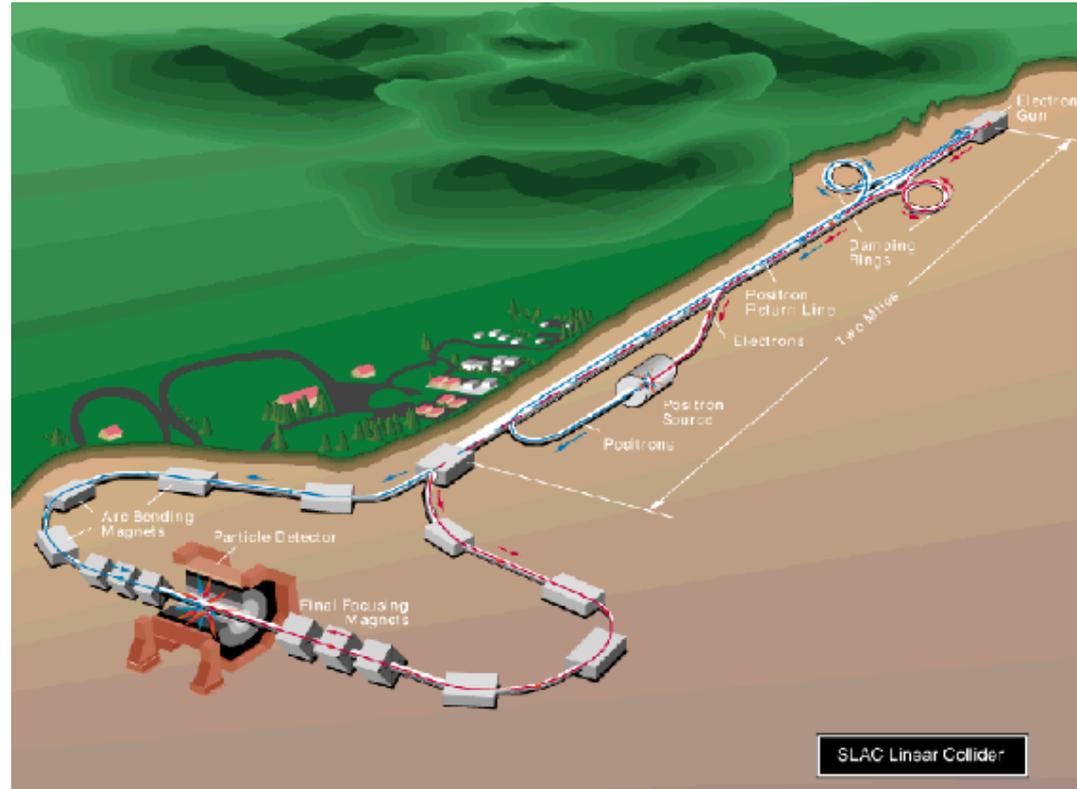


→ “Up to a center-of-mass energy of 350 GeV at least, a circular collider with superconducting magnets is the cheapest option”

→ “At and above 500 GeV, a  $e^+e^-$  collider can only be linear”

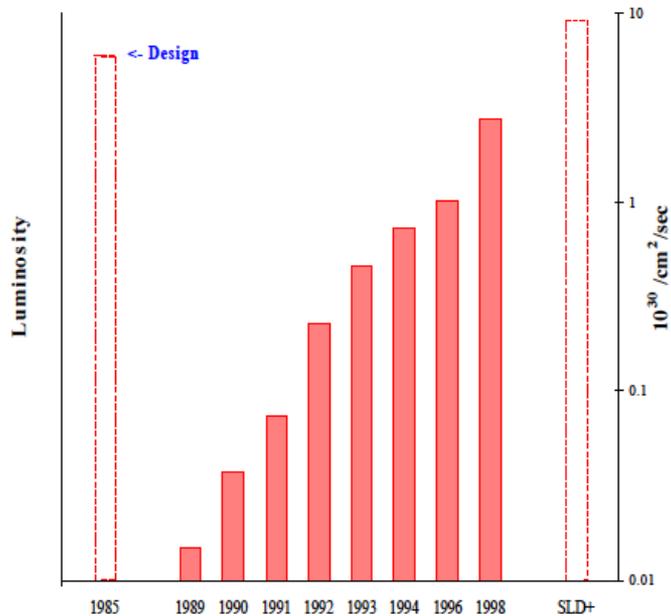
# SLC at SLAC

- First linear  $e^+e^-$  collider
  - Construction started in 1983, experiments in 1989
- $E_{cm} \sim 90 \text{ GeV} \rightarrow Z$  peak
- Unique measurements thanks to highly polarized beam

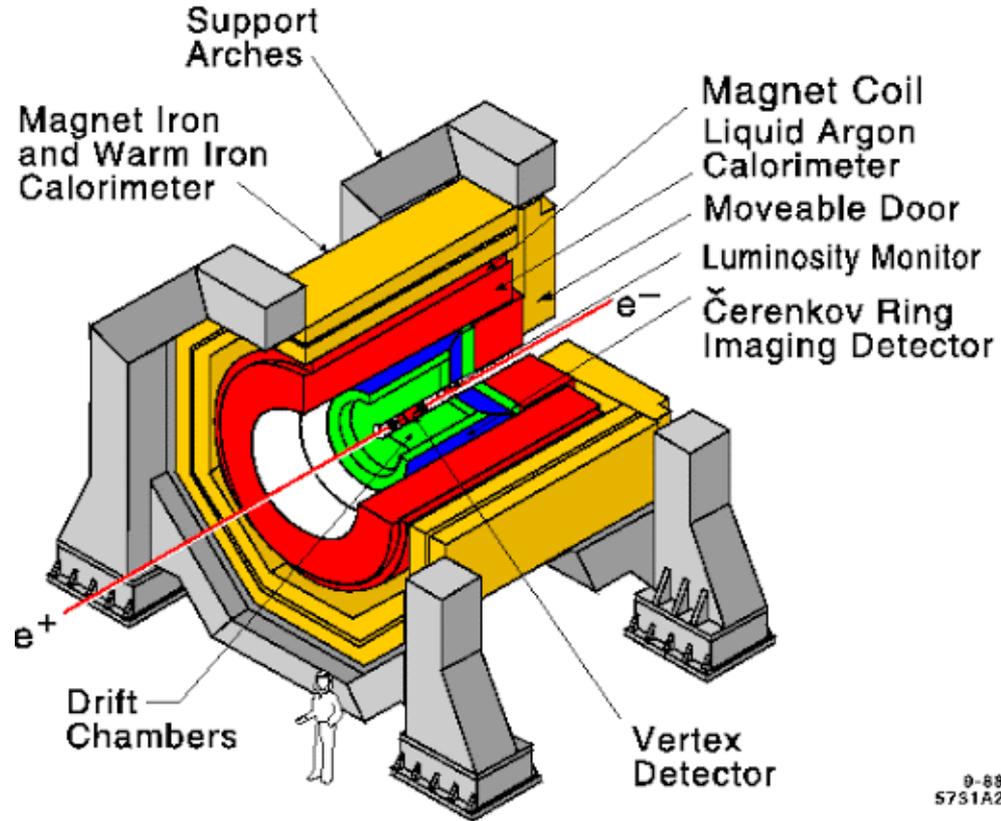


# SLD (1992-1998)

## SLC luminosity



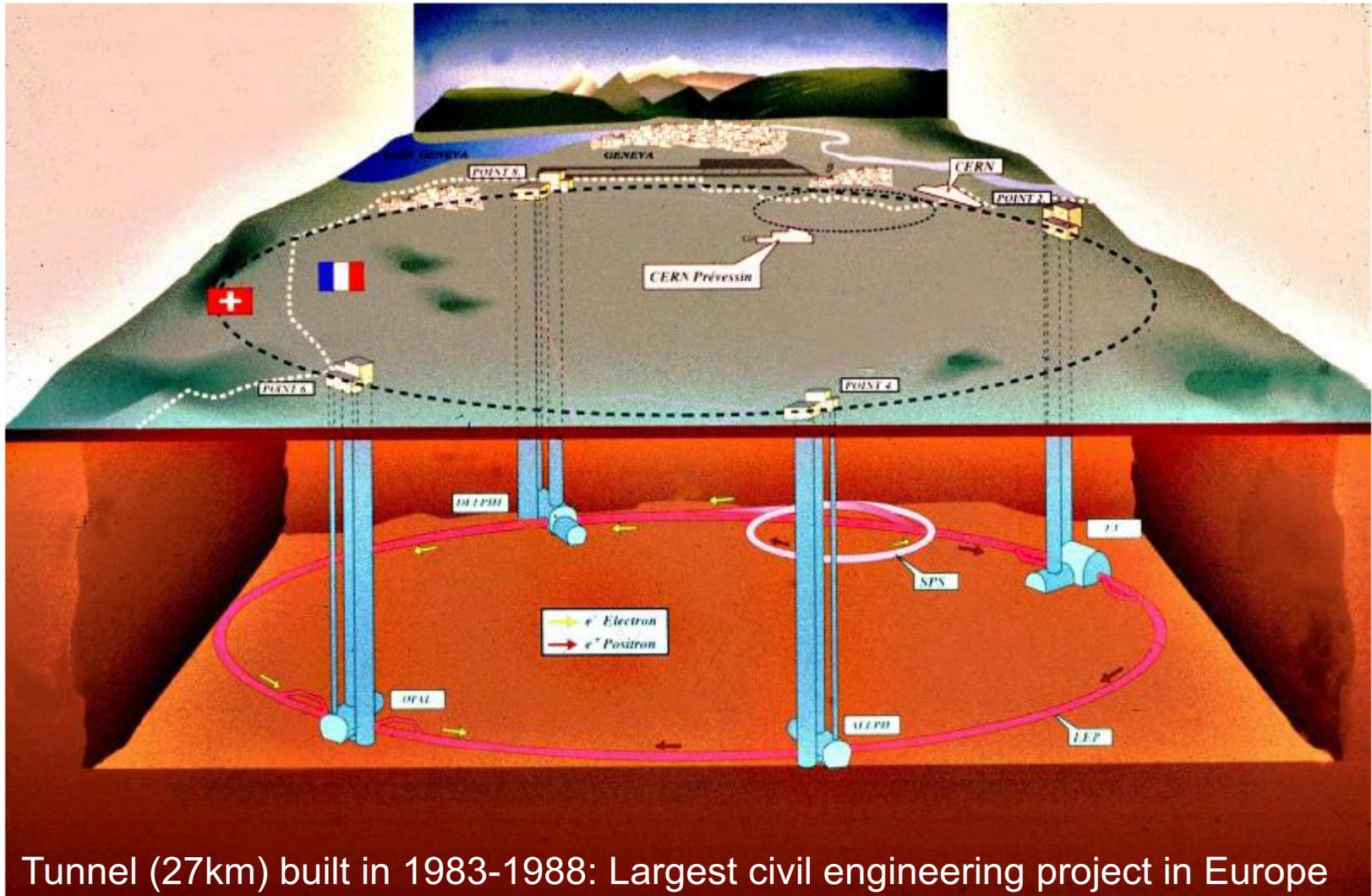
350'000 Z events



- Optimized for reconstruction of Z boson decays
- Silicon pixel detector for vertex reconstruction
  - Use of CCDs possible because of low collision rate (120 Hz)

