

# Exercises

	Hand out	Hand in	Discussion
Exercise 1	Wed 19.2.	Wed 26.2.	Fri 28.2.
Exercise 2	Wed 26.2.	Fri 6.3.	Fri 13.3.
Exercise 3	Fri 6.3.	Fri 20.3.	Fri 27.3.
Exercise 4	Fri 20.3.	Fri 3.4.	Fri 24.4.
Exercise 5	Fri 3.4.	Fri 1.5.	Fri 8.5.
Exercise 6	Fri 1.5.	Fri 15.5.	Fri 22.5.

## Praktikum

- Discussion on Fri 29.5. 13:00-15:45

# Addendum: Neutrino oscillation length

This lecture:

$$L_{osc} = \frac{4\pi E}{\Delta m^2}$$

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2(2\theta) \sin^2\left(\pi \frac{L}{L_{osc}}\right)$$

Martin & Shaw, „Particle Physics“, Chapter 2:

$$L_{osc} = \frac{4E}{\Delta m^2}$$

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2(2\theta) \sin^2\left(\frac{L}{L_{osc}}\right)$$



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Physik-Institut



PHY213 Kern- und Teilchenphysik II  
(FS 2020)

# Intensity Frontier: Neutrino physics

Lea Caminada

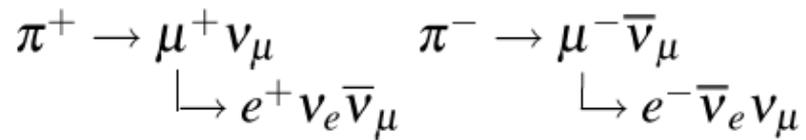
[lea.caminada@physik.uzh.ch](mailto:lea.caminada@physik.uzh.ch)

# Overview

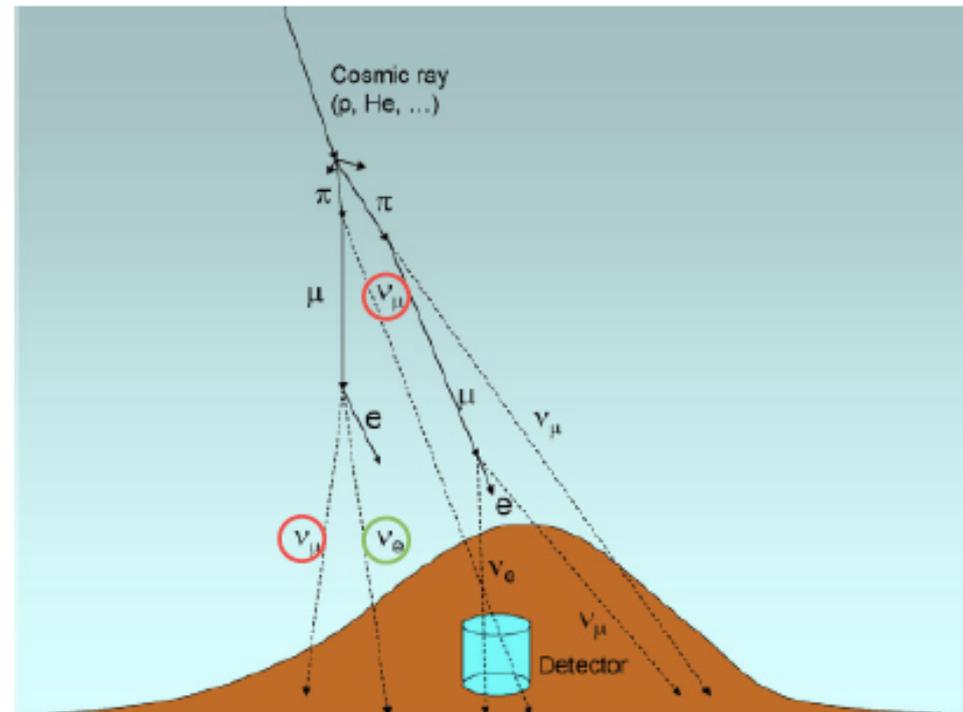
- Atmospheric neutrinos
- Identification with flavor
- Mass hierarchy
- Current status of measurements
- Experimental techniques
  - Sources
  - Reactor experiments
  - Accelerator experiments

# Atmospheric neutrinos

- High-energy cosmic rays interact in the upper part of the Earth's atmosphere
- The cosmic rays ( $\sim 86\%$  protons) mostly interact hadronically giving showers of mainly pions
- Subsequent decay of pions and muons:

