

Physik-Institut

Kern- und Teilchenphysik II Lecture 3: Weak Interaction

(adapted from the Handout of Prof. Mark Thomson)

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www.physik.uzh.ch/de/lehre/PHY213/FS2017.html



Parity

★The parity operator performs spatial inversion through the origin: $\Psi'(\vec{x},t) = \hat{P}\Psi(\vec{x},t) = \Psi(-\vec{x},t)$ •applying \hat{P} twice: $\hat{P}\hat{P}\psi(\vec{x},t) = \hat{P}\psi(-\vec{x},t) = \psi(\vec{x},t)$ so $\hat{P}\hat{P} = I \implies \hat{P}^{-1} = \hat{P}$ To preserve the normalisation of the wave-function $\langle \boldsymbol{\psi} | \boldsymbol{\psi} \rangle = \langle \boldsymbol{\psi}' | \boldsymbol{\psi}' \rangle = \langle \boldsymbol{\psi} | \hat{P}^{\dagger} \hat{P} | \boldsymbol{\psi} \rangle$ $\hat{P}^{\dagger}\hat{P} = I \longrightarrow \hat{P}$ Unitary • But since $\hat{P}\hat{P} = I$ $\hat{P} = \hat{P}^{\dagger}$ \rightarrow \hat{P} Hermitian which implies Parity is an observable quantity. If the interaction Hamiltonian commutes with \hat{P} , parity is an observable conserved quantity • If $\psi(\vec{x},t)$ is an eigenfunction of the parity operator with eigenvalue P $\hat{P}\psi(\vec{x},t) = P\psi(\vec{x},t) \qquad \implies \qquad \hat{P}\hat{P}\psi(\vec{x},t) = P\hat{P}\psi(\vec{x},t) = P^2\psi(\vec{x},t)$ since $\hat{P}\hat{P} = I$ $P^2 = 1$ \rightarrow Parity has eigenvalues $P = \pm 1$ **★ QED** and QCD are invariant under parity

★ Experimentally observe that Weak Interactions do not conserve parity



Intrinsic Parity

Intrinsic Parities of fundamental particles:

Spin-1 Bosons

•From Gauge Field Theory can show that the gauge bosons have P = -1

$$P_{\gamma} = P_g = P_{W^+} = P_{W^-} = P_Z = -1$$

Spin-¹/₂ Fermions

From the Dirac equation showed (see Dirac Equation Lectures in KTI): Spin ½ particles have opposite parity to spin ½ anti-particles
Conventional choice: spin ½ particles have P = +1 P_e- = P_μ- = P_τ- = P_ν = P_q = +1 and anti-particles have opposite parity, i.e.

$$P_{e^+} = P_{\mu^+} = P_{\tau^+} = P_{\overline{v}} = P_{\overline{q}} = -1$$

★ For Dirac spinors it was shown that the parity operator is:

$$\hat{P} = \gamma^0 = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$



Parity conservation

•Consider the QED process $e^-q \rightarrow e^-q$ •The Feynman rules for QED give: $-iM = [\overline{u}_e(p_3)ie\gamma^{\mu}u_e(p_1)]\frac{-ig_{\mu\nu}}{q^2}[\overline{u}_q(p_4)ie\gamma^{\nu}u_q(p_2)]$ •Which can be expressed in terms of the electron and quark 4-vector currents: $M = -\frac{e^2}{q^2}g_{\mu\nu}j_e^{\mu}j_q^{\nu} = -\frac{e^2}{q^2}j_e.j_q$ with $j_e = \overline{u}_e(p_3)\gamma^{\mu}u_e(p_1)$ and $j_q = \overline{u}_q(p_4)\gamma^{\mu}u_q(p_2)$

★Consider the what happen to the matrix element under the parity transformation

Spinors transform as

$$u \stackrel{\hat{P}}{\to} \hat{P}u = \gamma^0 u$$

Adjoint spinors transform as

$$\overline{u} = u^{\dagger} \gamma^{0} \xrightarrow{\hat{P}} (\hat{P}u)^{\dagger} \gamma^{0} = u^{\dagger} \gamma^{0\dagger} \gamma^{0} = u^{\dagger} \gamma^{0} \gamma^{0} = \overline{u} \gamma^{0}$$
$$\overline{u} \xrightarrow{\hat{P}} \overline{u} \gamma^{0}$$
$$\boxed{u} \xrightarrow{\hat{P}} \overline{u} \gamma^{0}$$
$$Ience \quad j_{e} = \overline{u}_{e}(p_{3}) \gamma^{\mu} u_{e}(p_{1}) \xrightarrow{\hat{P}} \overline{u}_{e}(p_{3}) \gamma^{0} \gamma^{\mu} \gamma^{0} u_{e}(p_{1})$$