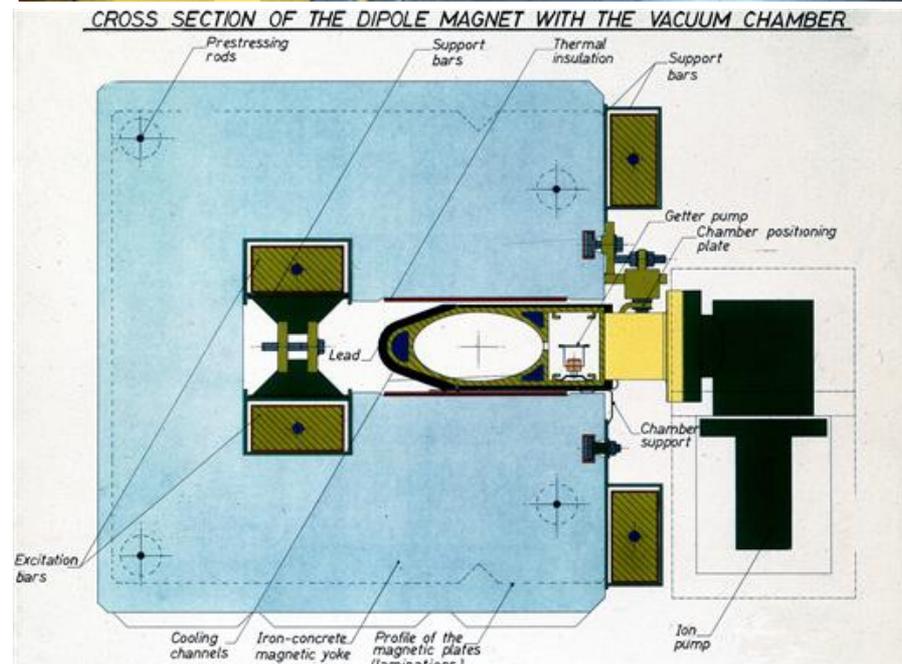
# LEP

## Experiments: ALEPH, DELPHI, L3, OPAL

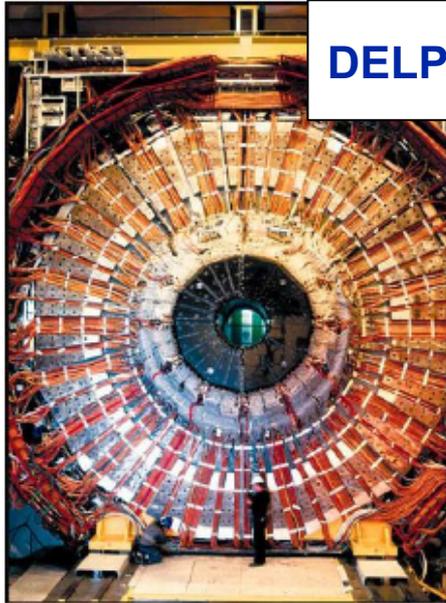


# LEP

- $e^+e^-$  collider
- Same magnets used for acceleration and storage of both beams
- $B_{\max} = 0.135\text{T}$
- $E = 104.5\text{ GeV}$
- $E_{\text{inj}} = 20\text{ GeV}$
- 4x4, 8x8, 12x12 bunches
- $1.7 \times 10^{11} e^+/e^-$  per bunch
- Bunch crossing rate of 450 kHz
- $L_{\text{inst}}^{\max} = 1 \times 10^{32} \text{cm}^{-2} \text{s}^{-1}$
- **LEP-I (1989-1995):** Operated as Z factory with  $\sqrt{s} \sim 91\text{ GeV}$
- **LEP-II (1996-2000):** Operated at/above WW threshold up to  $\sqrt{s} = 209\text{ GeV}$



# LEP experiments built by international collaborations

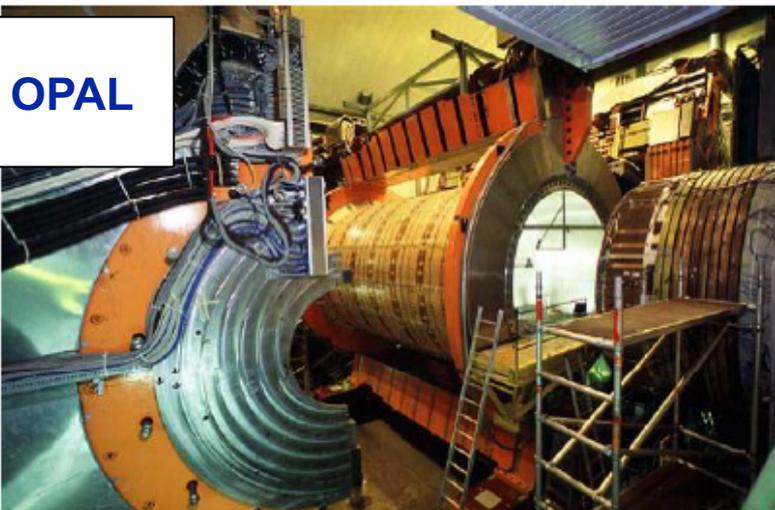


DELPHI

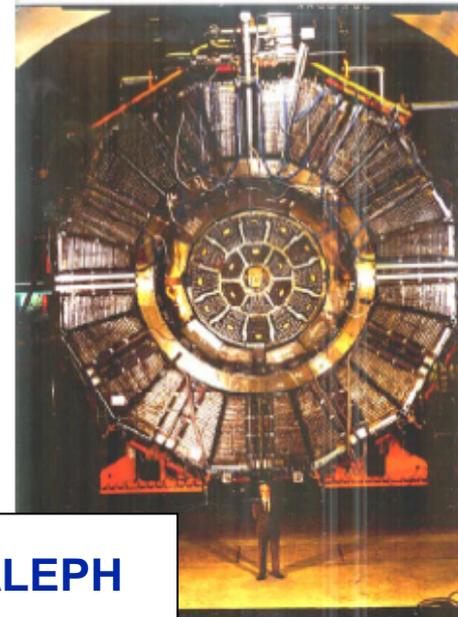


L3

LEP Experiments



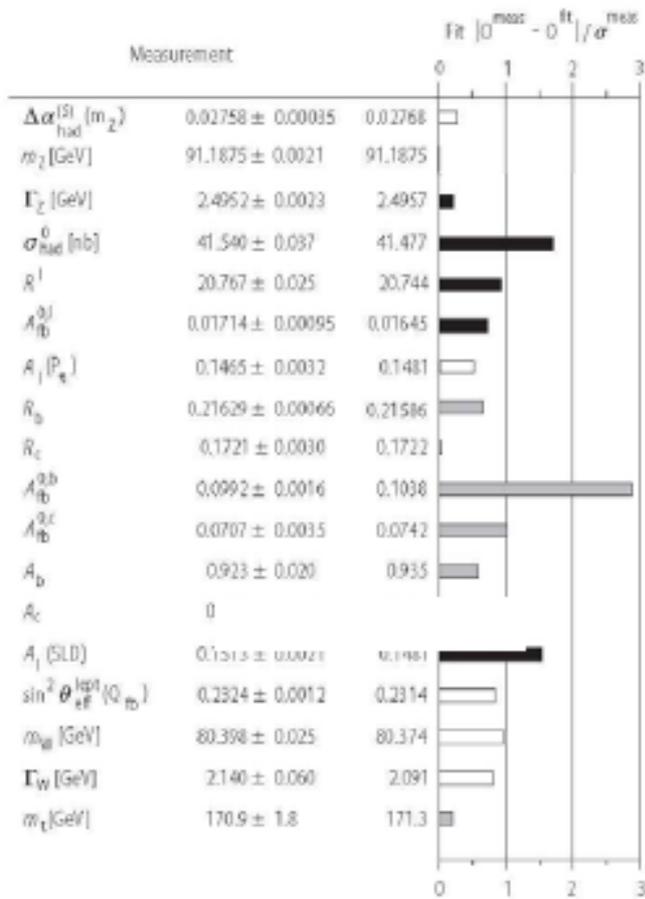
OPAL



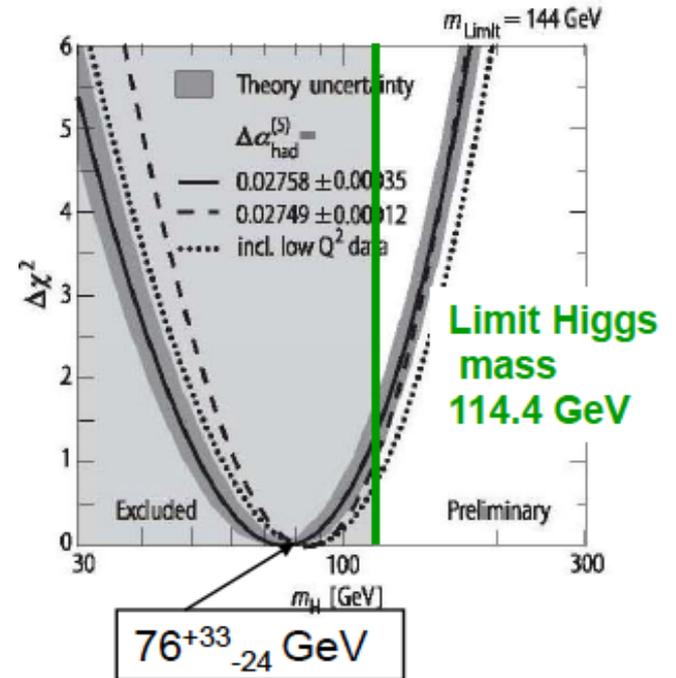
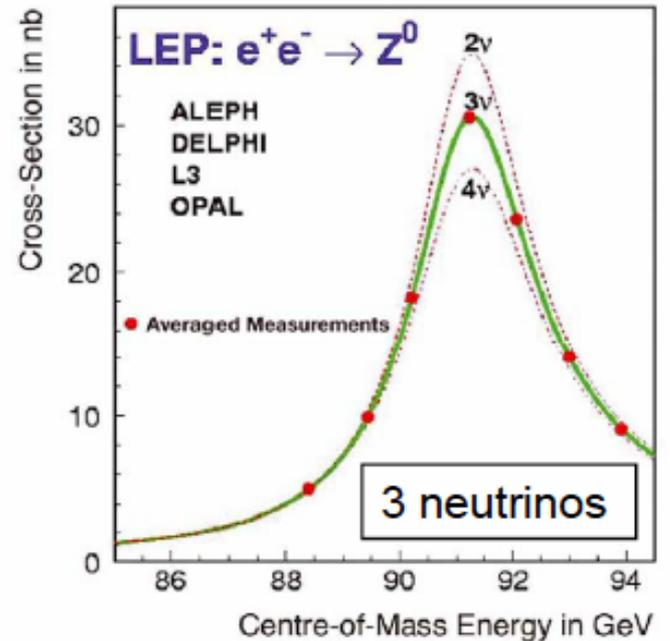
ALEPH

# LEP results

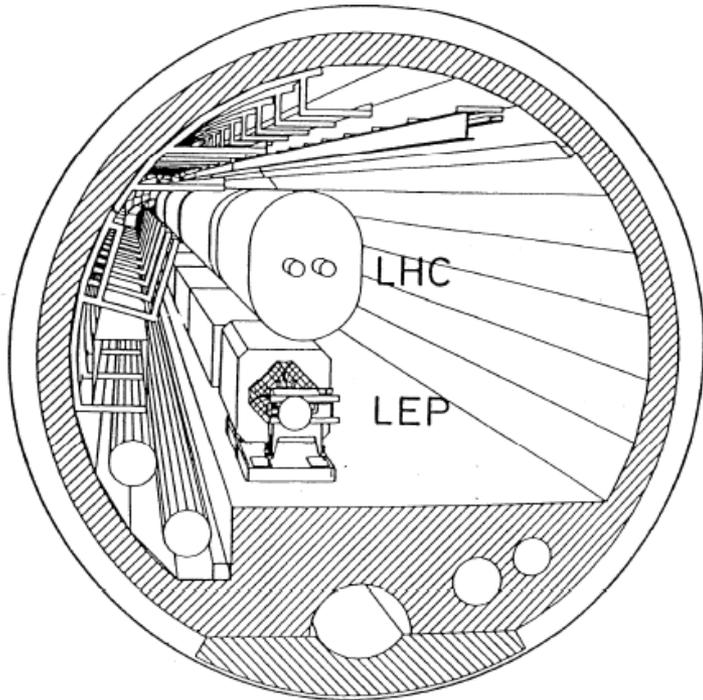
- No sensations (top, Higgs, SUSY), but precision measurement
- LEP turned HEP into precision physics