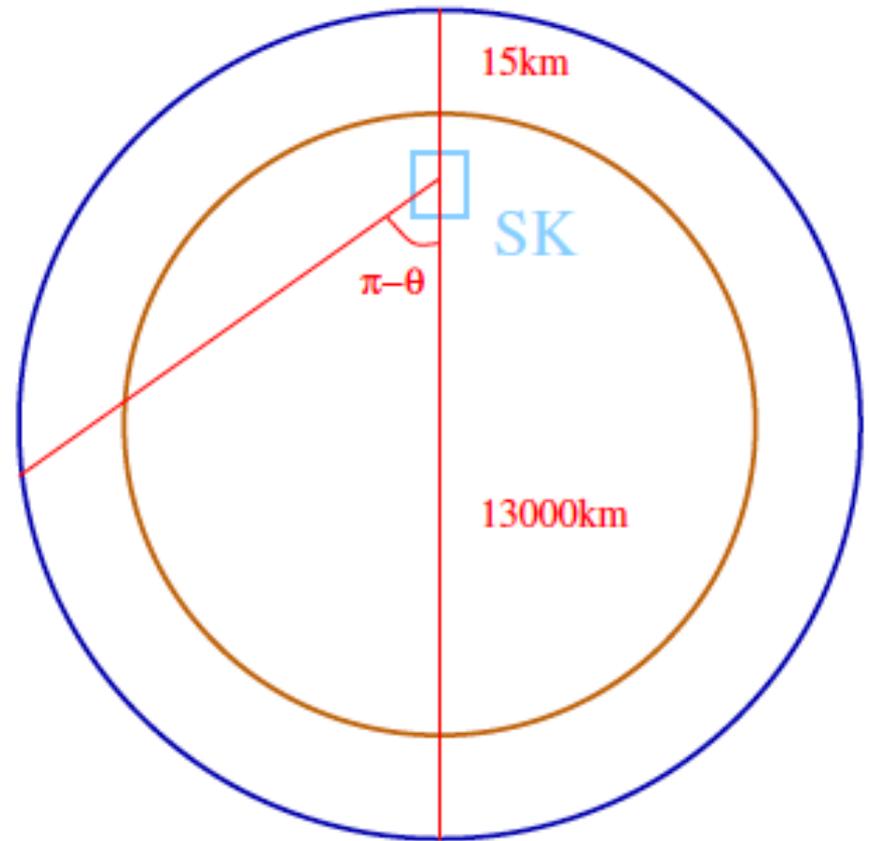


- Producing neutrinos with  $E_\nu \sim 100 \text{ MeV} - 1 \text{ TeV}$
- Expected ratio is  $\nu_\mu : \nu_e \sim 2 : 1$
- However, observed lower ratio ( $\nu_\mu$  deficit)