+



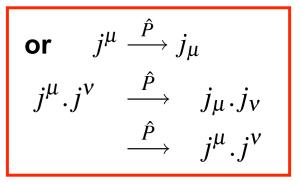
Parity Conservation

★ Consider the components of the four-vector current

$$\begin{array}{ccc} \mathbf{0:} & j_e^0 \xrightarrow{P} \overline{u} \gamma^0 \gamma^0 \gamma^0 u = \overline{u} \gamma^0 u = j_e^0 & \text{since } \gamma^0 \gamma^0 = 1 \\ & k \xrightarrow{\hat{P}} - 0 k k 0 & -k k 0 k 0 & -k k k 0 \\ \end{array}$$

- $j_e^k \xrightarrow{\hat{P}} \overline{u} \gamma^0 \gamma^k \gamma^0 u = -\overline{u} \gamma^k \gamma^0 \gamma^0 u = -\overline{u} \gamma^k u = -j_e^k \quad \text{since} \quad \gamma^0 \gamma^k = -\gamma^k \gamma^0$
- •The time-like component remains unchanged and the space-like components change sign
- •Similarly $j_q^0 \xrightarrow{\hat{P}} j_q^0 \longrightarrow j_q^k \longrightarrow -j_q^k \quad k = 1, 2, 3$
- **★** Consequently the four-vector scalar product

$$j_e.j_q = j_e^0 j_q^0 - j_e^k j_q^k \xrightarrow{\hat{P}} j_e^0 j_q^0 - (-j_e^k)(-j_q^k) = j_e.j_q \quad k = 1,3$$



QED Matrix Elements are Parity Invariant

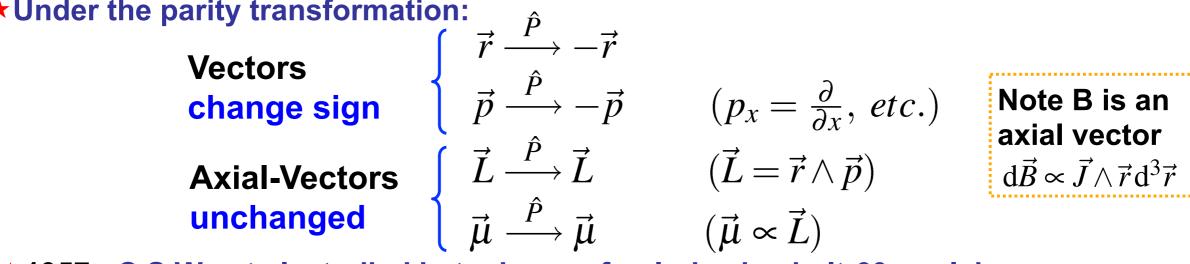
Parity Conserved in QED

★ The QCD vertex has the same form and, thus,

Parity Conserved in QCD

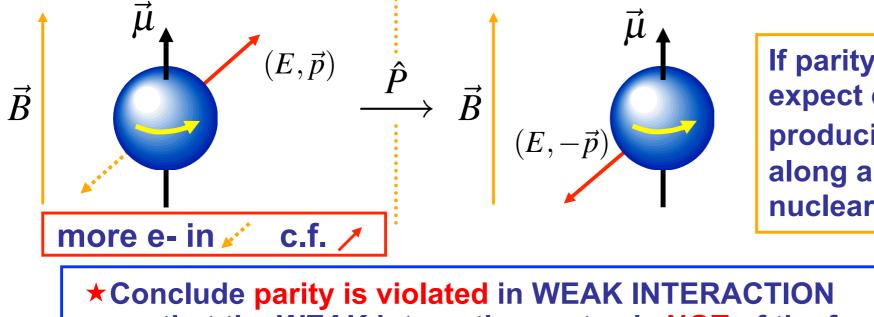
Universität Zürich¹²¹ Parity Violation in Beta decays

★The parity operator \hat{P} corresponds to a discrete transformation $x \to -x$, *etc*. **★**Under the parity transformation:



★1957: C.S.Wu et al. studied beta decay of polarized cobalt-60 nuclei: ${}^{60}\text{Co} \rightarrow {}^{60}Ni^* + e^- + \overline{\nu}_e$

*****Observed electrons emitted preferentially in direction opposite to applied field



If parity were conserved: expect equal rate for producing e⁻ in directions along and opposite to the nuclear spin.