SM confirmed with <1%



# LEP stopped in 2000...



LARGE HADRON COLLIDER  
IN THE LEP TUNNEL

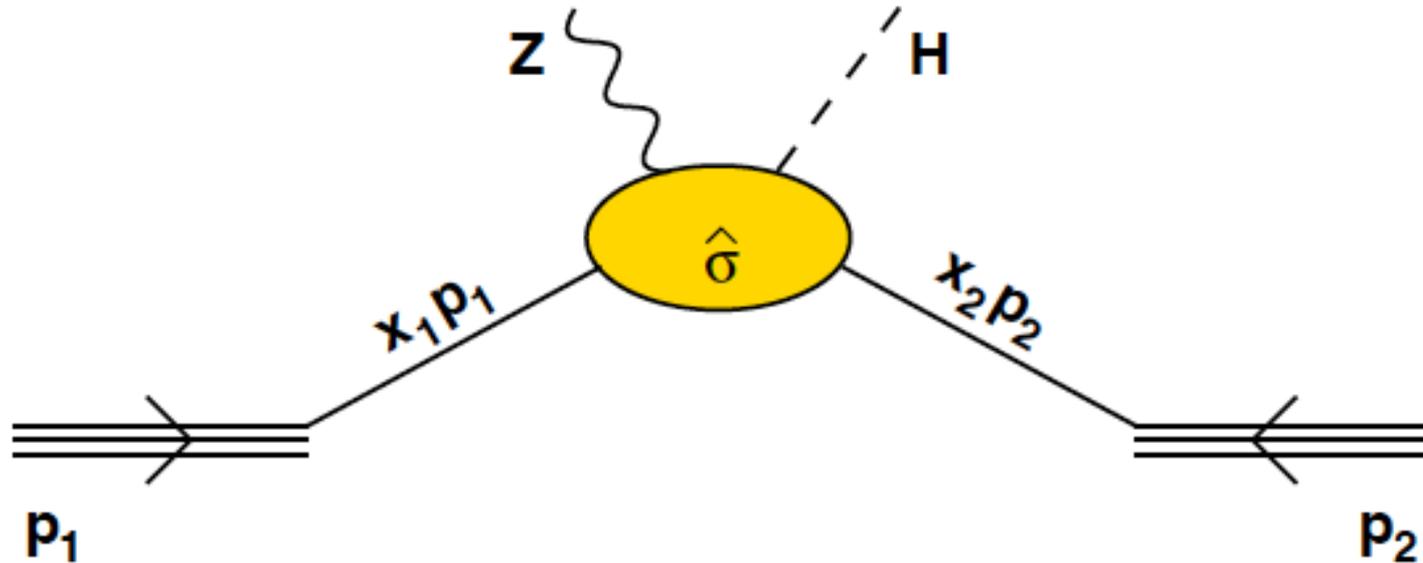


LEP closure 2.November 2000

→ Idea discarded...

# Hadron colliders

# Collisions at hadron colliders



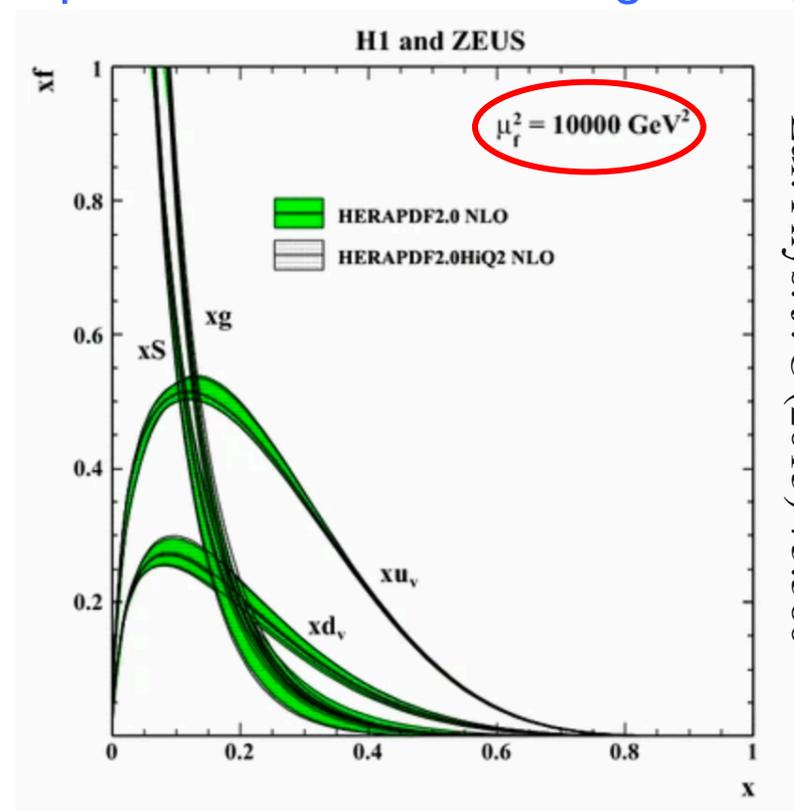
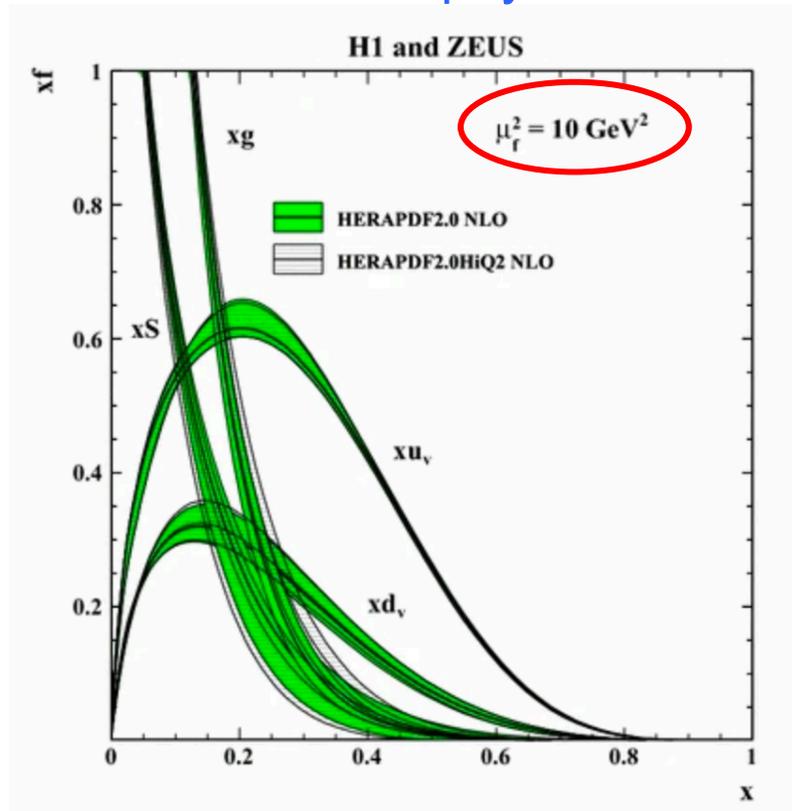
- Calculation of cross section of an interaction process at a hadron collider can be factorized into:

$$\sigma = \int dx_1 f_{q/p}(x_1, \mu^2) \int dx_2 f_{\bar{q}/\bar{p}}(x_2, \mu^2) \hat{\sigma}(x_1 p_1, x_2 p_2, \mu^2), \quad \hat{s} = x_1 x_2 s$$

- Probability for extracting partons with momentum fraction  $x_1, x_2$  (PDFs)
- Hard scattering cross section  $\hat{\sigma}$  at  $\hat{s} \rightarrow$  calculable in pQCD
- Evaluated at factorization scale  $\mu^2$

# Parton Distribution Functions (PDFs)

- PDFs: Probability for a parton to carry the fraction  $x$  of proton momentum
- Intrinsic property of the nucleon, process independent
- Dependence on  $Q^2$
- Precise knowledge of PDFs crucial for physics at hadron colliders
  - Limits accuracy of SM predictions (e.g. Higgs boson production)
  - Reach of new physics searches depends on PDF knowledge at high  $x$



# Properties of PDFs

**x-dependence** of PDFs is not calculable in perturbative QCD

→ parametrise PDFs at the starting scale  $Q_0^2$

**$Q^2$  dependence** is calculable in perturbative QCD:

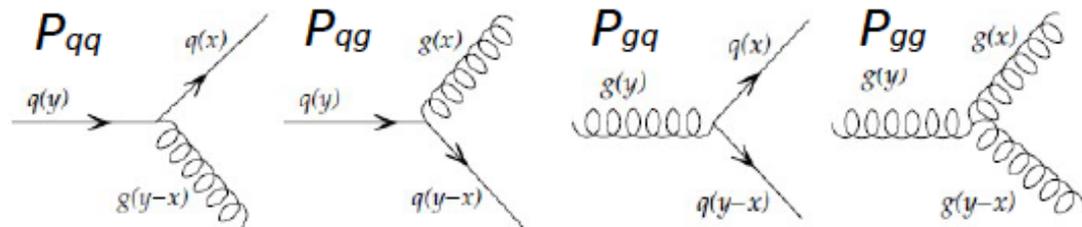
evolve PDFs using **DGLAP** equations to  $Q^2 > Q_0^2$

**DGLAP (Dokshitzer-Gribov-Lipatov-Altarelli-Parisi)** evolution equations:

$$\frac{\partial q(x, Q^2)}{\partial \ln Q^2} \propto \int_x^1 \frac{dz}{z} \left[ q(z, Q^2) P_{qq} \left( \frac{x}{z} \right) + g(z, Q^2) P_{qg} \left( \frac{x}{z} \right) \right]$$

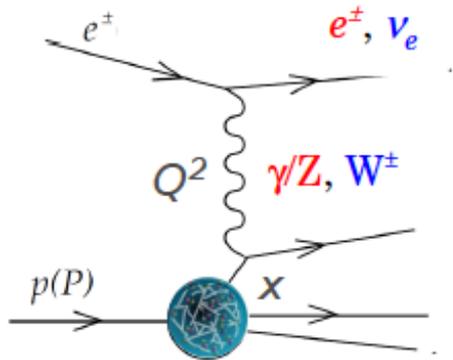
$$\frac{\partial g(x, Q^2)}{\partial \ln Q^2} \propto \int_x^1 \frac{dz}{z} \left[ q(z, Q^2) P_{gq} \left( \frac{x}{z} \right) + g(z, Q^2) P_{gg} \left( \frac{x}{z} \right) \right]$$

Probability via splitting functions:

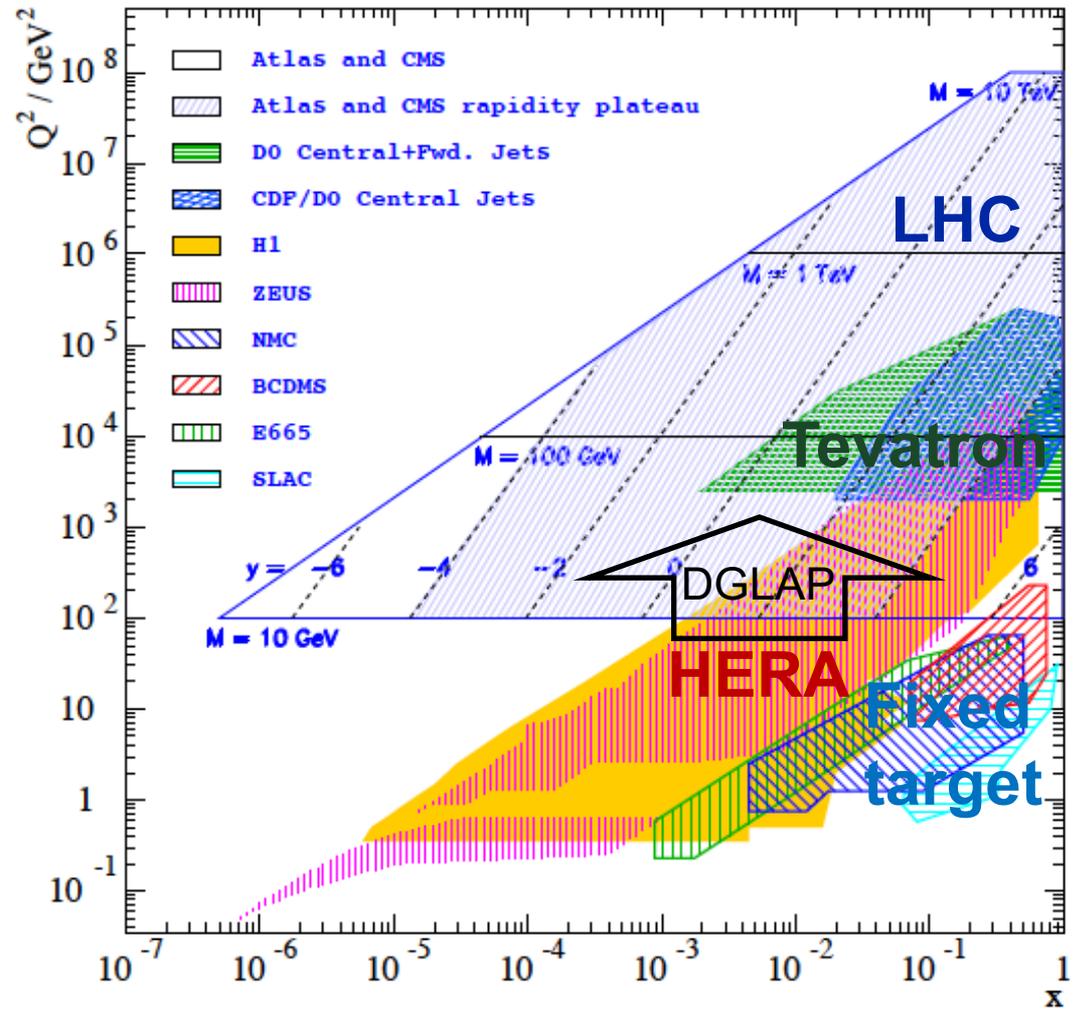


# Experimental data for PDFs

Deep Inelastic Scattering (DIS):  
*unique opportunity to study the structure of the proton (nucleon)*