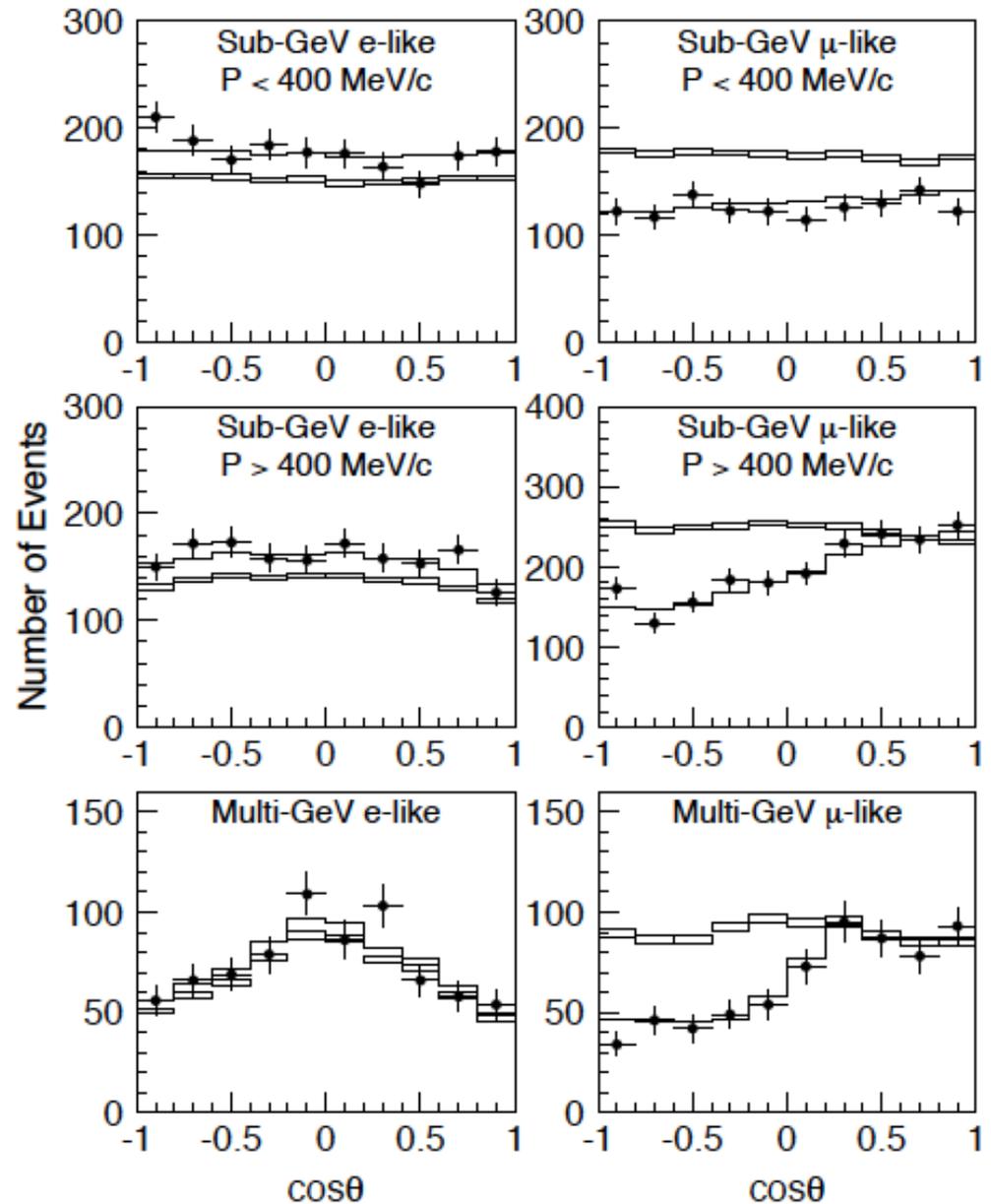
# Atmospheric neutrino oscillations

- Atmospheric neutrinos are an ideal source to look for neutrino oscillations  $\rightarrow E_\nu/L$  spans several orders of magnitude
- $E_\nu \sim 100 \text{ MeV} - 1 \text{ TeV}$
- $L \sim 10 - 10^4 \text{ km}$



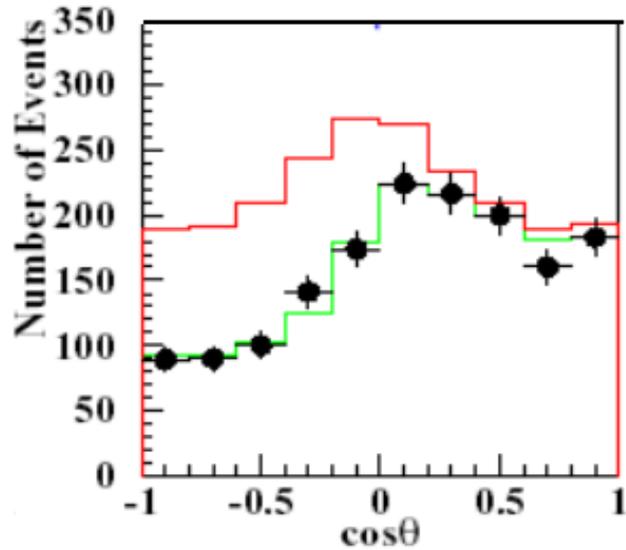
# Atmospheric neutrino oscillations

- SuperKamiokande experiment clarified origin of atmospheric  $\nu_\mu$  deficit
  - Experiment can separate  $\nu_\mu$  and  $\nu_e$  and measure direction of outgoing lepton
  - Measured flux for different energies
- Results
  - $\nu_e$  in rough agreement with predictions
  - Strong evidence for disappearance of  $\nu_\mu$  coming from below
  - Consistent with  $\nu_\mu \rightarrow \nu_\tau$  oscillations ( $\nu_\tau$  below detection threshold)