*Conclude parity is violated in WEAK INTERACTION \rightarrow that the WEAK interaction vertex is NOT of the form $\overline{u}_e \gamma^\mu u_V$



Bilinear Covariants

★ The requirement of Lorentz invariance of the matrix element severely restricts the form of the interaction vertex. QED and QCD are "VECTOR" interactions:

$$j^{\mu} = \overline{\psi} \gamma^{\mu} \phi$$

- ★This combination transforms as a 4-vector
- ★ In general, there are only 5 possible combinations of two spinors and the gamma matrices that form Lorentz invariant currents, called "bilinear covariants":

Туре	Form	Components	"Boson Spin"
SCALAR	$\overline{\psi}\phi_{}$	1	0
PSEUDOSCALAR	$\overline{\psi}\gamma^5\phi$	1	0
VECTOR	$\overline{\psi}\gamma^{\mu}\phi$	4	1
AXIAL VECTOR	$\overline{\psi}\gamma^{\mu}\gamma^{5}\phi$	4	1
TENSOR	$\overline{\psi}(\gamma^{\mu}\gamma^{\nu}-\gamma^{\nu}$	$\gamma^{\mu})\phi$ 6	2

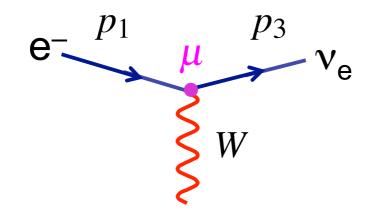
★ Note that in total the sixteen components correspond to the 16 elements of a general 4x4 matrix: "decomposition into Lorentz invariant combinations"

- ★ In QED the factor $g_{\mu\nu}$ arose from the sum over polarization states of the virtual photon (2 transverse + 1 longitudinal, 1 scalar) = (2J+1) + 1
- ★ Associate SCALAR and PSEUDOSCALAR interactions with the exchange of a SPIN-0 boson, etc. – no spin degrees of freedom



V-A in Weak interactions

- ★The most general form for the interaction between a fermion and a boson is a linear combination of bilinear covariants
- ★ For an interaction corresponding to the exchange of a spin-1 particle the most general form is a linear combination of VECTOR and AXIAL-VECTOR
- ★The form for WEAK interaction is <u>determined from experiment</u> to be VECTOR – AXIAL-VECTOR (V – A)



$$j^{\mu} \propto \overline{u}_{\nu_e} (\gamma^{\mu} - \gamma^{\mu} \gamma^5) u_e$$

V – A

- **★** Can this account for parity violation?
- **★** First consider parity transformation of a pure AXIAL-VECTOR current

 $j_{A} = \overline{\psi} \gamma^{\mu} \gamma^{5} \phi \qquad \text{with} \qquad \gamma^{5} = i \gamma^{0} \gamma^{1} \gamma^{2} \gamma^{3}; \qquad \gamma^{5} \gamma^{0} = -\gamma^{0} \gamma^{5}$ $j_{A} = \overline{\psi} \gamma^{\mu} \gamma^{5} \phi \xrightarrow{\hat{P}} \overline{\psi} \gamma^{0} \gamma^{\mu} \gamma^{5} \gamma^{0} \phi = -\overline{\psi} \gamma^{0} \gamma^{\mu} \gamma^{0} \gamma^{5} \phi$ $j_{A}^{0} = \xrightarrow{\hat{P}} -\overline{\psi} \gamma^{0} \gamma^{0} \gamma^{0} \gamma^{5} \phi = -\overline{\psi} \gamma^{0} \gamma^{5} \phi = -j_{A}^{0}$ $j_{A}^{k} = \xrightarrow{\hat{P}} -\overline{\psi} \gamma^{0} \gamma^{k} \gamma^{0} \gamma^{5} \phi = +\overline{\psi} \gamma^{k} \gamma^{5} \phi = +j_{A}^{k} \qquad k = 1, 2, 3 \qquad \text{or} \qquad j_{A}^{\mu} \xrightarrow{\hat{P}} -j_{A\mu}$



V-A in Weak interactions

• The space-like components remain unchanged and the time-like components change sign (the opposite to the parity properties of a vector-current)

$$j_A^0 \xrightarrow{\hat{P}} -j_A^0; \quad j_A^k \xrightarrow{\hat{P}} +j_A^k; \qquad j_V^0 \xrightarrow{\hat{P}} +j_V^0; \quad j_V^k \xrightarrow{\hat{P}} -j_V^k$$