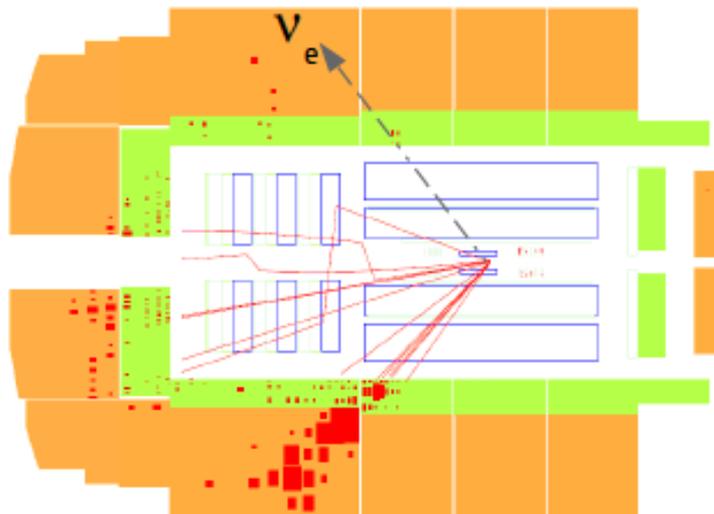


Neutral Current (NC):  $ep \rightarrow eX$   
 Charged Current (CC):  $ep \rightarrow \nu X$



# HERA (1992-2007)

- ep collider at DESY, Hamburg
- Up to now only collider in which two different types of particles were accelerated separately and then brought to collision
- Circumference of 6.3 km
- 4 experiments (H1, ZEUS, Hermes and HERA-B)

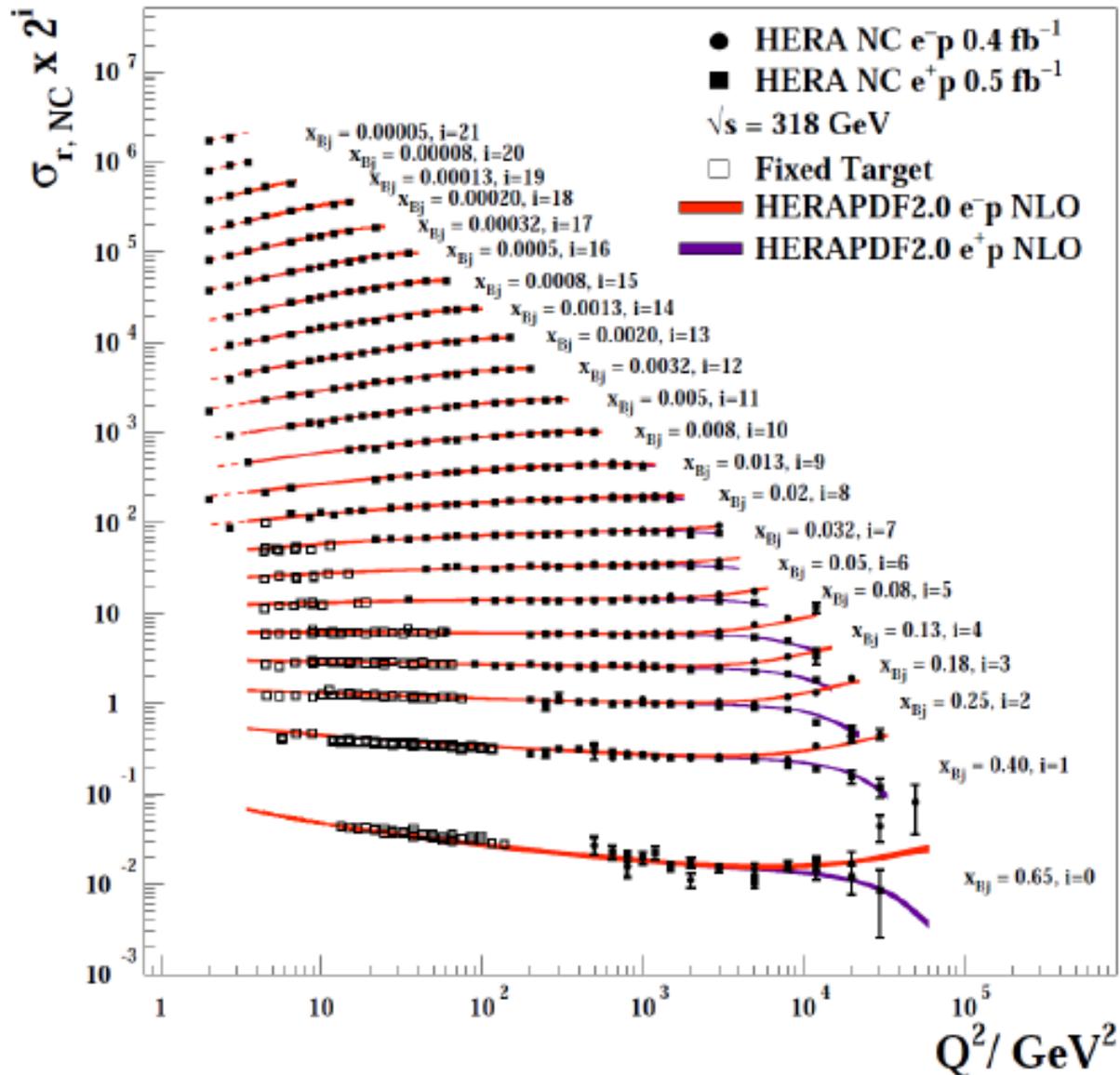


CC event in H1 detector



# Legacy of HERA experiments

## H1 and ZEUS



# Tevatron

- 1972: Main ring (circumference of 6.3km) first operated with conventional magnets → 500 GeV proton beam
- 1981-1986 installation of superconducting magnets → 900 GeV proton beam → first machine to reach collisions at  $\sqrt{s} > 1$  TeV (hence the name)

## Run I 1992 - 1996

$\sqrt{s} = 1.8$  TeV

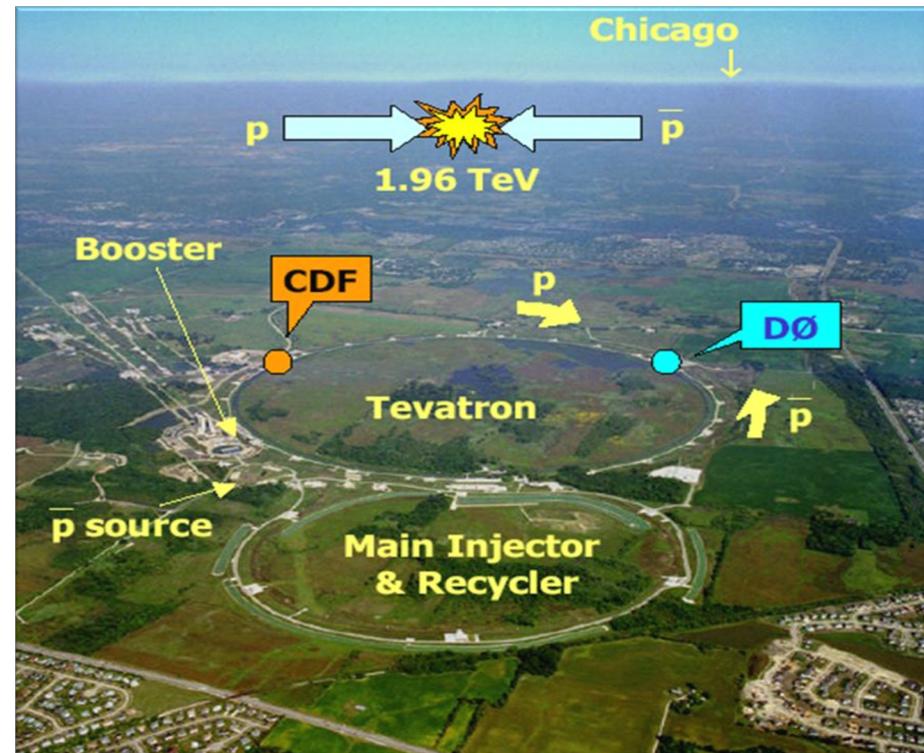
Integrated luminosity 110 pb<sup>-1</sup>

- 1993-1999 addition of main injector → 980 GeV proton beam, higher inst. luminosity

## Run II 2001 - 2011

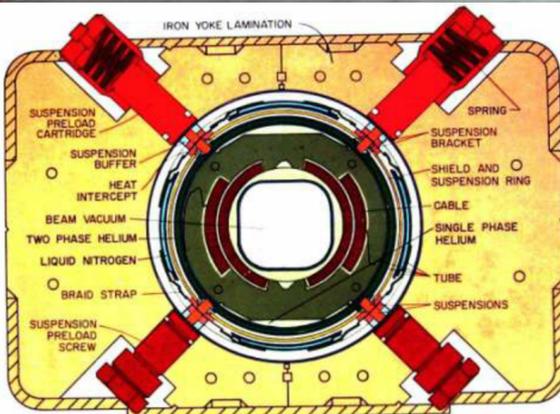
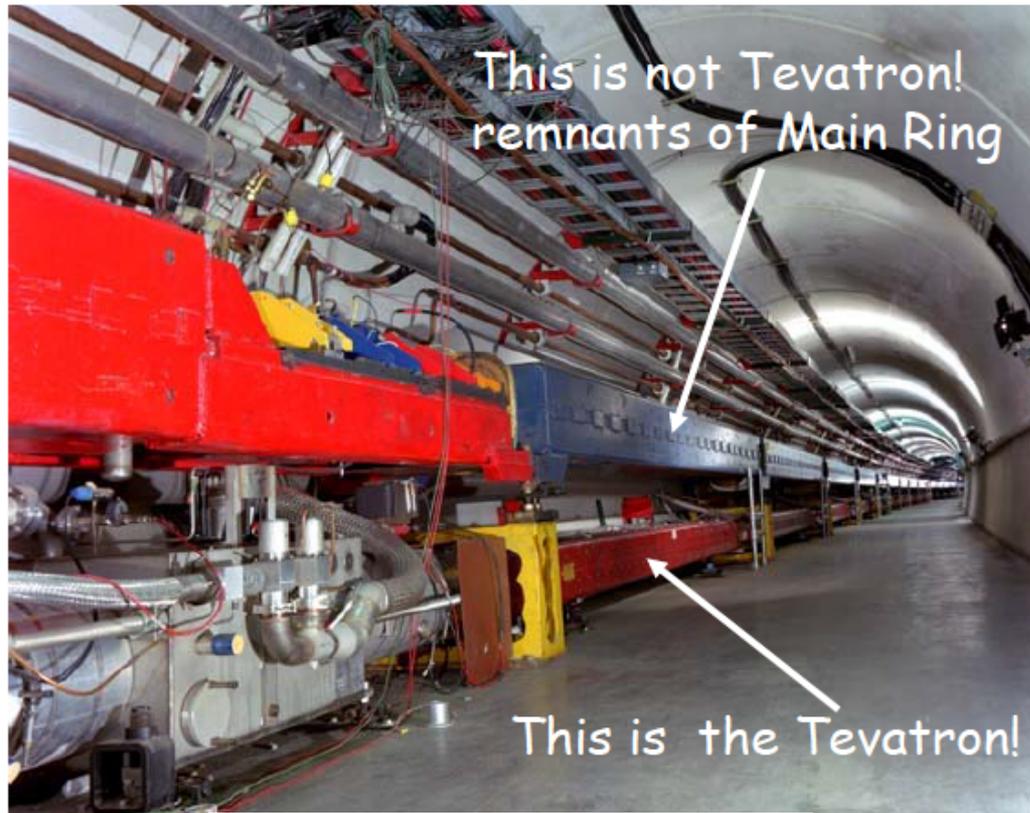
$\sqrt{s} = 1.96$  TeV