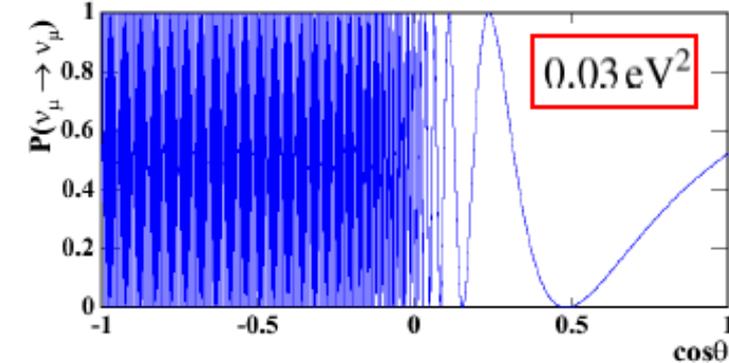
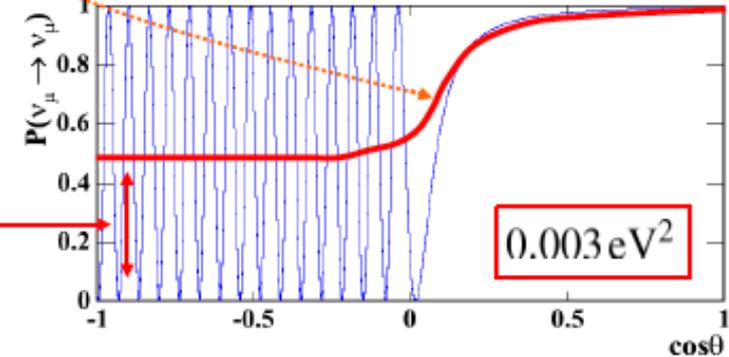
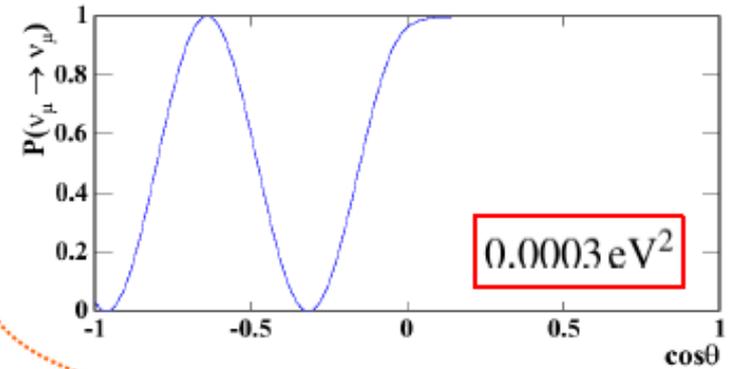
# Atmospheric neutrino oscillations

- Measure muon direction and energy not neutrino direction/energy
- Don't have  $E/\theta$  resolution to see oscillations
- Oscillations "smeared" out in data
- Compare data to predictions for  $|\Delta m^2|$



$|\Delta m^2|$

$$1 - \frac{1}{2} \sin^2 2\theta$$



★ Data consistent with:

$$|\Delta m_{\text{atmos}}^2| \approx 0.0025 \text{ eV}^2$$

$$\sin^2 2\theta_{\text{atmos}} \approx 1$$

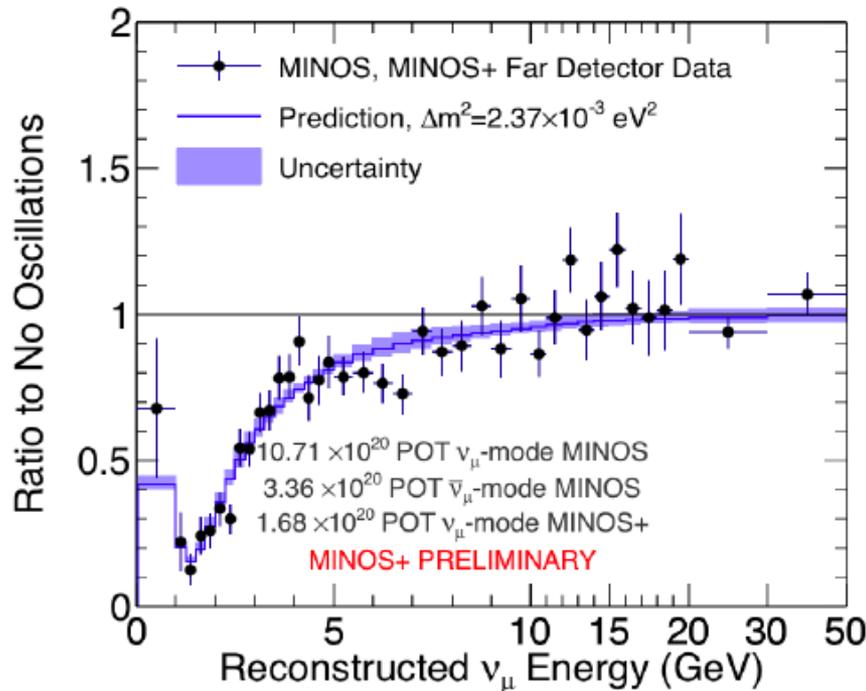
# Confirmation by accelerator neutrinos

- Atmospheric neutrino oscillations confirmed by long-baseline accelerator neutrino experiments