Now consider the matrix elements

$$M \propto g_{\mu\nu} j_1^{\mu} j_2^{\nu} = j_1^0 j_2^0 - \sum_{k=1,3} j_1^k j_2^k$$

For the combination of a two axial-vector currents

$$j_{A1}.j_{A2} \xrightarrow{\hat{P}} (-j_1^0)(-j_2^0) - \sum_{k=1,3} (j_1^k)(j_2^k) = j_{A1}.j_{A2}$$

- Consequently parity is conserved for both a pure vector and pure axial-vector interactions
- However the combination of a vector current and an axial vector current

$$j_{V1}.j_{A2} \xrightarrow{P} (j_1^0)(-j_2^0) - \sum_{k=1,3} (-j_1^k)(j_2^k) = -j_{V1}.j_{A2}$$

changes sign under parity – can give parity violation !



V-A in Weak interactions

★ Now consider a general linear combination of VECTOR and AXIAL-VECTOR (note this is relevant for the Z-boson vertex)

$$\begin{array}{c}
\psi_{1} & \mu & \phi_{1} \\
\psi_{2} & \psi_{2} & \psi_{2} \\
\psi_{2} & \psi_{2} & \phi_{2} \\
\end{array} \begin{pmatrix}
j_{1} = \overline{\phi}_{1} (g_{V} \gamma^{\mu} + g_{A} \gamma^{\mu} \gamma^{5}) \psi_{1} = g_{V} j_{1}^{V} + g_{A} j_{1}^{A} \\
\frac{g_{\mu\nu}}{q^{2} - m^{2}} \\
j_{2} = \overline{\phi}_{2} (g_{V} \gamma^{\mu} + g_{A} \gamma^{\mu} \gamma^{5}) \psi_{2} = g_{V} j_{2}^{V} + g_{A} j_{2}^{A} \\
M_{fi} \propto j_{1} \cdot j_{2} = g_{V}^{2} j_{1}^{V} \cdot j_{2}^{V} + g_{A}^{2} j_{1}^{A} \cdot j_{2}^{A} + g_{V} g_{A} (j_{1}^{V} \cdot j_{2}^{A} + j_{1}^{A} \cdot j_{2}^{V})
\end{array}$$

•Consider the parity transformation of this scalar product

$$j_1.j_2 \xrightarrow{P} g_V^2 j_1^V.j_2^V + g_A^2 j_1^A.j_2^A - g_V g_A(j_1^V.j_2^A + j_1^A.j_2^V)$$

- If either g_A or g_V is zero, Parity is conserved, i.e. parity conserved in a pure VECTOR or pure AXIAL-VECTOR interaction
- Relative strength of parity violating part

$$\frac{g_V g_A}{g_V^2 + g_A^2}$$

Maximal Parity Violation for V-A (or V+A)

 \propto



Chiral Structure

★ Recall (QED lectures in KTI) introduced CHIRAL projections operators

$$P_R = \frac{1}{2}(1+\gamma^5);$$
 $P_L = \frac{1}{2}(1-\gamma^5)$

project out chiral right- and left- handed states

- **★** In the ultra-relativistic limit, chiral states correspond to helicity states
- **★** Any spinor can be expressed as:

$$\boldsymbol{\psi} = \frac{1}{2}(1+\gamma^5)\boldsymbol{\psi} + \frac{1}{2}(1-\gamma^5)\boldsymbol{\psi} = P_R\boldsymbol{\psi} + P_L\boldsymbol{\psi} = \boldsymbol{\psi}_R + \boldsymbol{\psi}_L$$

•The QED vertex $\overline{\Psi}\gamma^{\mu}\phi$ in terms of chiral states:

$$\overline{\psi}\gamma^{\mu}\phi = \overline{\psi}_{R}\gamma^{\mu}\phi_{R} + \overline{\psi}_{R}\gamma^{\mu}\phi_{L} + \overline{\psi}_{L}\gamma^{\mu}\phi_{R} + \overline{\psi}_{L}\gamma^{\mu}\phi_{L}$$

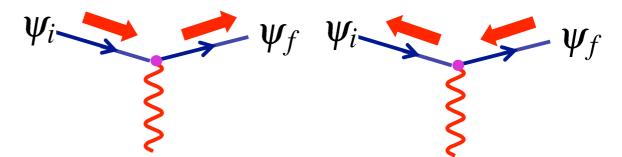
conserves chirality, e.g.