Integrated luminosity 1 fb<sup>-1</sup>



# Tevatron

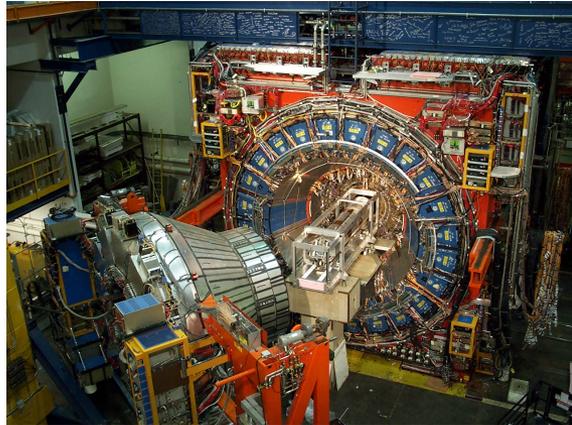
- $p\bar{p}$  collider
- Same magnets used for acceleration and storage of both beams
- Single beam pipe  $\rightarrow$   $p/\bar{p}$  placed on different orbits
- $B_{\max} = 4.5\text{T}$
- $E = 980\text{ GeV}$
- $E_{\text{inj}} = 150\text{ GeV}$
- 36 + 36 bunches
- $2.9(1.0)\times 10^{11}$   $p(\bar{p})$  per bunch
- $L_{\text{inst}}^{\max} = 4\times 10^{32}\text{cm}^{-2}\text{s}^{-1}$



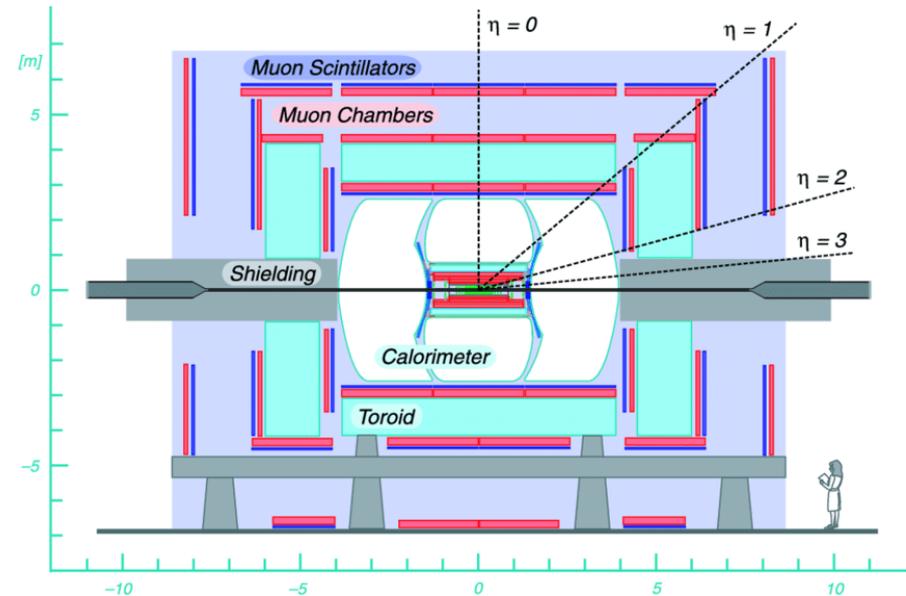
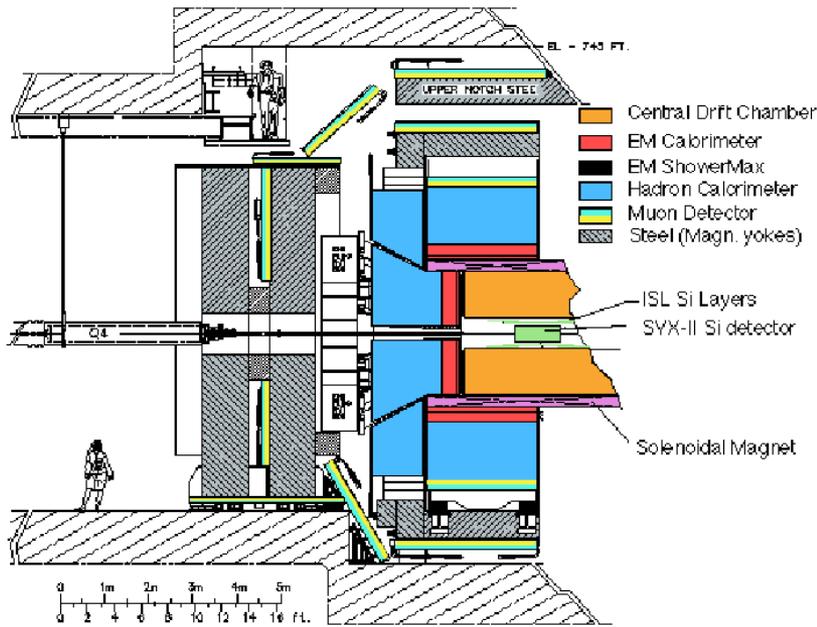
# Tevatron experiments

- Two multipurpose experiments CDF and D0
- Tracking and silicon vertex detector added for Run 2

CDF

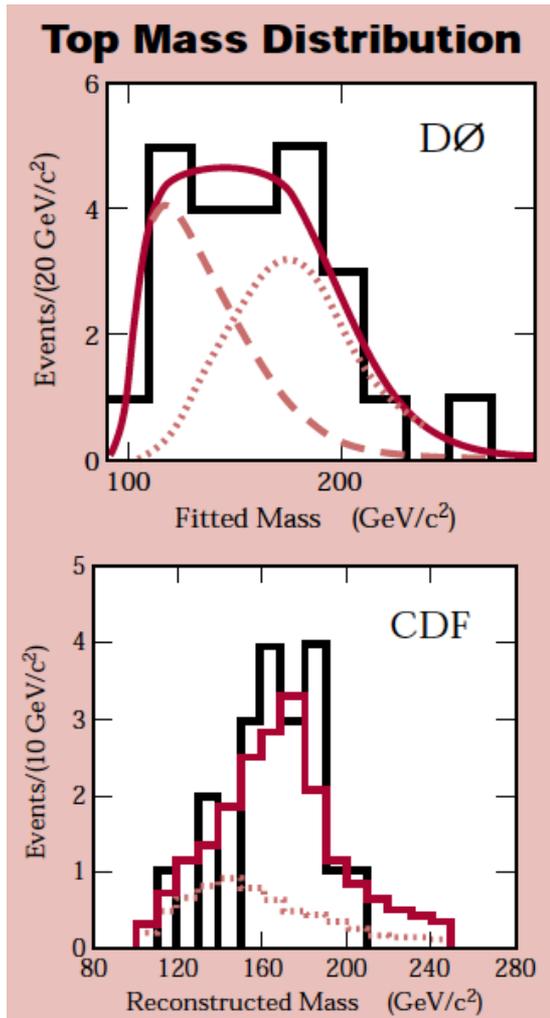


D0

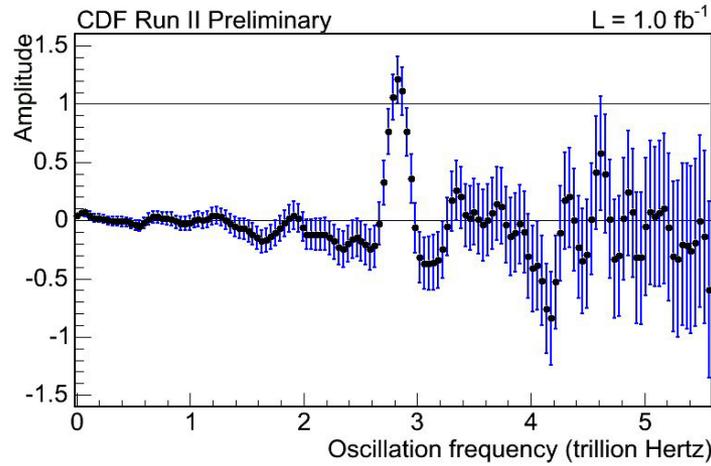


# Legacy of Tevatron experiments

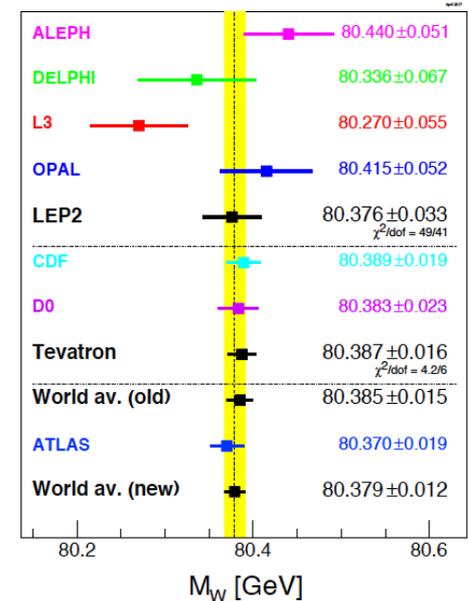
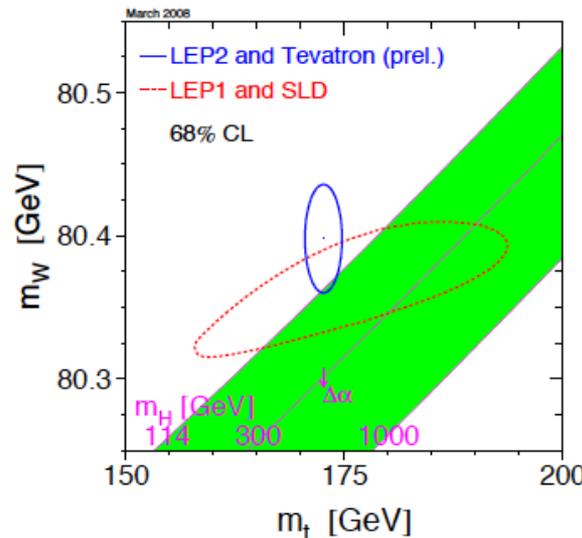
Top quark discovery  
1995