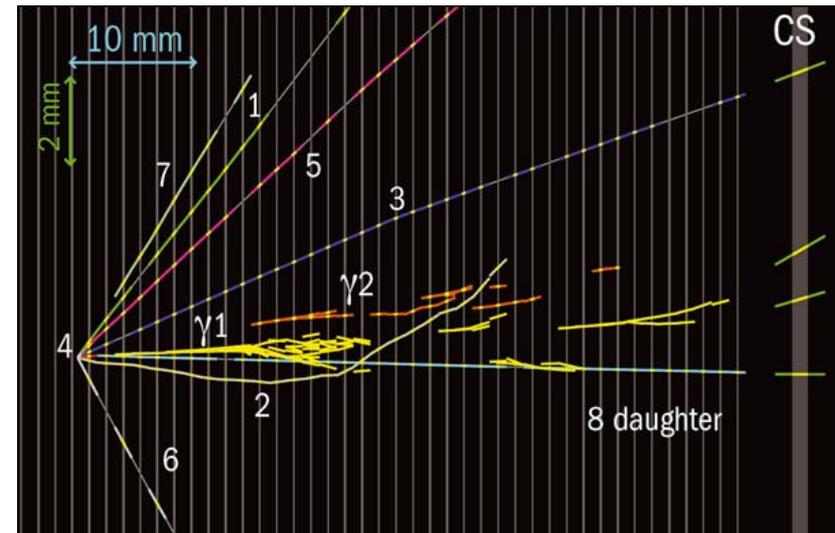
$$\Delta m_{\text{atm}}^2 = 2.5 \times 10^{-3} \text{eV}^2$$

$$|\Delta m_{\text{atm}}^2| \sim \frac{\mathcal{O}(\text{GeV})}{\mathcal{O}(1000\text{km})}$$

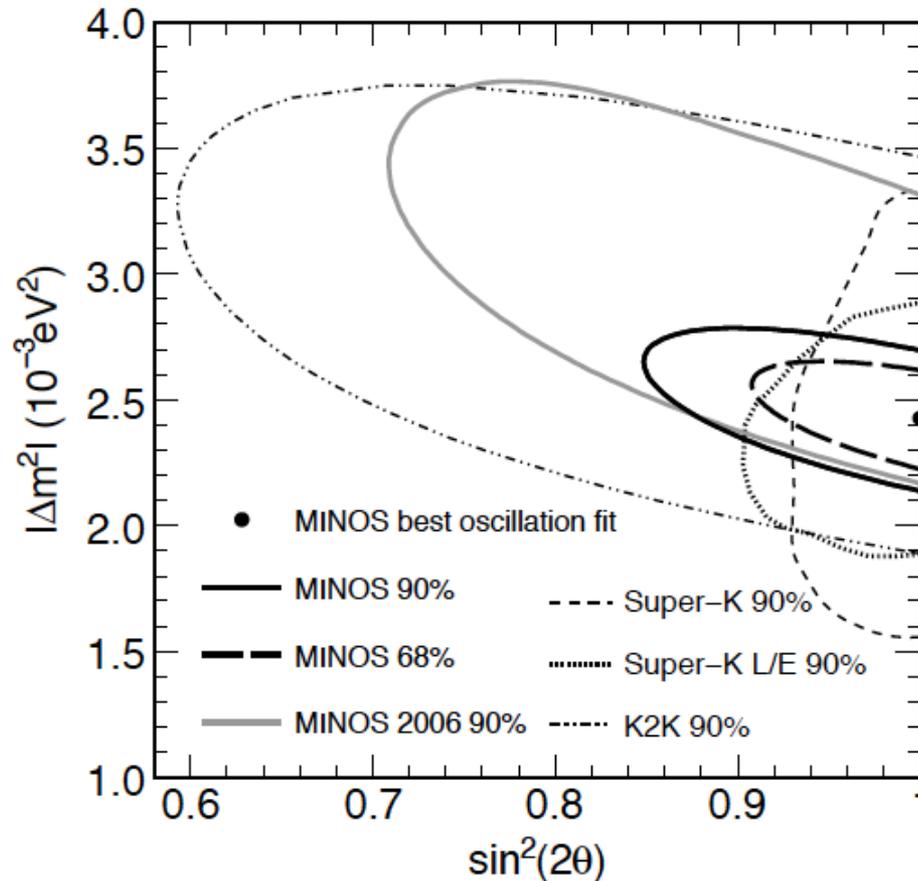
- $\nu_{\mu}$  disappearance first measured by MINOS (Fermilab, L=730km) and K2K (JPARC, L=235km)
- $\nu_{\tau}$  appearance measured by OPERA (CERN/LNGS, L=730km)