$$\overline{\psi}_{R} \gamma^{\mu} \phi_{L} = \frac{1}{2} \psi^{\dagger} (1 + \gamma^{5}) \gamma^{0} \gamma^{\mu} \frac{1}{2} (1 - \gamma^{5}) \phi$$

$$= \frac{1}{4} \psi^{\dagger} \gamma^{0} (1 - \gamma^{5}) \gamma^{\mu} (1 - \gamma^{5}) \phi$$

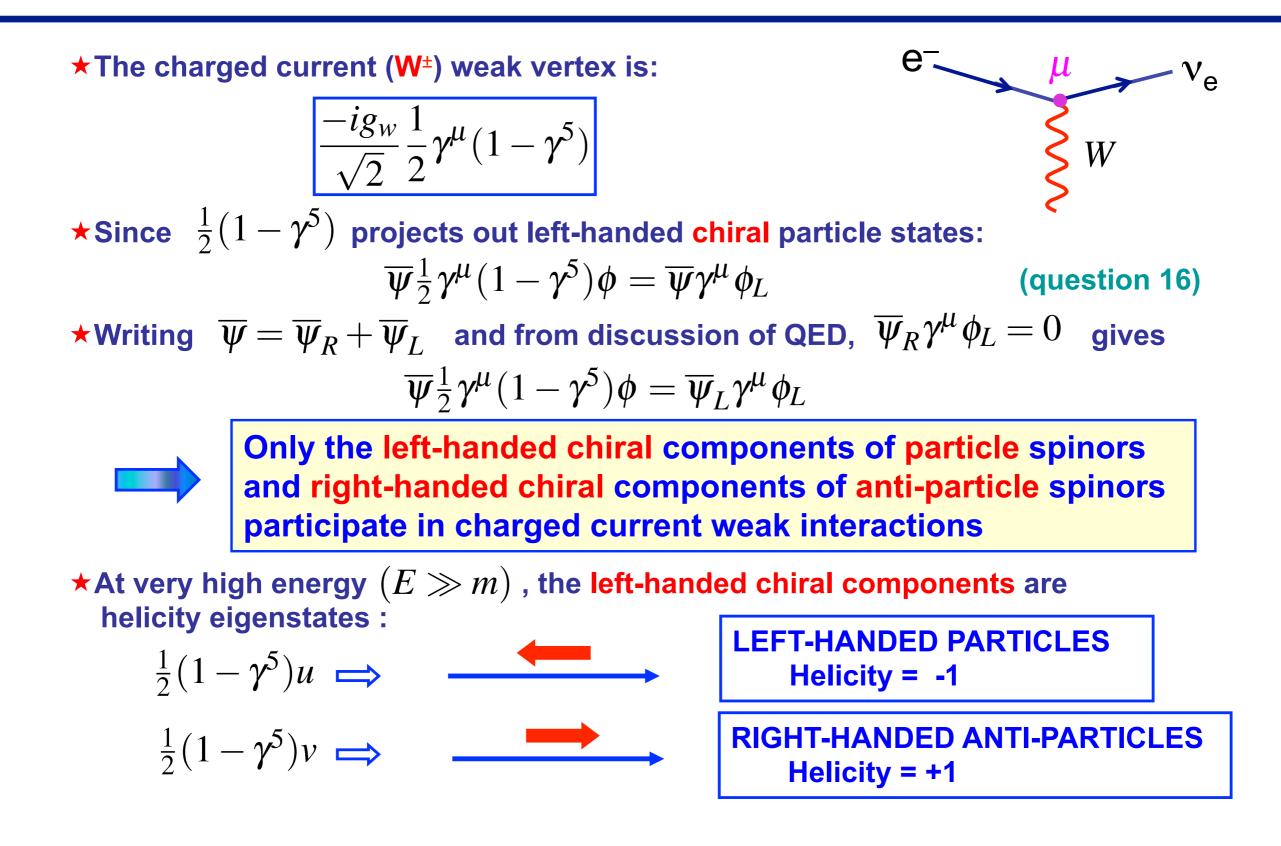
$$= \frac{1}{4} \overline{\psi} \gamma^{\mu} (1 + \gamma^{5}) (1 - \gamma^{5}) \phi = 0$$