Discovery of B<sub>s</sub> oscillations 2006



W mass measurement 2008



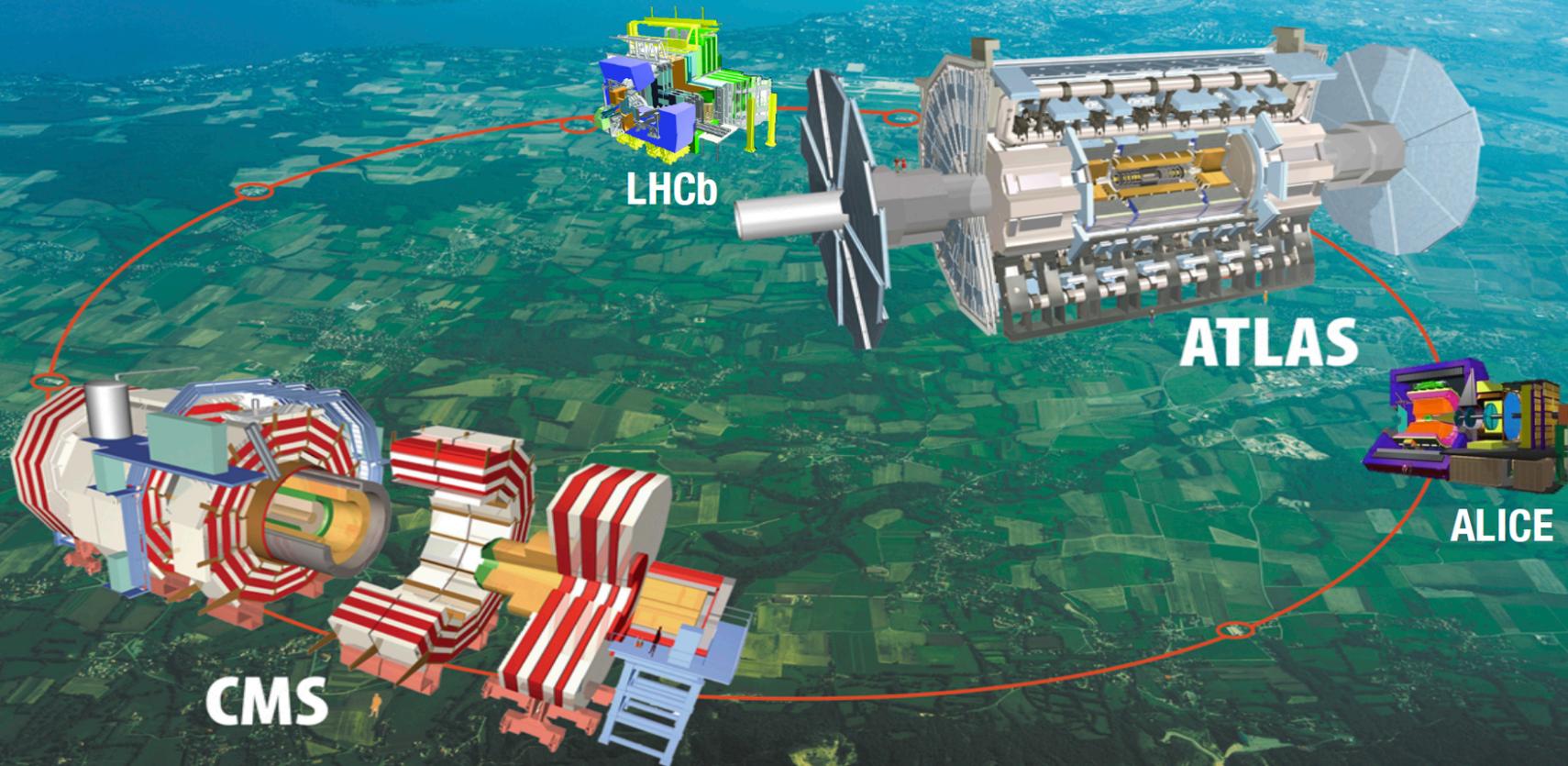
# Superconducting Super Collider (SSC)

- SSC proposed by US HEP community and approved by President Reagan in 1987
  - 20+20 TeV pp collider in 87 km long tunnel in Texas
- Asked for international participation because of high cost
  - Denied as no participation in the design was possible
- 22.5 km of tunnel bored by 1993 when project got cancelled by US Congress
  - Many reasons...
- “Great tragedy of science”

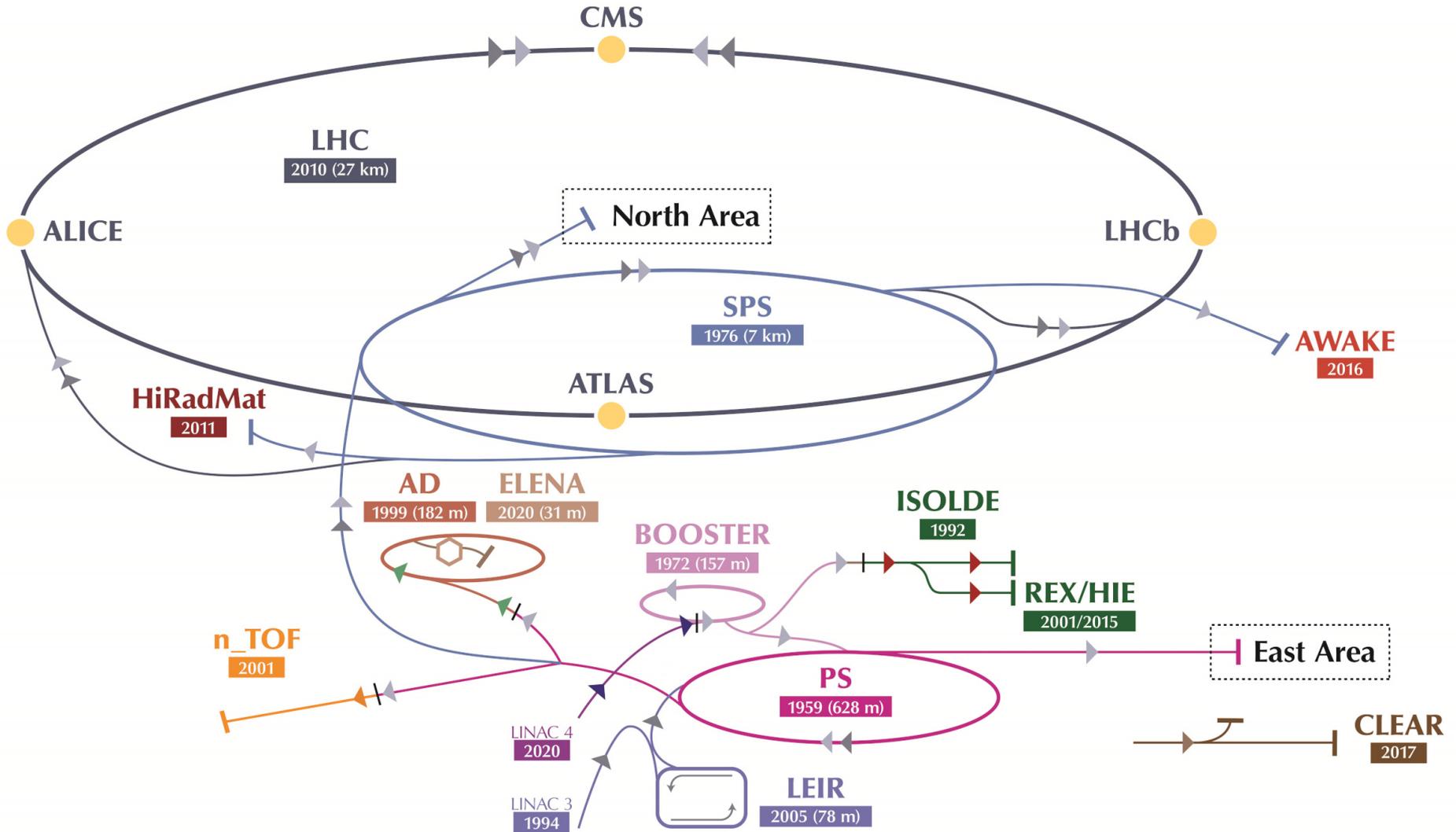


# The Large Hadron Collider (LHC)

27 km circumference proton-proton collider at CERN  
Largest and highest energy accelerator ever built  
Started operation in 2010



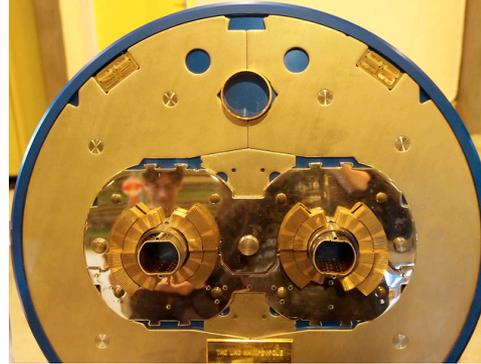
# CERN accelerator complex



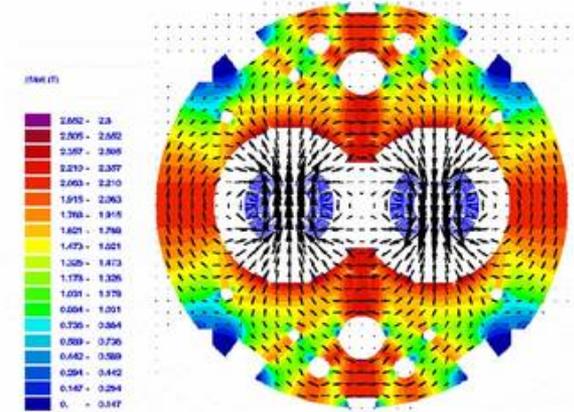
# LHC

- 9300 magnets
- 1232 dipole magnets
- $B_{\max} = 8.3\text{T}$
- "2 in 1" concept:  
both beams share same mechanical structure and cryostat (1.9K)
- $E = 7\text{ TeV}$
- $E_{\text{inj}} = 450\text{ GeV}$