OPERA 2010



# Measurement of $\Delta m_{23}$ and $\theta_{23}$



$$\theta_{23} = (38 - 50)^\circ (3\sigma)$$

→ Which octant? Is  $q_{23}$  smaller or larger than  $45^\circ$ ?

$$|\Delta m_{32}^2| \approx (2.5 \pm 0.4) \times 10^{-3} \text{eV}^2$$

# Identification with flavors

- Have two distinct  $\Delta m^2$  related to solar and atmospheric oscillation frequencies

$$\underbrace{|\Delta m_{\text{solar}}^2|}_{\sim 8 \cdot 10^{-5} \text{ eV}^2} \ll \underbrace{|\Delta m_{\text{atmos}}^2|}_{\sim 2.5 \cdot 10^{-3} \text{ eV}^2}$$

- Conventional assignment to mass eigenstates

$$\Delta m_{23}^2 = m_3^2 - m_2^2 \equiv \Delta m_{\text{atm}}^2$$

$$\Delta m_{12}^2 = m_2^2 - m_1^2 \equiv \Delta m_{\text{sol}}^2$$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U_{23}(\theta_{23})U_{13}(\theta_{13}, \delta)U_{12}(\theta_{12}) \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

# Decoupling as 2 flavor mixing

- Three flavor mixing phenomena decouple to 2 flavor mixing phenomena since  $\Delta m_{\text{atmos}} \gg \Delta m_{\text{solar}}$  and  $\theta_{13}$  small
- For atmospheric neutrino oscillations:

$$E_\nu/L \sim |\Delta m_{\text{atmos}}^2| \quad \rightarrow \quad \sin\left(\frac{\Delta m_{\text{solar}}^2 L}{4E_\nu}\right) \sim \frac{\Delta m_{\text{solar}}^2 L}{4E_\nu} \sim 0$$

$$\theta_{13} \rightarrow 0$$

$$P(\nu_e \rightarrow \nu_\mu) = s_{23}^2 \sin^2 2\theta_{13} \sin^2\left(\frac{\Delta m_{23}^2}{4E} L\right) = 0$$

$$P(\nu_e \rightarrow \nu_\tau) = c_{23}^2 \sin^2 2\theta_{13} \sin^2\left(\frac{\Delta m_{23}^2}{4E} L\right) = 0$$

$$P(\nu_\mu \rightarrow \nu_\tau) = c_{13}^4 \sin^2 2\theta_{23} \sin^2\left(\frac{\Delta m_{23}^2}{4E} L\right) = \sin^2 2\theta_{23} \sin^2\left(\frac{\Delta m_{23}^2}{4E} L\right)$$

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \sin^2 2\theta_{13} \sin^2\left(\frac{\Delta m_{23}^2}{4E} L\right) = 1$$

- Described by 2x2 mixing with mixing parameters:

$$(\Delta m_{23}^2, \theta_{23}) = (\Delta m_{\text{atm}}^2, \theta_{\text{atm}})$$

# Decoupling as 2 flavor mixing

- Three flavor mixing phenomena decouple to 2 flavor mixing phenomena since  $\Delta m_{\text{atmos}} \gg \Delta m_{\text{solar}}$  and  $\theta_{13}$  small
- For solar neutrino oscillations:

$E_\nu/L \sim |\Delta m_{\text{solar}}^2| \rightarrow$  Atmospheric oscillations too rapid and get averaged out

$$P(\nu_e \rightarrow \nu_e) = P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \simeq c_{13}^4 \left( 1 - \sin^2 2\theta_{12} \sin^2 \left( \frac{\Delta m_{12}^2 L}{4E_\nu} \right) \right) + s_{13}^4$$

*(Note: Red arrows in the original image point to  $c_{13}^4$  and  $s_{13}^4$  with labels 1 and 0 respectively, and  $\theta_{13} \rightarrow 0$  is written above the equation.)*