In the ultra-relativistic limit only two helicity combinations are non-zero





Helicity Structure in Weak Interaction

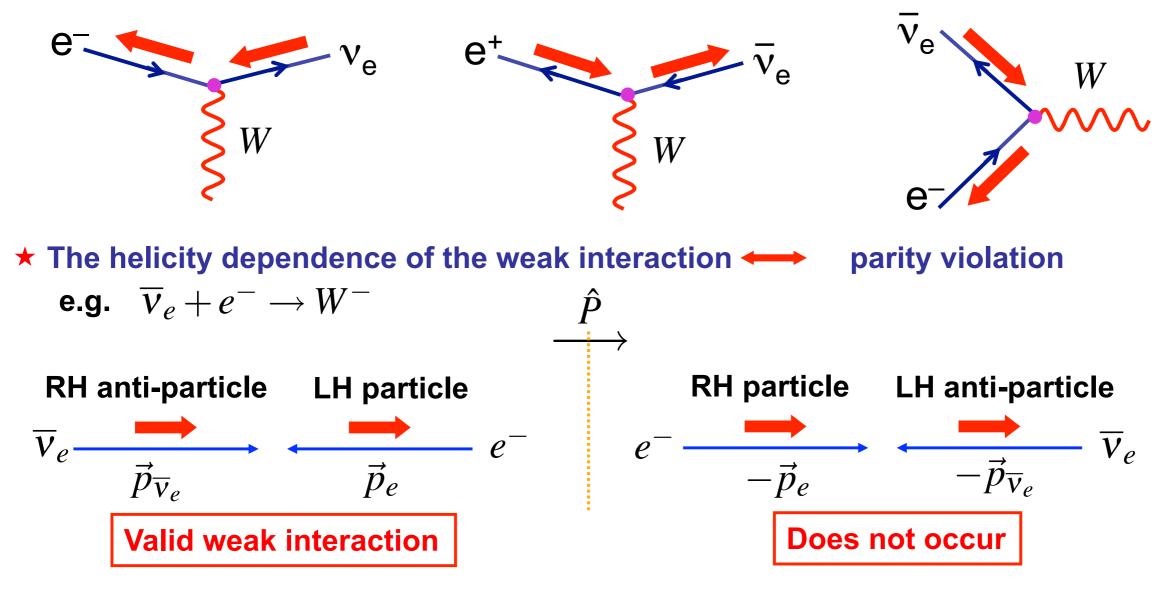




Helicity Structure in Weak Interaction



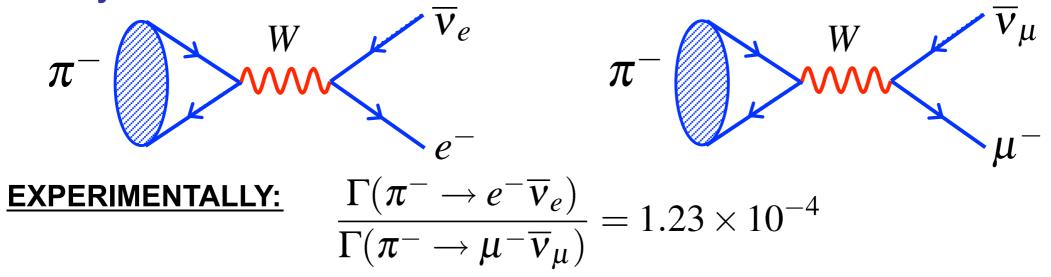
e.g. In the relativistic limit, the only possible electron – neutrino interactions are:





Helicity in pion decay

The decays of charged pions provide a good demonstration of the role of helicity in the weak interaction



•Might expect the decay to electrons to dominate – due to increased phase space.... The opposite happens, the electron decay is helicity suppressed

★Consider decay in pion rest frame.

- Pion is spin zero: so the spins of the $\overline{\nu}$ and μ are opposite
- Weak interaction only couples to RH chiral anti-particle states. Since neutrinos are (almost) massless, must be in RH Helicity state
- Therefore, to conserve angular mom. muon is emitted in a RH HELICITY state