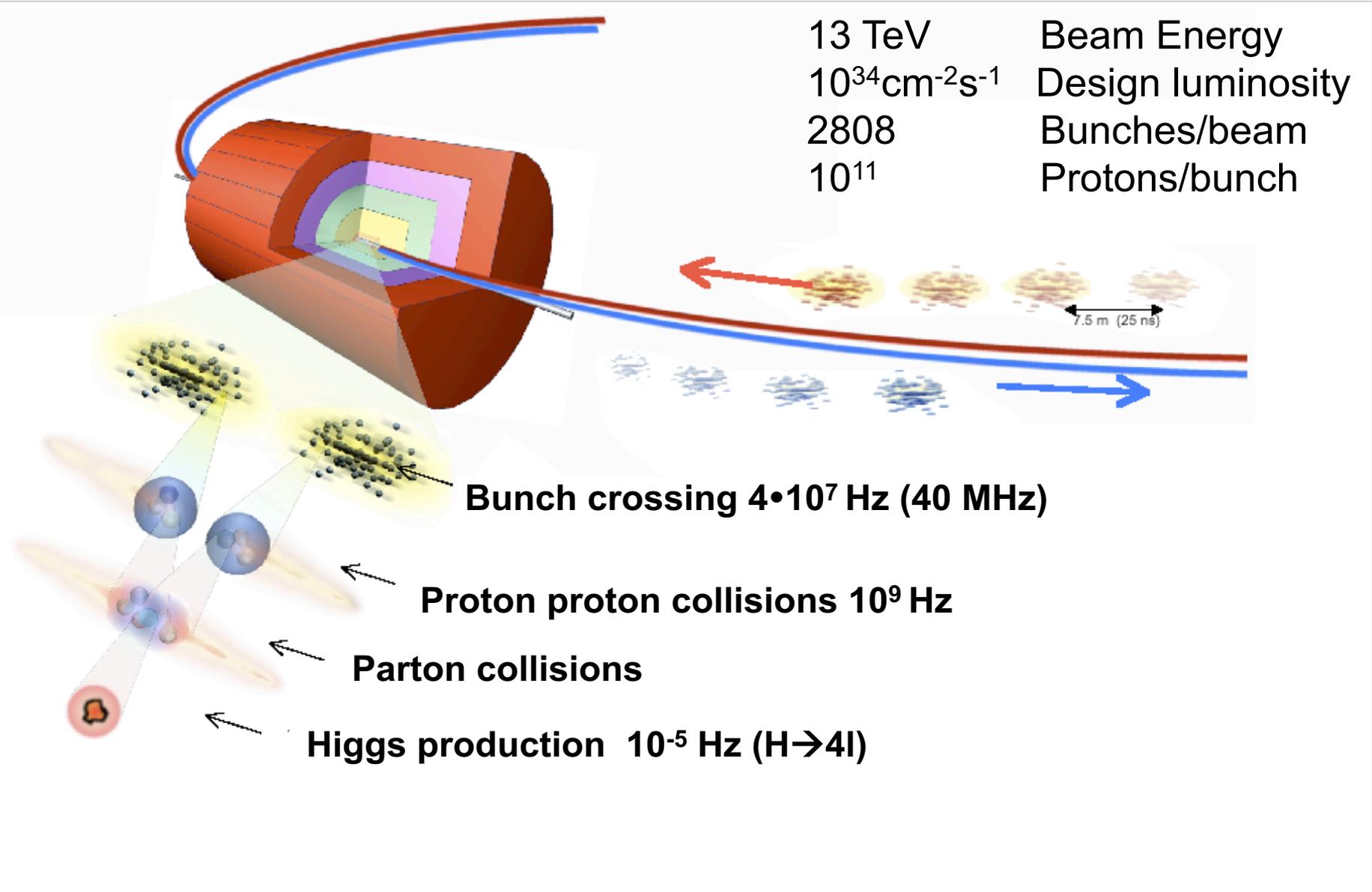
Dipole cross section



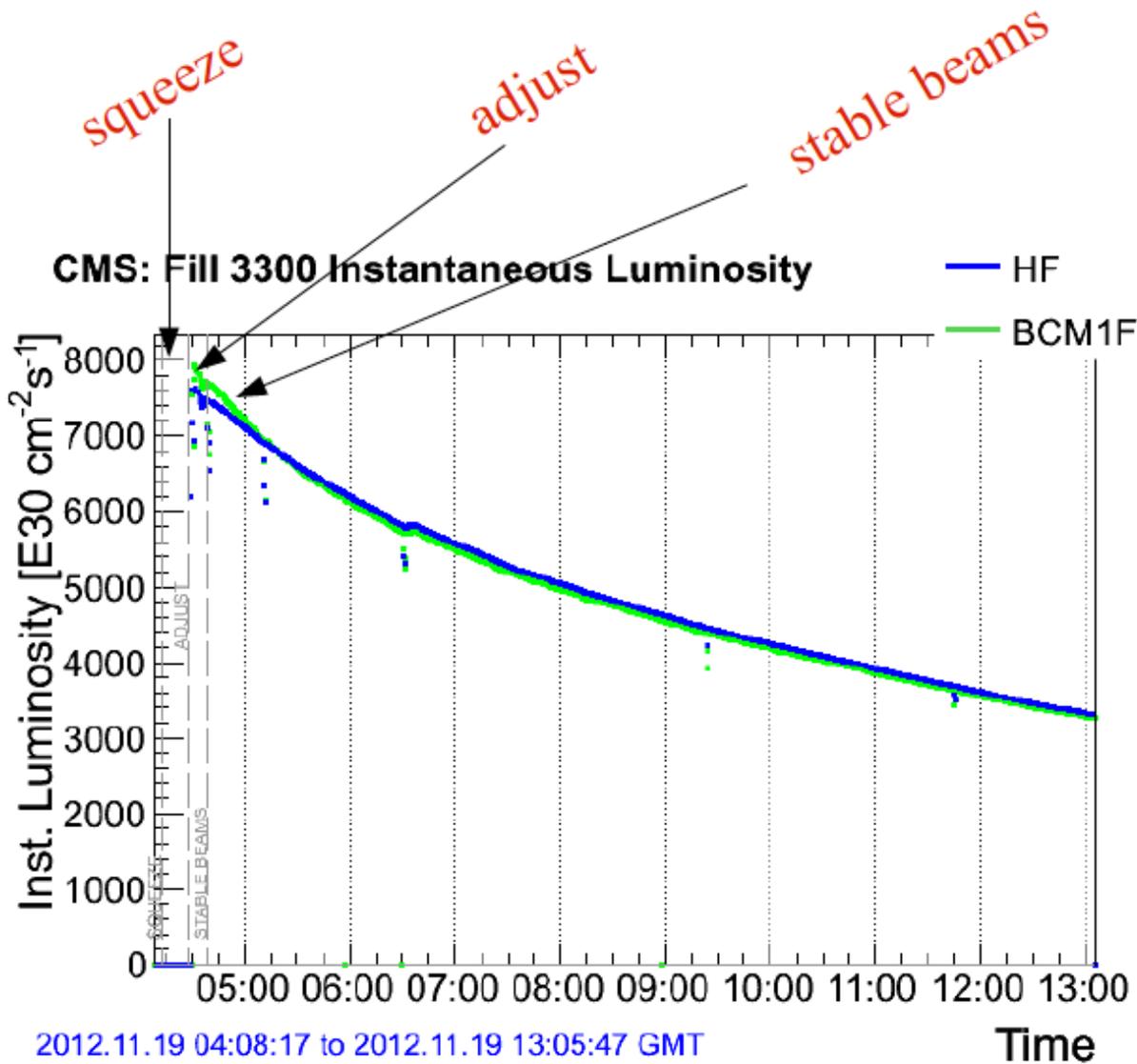
magnetic field configuration



# LHC parameters



# LHC Fill

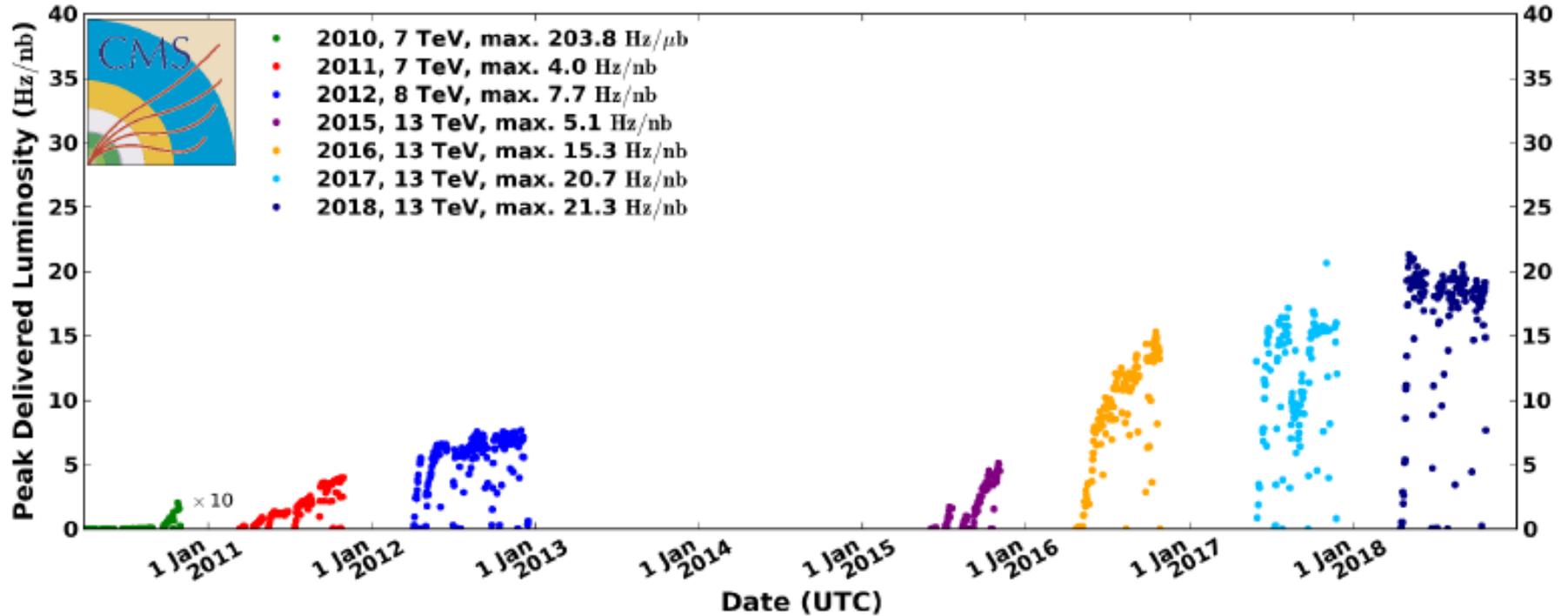


- An LHC fill usually lasts a few hours
- After injection and acceleration, the beams are
  - first, focused
  - then, brought into collision
- LHC then “declares stable beams” → experiments start data-taking
- Luminosity decreases over the course of the run
- Divide run into “luminosity sections” (also called “luminosity blocks”)

# LHC luminosity

## CMS Peak Luminosity Per Day, pp

Data included from 2010-03-30 11:22 to 2018-10-24 04:00 UTC



$$1 \text{ Hz/nb} = 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$$

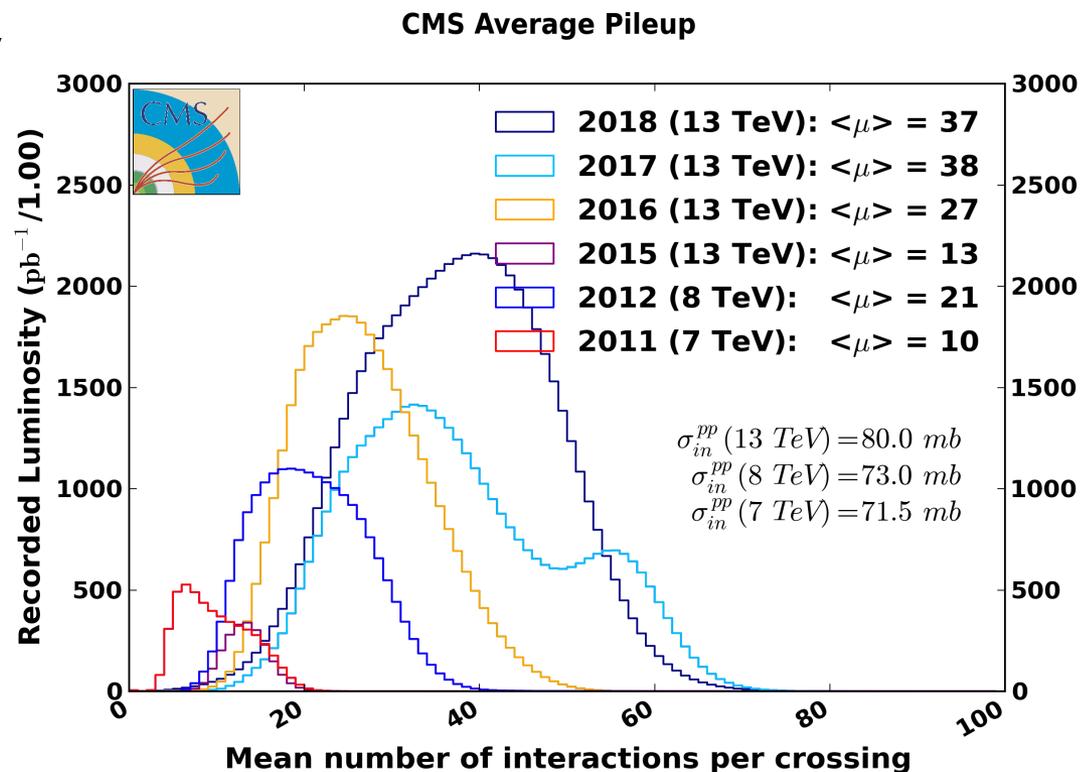
# Pileup

- Average number of proton-proton collisions per bunch crossing

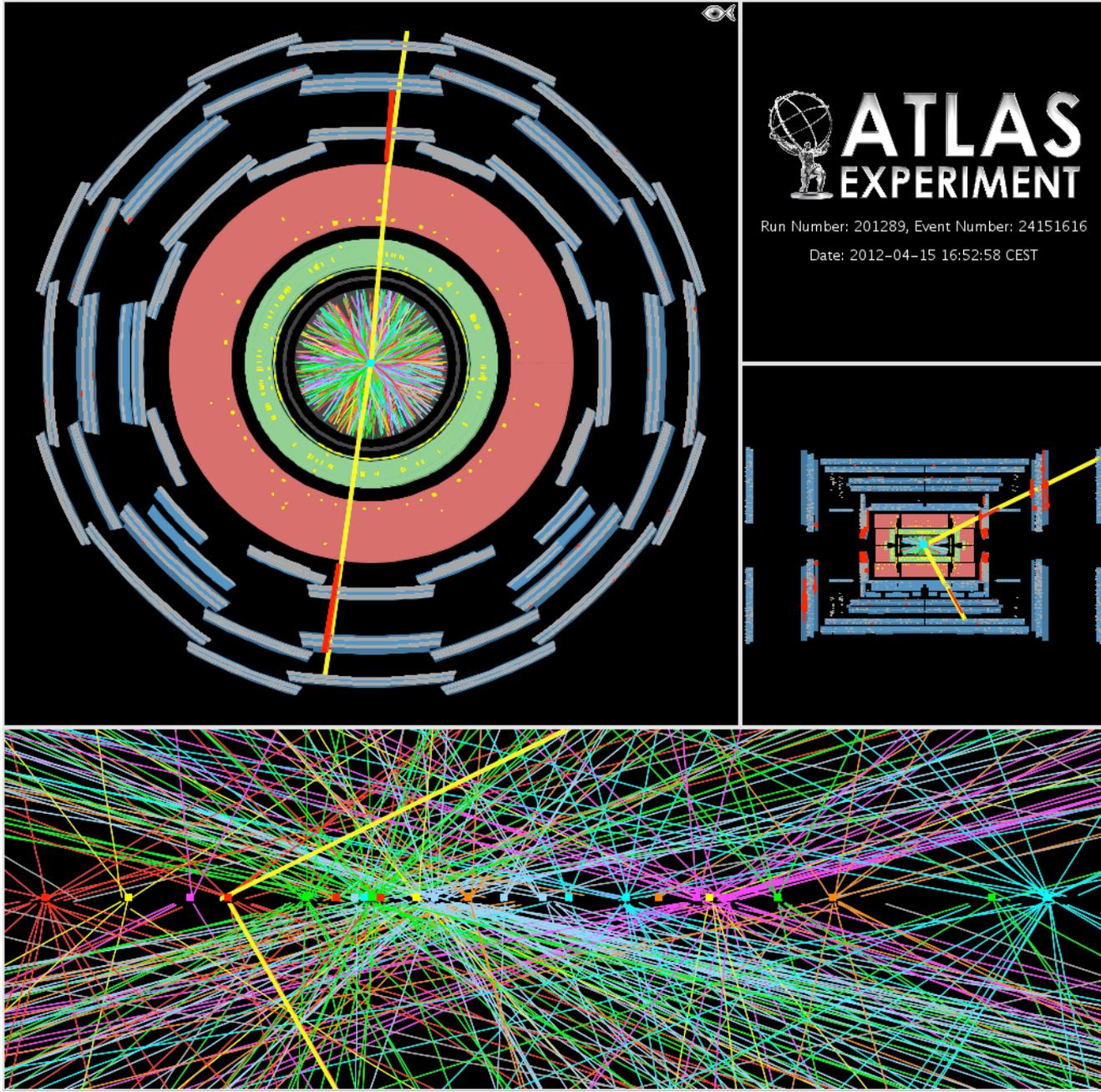
$$\mu(t) = \frac{\sigma \mathcal{L}(t)}{f n_b}$$

