

Discussion on $9^{\rm th}$ March

Due on 16th March

Exercise 1 Laue method

Estimate the maximal possible number of interference maxima of a Laue recording. Assume that the voltage of the X-ray tube is 60 kV and the crystal is simple cubic with a lattice constant of 0.2 nm. The X-ray tube produces a continuous spectrum of Bremsstrahlung.

Exercise 2 Debye-Scherrer method

Powder specimens of three different monoatomic cubic crystals are analysed with a Debye-Scherrer camera. It is known that one sample is face-centred cubic, one is body-centred cubic and one has the diamond structure. The approximate positions of the first four diffraction rings in each case are given in table 1. The meaning of the angle ϕ is shown in figure 1. Pay attention to the definition of the angle in Bragg's law and the definition of the angle in the figure.

А	В	С
42.2°	28.8°	42.8°
49.2°	41.0°	73.2°
72.0°	50.8°	89.0°
87.3°	59.6°	115.0°

Table 1: The angles ϕ of the diffraction rings in samples A, B, and C.

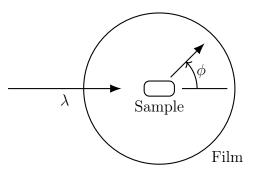


Figure 1: The working principle of a Debye-Scherrer camera.

(a) Identify the crystal structure of A, B, and C.

(b) If the wavelength of the incident X-ray beam is 1.5 Å, what is the length of the side of the conventional cubic cell in each case?

(c) If the diamond structure were replaced by a zincblende structure with a cubic unit cell of the same side, at what angles would the first four rings now occur?

a) The Yukawa potential

$$V(r) = V_0 \frac{e^{-\mu r}}{\mu r} \tag{1}$$

describes the nucleon-nucleon interactions in the atomic nucleus. Its typical reach is $1/\mu$. Calculate the differential scattering cross section

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\omega} = \left| f(\vec{k}, \vec{k}') \right|^2,$$

where

$$f(\vec{k},\vec{k}') = -\frac{m}{2\pi\hbar^2} \int e^{i(\vec{k}-\vec{k}')\cdot\vec{r}} V(\vec{r}) \,\mathrm{d}^3r.$$

The result should (hopefully) be:

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\omega} = \left(\frac{2mV_0}{\mu\hbar^2}\right)^2 \frac{1}{[2k^2(1-\cos\Theta)+\mu^2]^2}.$$
(2)

b) Derive the scattering cross section for the Coulomb potential by considering the limit $\mu \to 0$ with

$$\frac{V_0}{\mu} = \frac{Ze^2}{4\pi\epsilon_0}$$

fixed. (Plug this into equation (2).) Why is it necessary to compute the case for the Yukawa potential first? Why do we not take the Coulomb potential in equation (1)?