But only left-handed CHIRAL particle states participate in weak interaction



Helicity in pion decay

*****The general right-handed helicity solution to the Dirac equation is

$$u_{\uparrow} = N \begin{pmatrix} c \\ e^{i\phi}s \\ \frac{|\vec{p}|}{E+m}c \\ \frac{|\vec{p}|}{E+m}e^{i\phi}s \end{pmatrix}$$

with
$$c = \cos \frac{\theta}{2}$$
 and $s = \sin \frac{\theta}{2}$

 project out the left-handed <u>chiral</u> part of the wave-function using

$$P_L = \frac{1}{2}(1 - \gamma^5) = \frac{1}{2} \begin{pmatrix} 1 & 0 & -1 & 0 \\ 0 & 1 & 0 & -1 \\ -1 & 0 & 1 & 0 \\ 0 & -1 & 0 & 1 \end{pmatrix}$$

giving
$$P_L u_{\uparrow} = \frac{1}{2} N \left(1 - \frac{|\vec{p}|}{E+m} \right) \begin{pmatrix} c \\ e^{i\phi}s \\ -c \\ -e^{i\phi}s \end{pmatrix} = \frac{1}{2} N \left(1 - \frac{|\vec{p}|}{E+m} \right) u_L$$

In the limit $m \ll E$ this tends to zero

1

similarly

$$P_{R}u_{\uparrow} = \frac{1}{2}N\left(1 + \frac{|\vec{p}|}{E+m}\right)\begin{pmatrix}c\\e^{i\phi}s\\c\\e^{i\phi}s\end{pmatrix} = \frac{1}{2}N\left(1 + \frac{|\vec{p}|}{E+m}\right)u_{R}$$

In the limit $m \ll E$, $P_{R}u_{\uparrow} \rightarrow u_{R}$

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Helicity in pion decay

★Hence
$$u_{\uparrow} = P_R u_{\uparrow} + P_L u_{\uparrow} = \frac{1}{2} \left(1 + \frac{|\vec{p}|}{E+m} \right) u_R + \frac{1}{2} \left(1 - \frac{|\vec{p}|}{E+m} \right) u_L$$
RH Helicity
RH Chiral

•In the limit $E \gg m$, as expected, the RH chiral and helicity states are identical

•Although only LH chiral particles participate in the weak interaction the contribution from RH Helicity states is not necessarily zero !

$$\overline{v}_{\mu}$$
 ← → μ^{-}
m_ν ≈ 0: RH Helicity ≡ RH Chiral $m_{\mu} ≠ 0$: RH Helicity has LH Chiral Component

★ Expect matrix element to be proportional to LH chiral component of RH Helicity electron/muon spinor

$$M_{fi} \propto \frac{1}{2} \left(1 - \frac{|\vec{p}|}{E+m} \right) = \frac{m_{\mu}}{m_{\pi} + m_{\mu}} \qquad \text{from the kinematics}$$
 of pion decay at rest

★ Hence because the electron mass is much smaller than the pion mass the decay $\pi^- \rightarrow e^- \overline{v}_e$ is heavily suppressed.



Evidence of V-A

★The V-A nature of the charged current weak interaction vertex fits with experiment

EXAMPLE charged pion decay(question 17)•Experimentally measure:
$$\frac{\Gamma(\pi^- \to e^- \overline{\nu}_e)}{\Gamma(\pi^- \to \mu^- \overline{\nu}_\mu)} = (1.230 \pm 0.004) \times 10^{-4}$$
•Theoretical predictions (depend on Lorentz Structure of the interaction)V-A $(\overline{\psi}\gamma^{\mu}(1-\gamma^5)\phi)$ or V+A $(\overline{\psi}\gamma^{\mu}(1+\gamma^5)\phi)$ \Rightarrow $\frac{\Gamma(\pi^- \to e^- \overline{\nu}_e)}{\Gamma(\pi^- \to \mu^- \overline{\nu}_\mu)} \approx 1.3 \times 10^{-4}$ Scalar ($\overline{\psi}\phi$) or Pseudo-Scalar $(\overline{\psi}\gamma^5\phi)$ \Rightarrow $\frac{\Gamma(\pi^- \to e^- \overline{\nu}_e)}{\Gamma(\pi^- \to \mu^- \overline{\nu}_\mu)} = 5.5$

EXAMPLE muon decay

Measure electron energy and angular distributions relative to muon spin direction. Results expressed in terms of general S+P+V+A+T form in "Michel Parameters"

e.g. TWIST expt: $6x10^9 \mu$ decays Phys. Rev. Lett. 95 (2005) 101805

 $\rho = 0.75080 \pm 0.00105$

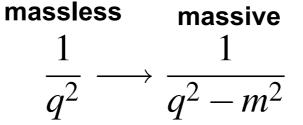
V-A Prediction: $\rho = 0.75$

 θ_e



W Propagator

- ★ The charged-current Weak interaction is different from QED and QCD in that it is mediated by massive W-bosons (80.3 GeV)
- **★**This results in a more complicated form for the propagator:
 - in handout 4 showed that for the exchange of a massive particle:



In addition the sum over W boson polarization states modifies the numerator

W-boson propagator

spin 1 W[±]
$$\frac{-i\left[g_{\mu\nu} - q_{\mu}q_{\nu}/m_W^2\right]}{q^2 - m_W^2} \qquad \overset{\mu}{\longrightarrow} \overset{q}{\longrightarrow} \overset{\nu}{\longrightarrow}$$

★ However in the limit where q^2 is small compared with $m_W = 80.3 \,\text{GeV}$ the interaction takes a simpler form.