- $\sigma$ : inelastic proton-proton cross section
- $\mathcal{L}$ : instantaneous luminosity
- $f$ : revolution frequency
- $n_b$ : number of bunches

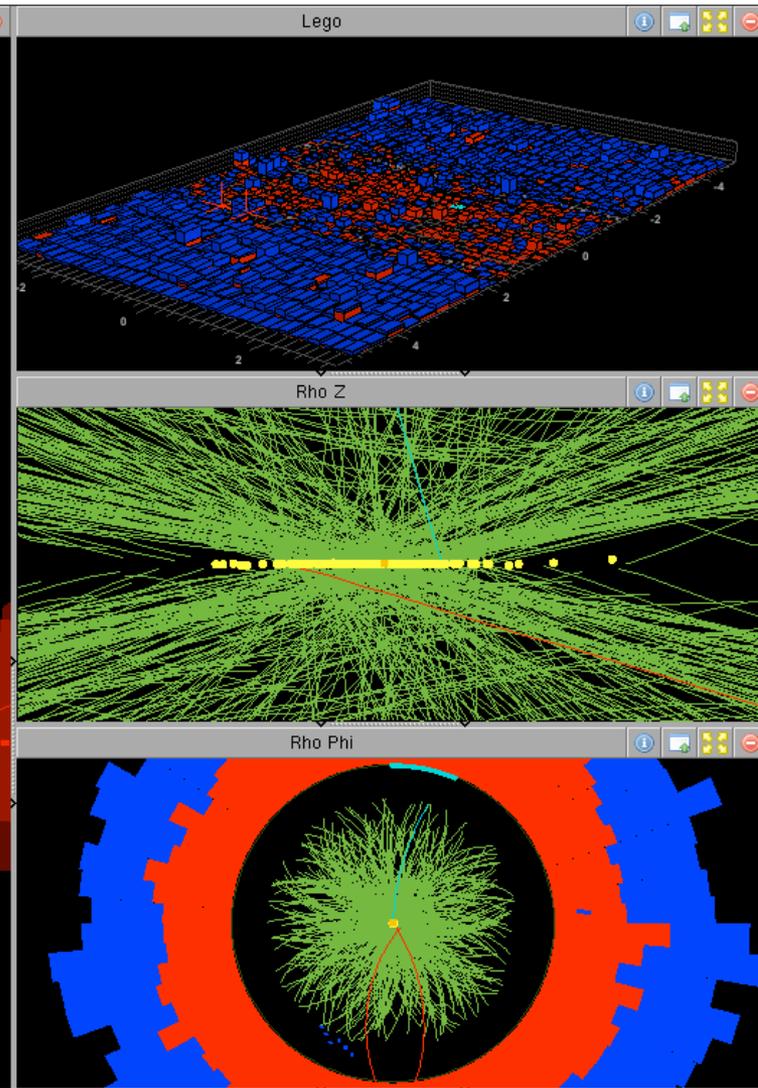
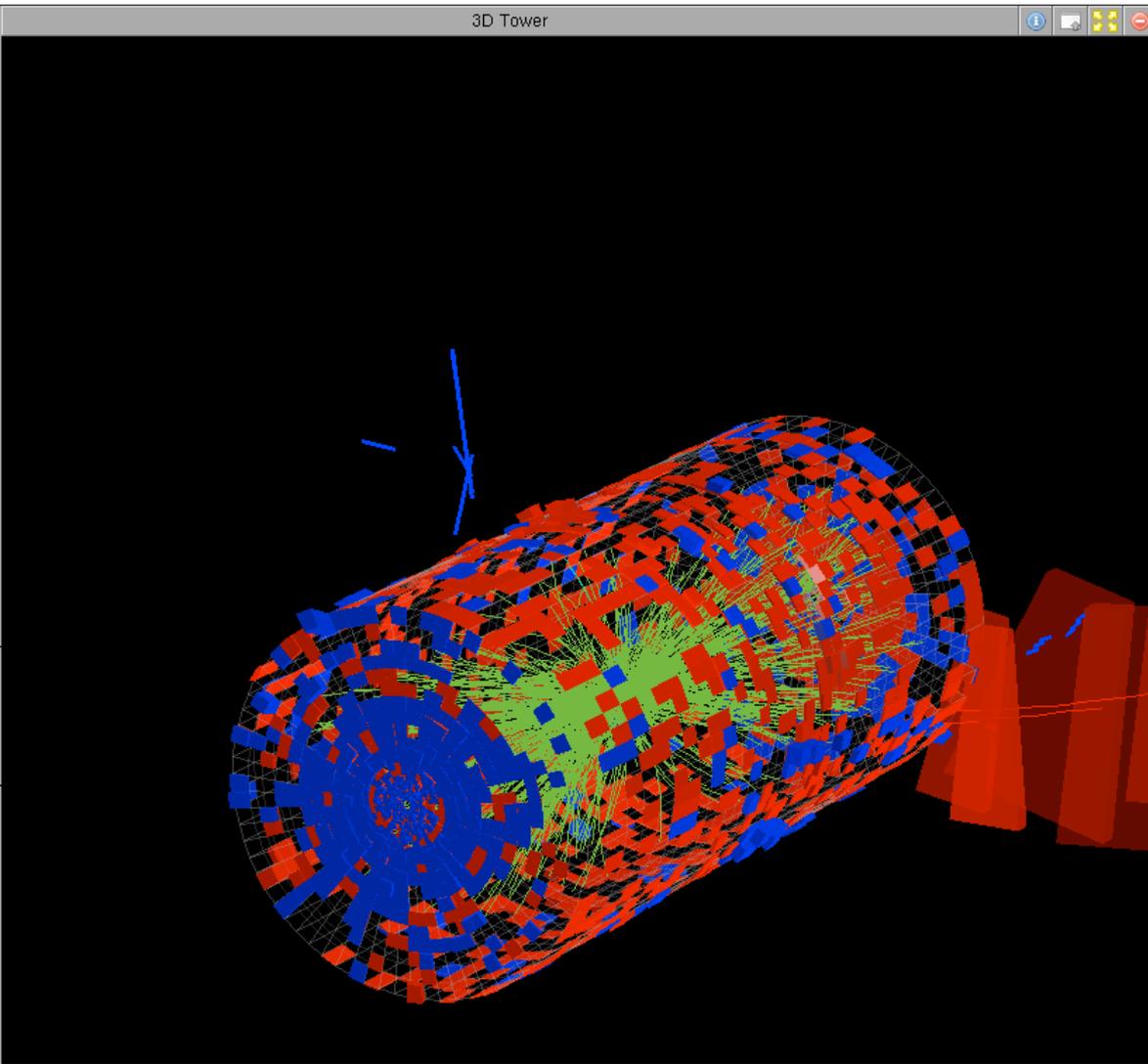
→ Major challenge for physics at the LHC experiments



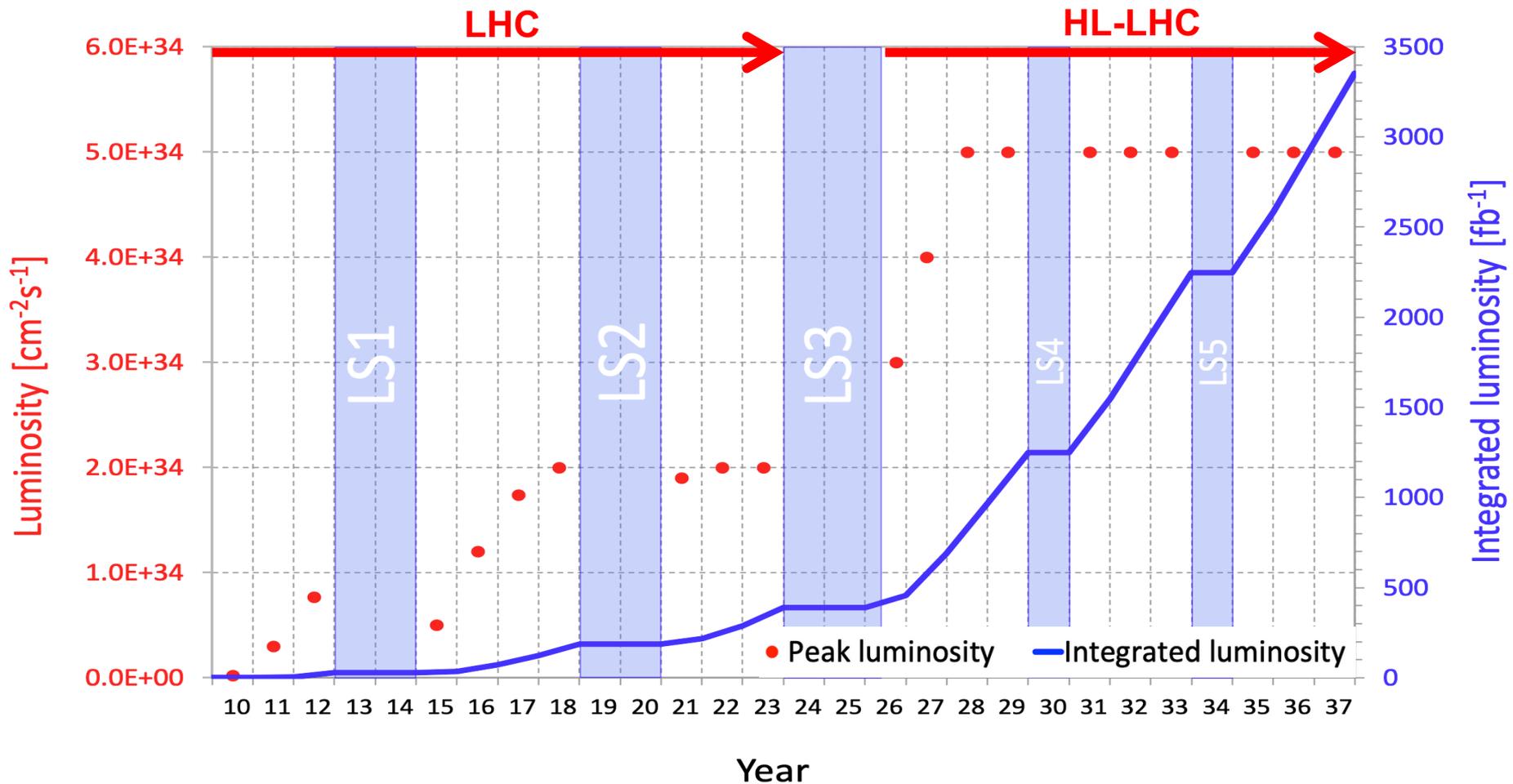
# Pileup in ATLAS



# Pileup in CMS



# From LHC to HL-LHC



- High-luminosity LHC upgrade enables experiments to increase data set by one order of magnitude!  
→ Need improved detectors to make best use of it in physics analysis

# References

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