W-boson propagator (
$$q^2 \ll m_W^2$$
)
 $\frac{ig_{\mu\nu}}{m_W^2}$ μ_V

•The interaction appears point-like (i.e no q² dependence)



★In 1934, before the discovery of parity violation, Fermi proposed, in analogy with QED, that the invariant matrix element for β -decay was of the form:

$$M_{fi} = G_{\rm F} g_{\mu\nu} [\overline{\psi} \gamma^{\mu} \psi] [\overline{\psi} \gamma^{\nu} \psi]$$

10⁻⁵ GeV⁻²

where $G_F = 1.166 \times 10^{-5} \,\text{GeV}^{-2}$ •Note the absence of a propagator : i.e. this represents an interaction at a point

★After the discovery of parity violation in 1957 this was modified to

$$M_{fi} = \frac{G_{\rm F}}{\sqrt{2}} g_{\mu\nu} [\overline{\psi} \gamma^{\mu} (1 - \gamma^5) \psi] [\overline{\psi} \gamma^{\nu} (1 - \gamma^5) \psi]$$

(the factor of $\sqrt{2}$ was included so the numerical value of G_F did not need to be changed) **★** Compare to the prediction for W-boson exchange

$$M_{fi} = \left[\frac{g_W}{\sqrt{2}}\overline{\psi}\frac{1}{2}\gamma^{\mu}(1-\gamma^5)\psi\right]\frac{g_{\mu\nu} - q_{\mu}q_{\nu}/m_W^2}{q^2 - m_W^2}\left[\frac{g_W}{\sqrt{2}}\overline{\psi}\frac{1}{2}\gamma^{\nu}(1-\gamma^5)\psi\right]$$

which for $q^2 \ll m_W^2$ becomes:

$$M_{fi} = \frac{g_W^2}{8m_W^2} g_{\mu\nu} [\overline{\psi}\gamma^{\mu}(1-\gamma^5)\psi] [\overline{\psi}\gamma^{\nu}(1-\gamma^5)\psi]$$

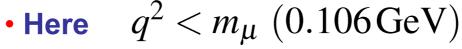
 $G_{\rm T}$

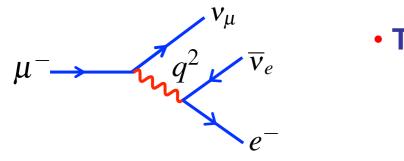
Still usually use $G_{
m F}\,$ to express strength of weak interaction as the is the quantity that is precisely determined in muon decay



Strength of Weak Interaction

★ Strength of weak interaction most precisely measured in muon decay





 To a very good approximation the W-boson propagator can be written

$$e^{-} \qquad \frac{-i\left[g_{\mu\nu} - q_{\mu}q_{\nu}/m_{W}^{2}\right]}{q^{2} - m_{W}^{2}} \approx \frac{ig_{\mu\nu}}{m_{W}^{2}}$$
• In muon decay measure g_{W}^{2}/m_{W}^{2}

• Muon decay \rightarrow $G_{\rm F} = 1.16639(1) \times 10^{-5} \, {\rm GeV}^{-2}$

$$\frac{G_{\rm F}}{\sqrt{2}} = \frac{g_W^2}{8m_W^2}$$

★ To obtain the intrinsic strength of weak interaction need to know mass of W-boson: $m_W = 80.403 \pm 0.029 \,\text{GeV}$ (see handout 14)

$$\Rightarrow \qquad \alpha_W = \frac{g_W^2}{4\pi} = \frac{8m_W^2 G_F}{4\sqrt{2}\pi} = \frac{1}{30}$$

 \star

The intrinsic strength of the weak interaction is similar to, but greater than, the EM interaction ! It is the massive W-boson in the propagator which makes it appear weak. For $q^2 \gg m_W^2$ weak interactions are more likely than EM.