- Described by 2x2 mixing with mixing parameters:

$$(\Delta m_{12}^2, \theta_{12}) = (\Delta m_{\text{solar}}^2, \theta_{\text{solar}})$$

- Note: measurement of  $\theta_{13} \sim 9^\circ \rightarrow$  get sizeable corrections

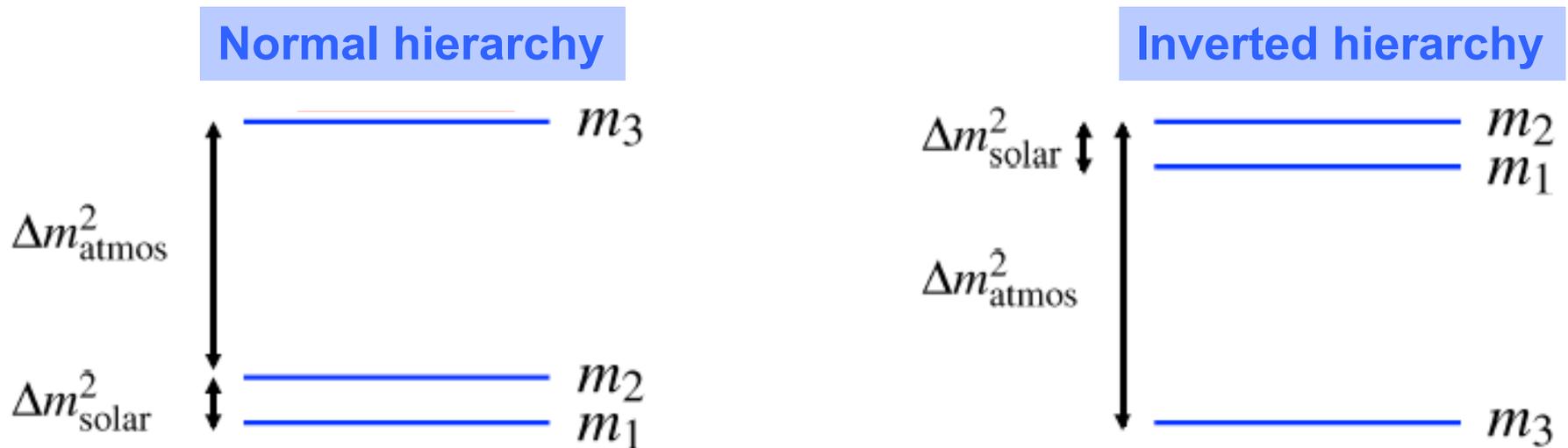
# Mass hierarchy

- Results of neutrino oscillations determine  $|\Delta m_{ji}^2| = |m_j^2 - m_i^2|$
- Two distinct and very different mass scales

$$|\Delta m^2|_{\text{atmos}} \sim 2.5 \times 10^{-3} \text{ eV}^2$$

$$|\Delta m^2|_{\text{solar}} \sim 8 \times 10^{-5} \text{ eV}^2$$

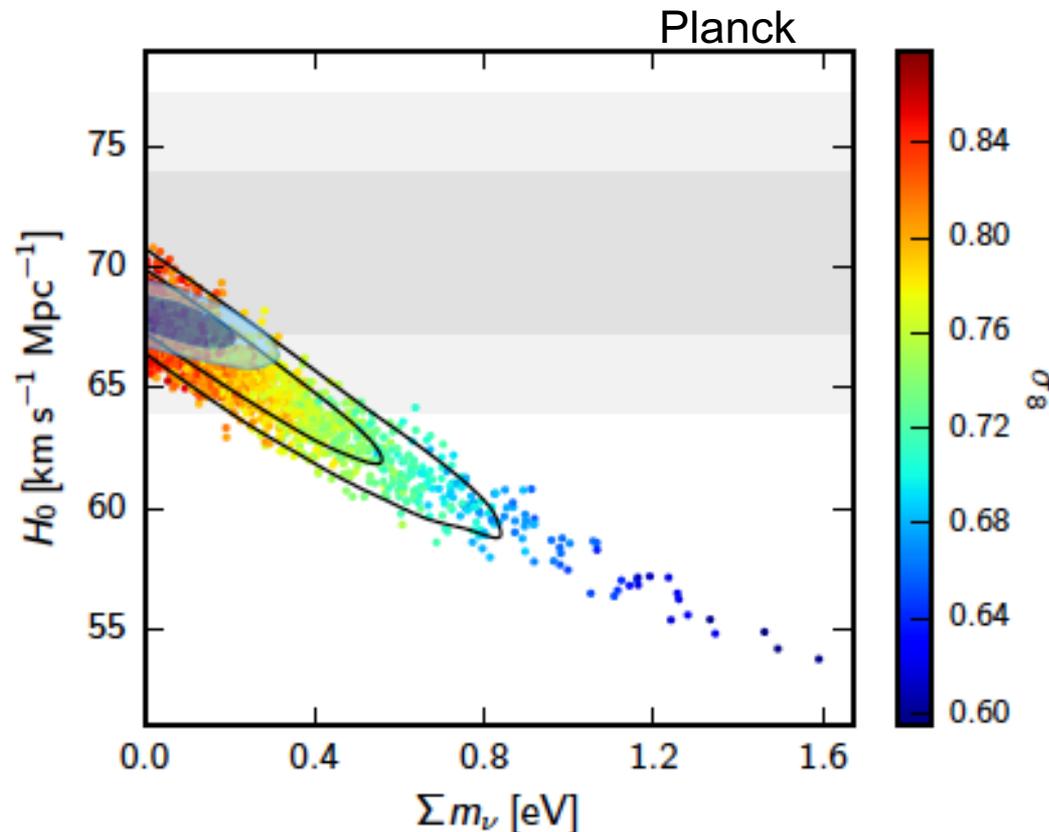
- Two possible assignments of mass hierarchy:



- In both cases:  $\Delta m_{21}^2 \sim 8 \times 10^{-5} \text{ eV}^2$  (solar)
- $|\Delta m_{31}^2| \approx |\Delta m_{32}^2| \sim 2.5 \times 10^{-3} \text{ eV}^2$  (atmospheric)

# Constraints on neutrino masses

- Neutrino oscillations cannot provide information about absolute mass scales
- Best sensitivity to sum of neutrino masses coming from cosmology (CMB temperature power spectrum, galaxy structure formation)



# Measurement of mixing parameters

$$c_{ij} = \cos \theta_{ij}$$

$$s_{ij} = \sin \theta_{ij}$$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{+i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

atmospheric, accelerator

accelerator, reactor

solar, reactor

3 mixing angles, 2 squared mass difference, 1 complex phase ( $\delta_{CP}$ )

3 Flavour states

3 Mass states  
 $m_1 \neq m_2 \neq m_3$

more than 15 years of experimental efforts

Parameters		Experiment	signal
$ \Delta m_{21} ^2 =  m_2^2 - m_1^2 $	$\theta_{12}$	solar and reactor	$P(\nu_e \rightarrow \nu_{\mu,\tau})$
$ \Delta m_{32} ^2 =  m_3^2 - m_2^2 $	$\theta_{23}$	atmospheric and accelerator	$P(\nu_\mu \rightarrow \nu_\mu) \ \& \ P(\nu_\mu \rightarrow \nu_\tau)$
	$\theta_{13}$	reactor and accelerator	$P(\nu_\mu \rightarrow \nu_e) \ \& \ P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$
	$\delta_{CP}$	accelerator	$P(\nu_\mu \rightarrow \nu_e)$

# Knowns and unknowns

$$\theta_{12} = 33.6 \pm 0.8^\circ$$

$$\Delta m_{21}^2 = +(7.5 \pm 0.2) \times 10^{-5} \text{eV}^2$$

## Solar parameters

$$P(\nu_e \rightarrow \nu_{\mu,\tau}) \quad \text{SNO, SK, BOREXINO, GALLEX, SAGE..}$$

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \quad \text{KamLAND}$$

$$\theta_{23} = (38 - 50)^\circ (3\sigma) \rightarrow \text{Octant?}$$

$$|\Delta m_{32}^2| \approx (2.5 \pm 0.4) \times 10^{-3} \text{eV}^2$$

$\rightarrow$  Mass hierarchy?

## Atmospheric parameters

$$P(\nu_\mu \rightarrow \nu_\mu) \quad \text{Kamiokande, SK, IMB, K2K, MINOS, T2K, NOvA}$$

$$P(\nu_\mu \rightarrow \nu_\tau) \quad \text{(Opera)}$$

$$\theta_{13} = 8.4 \pm 0.2^\circ$$

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \quad \text{Daya-Bay, RENO, Double Chooz}$$

$$P(\nu_\mu \rightarrow \nu_e) \quad \text{T2K, NOvA}$$

$$\delta_{CP} = [0, 2\pi] \rightarrow \text{CP violation?}$$

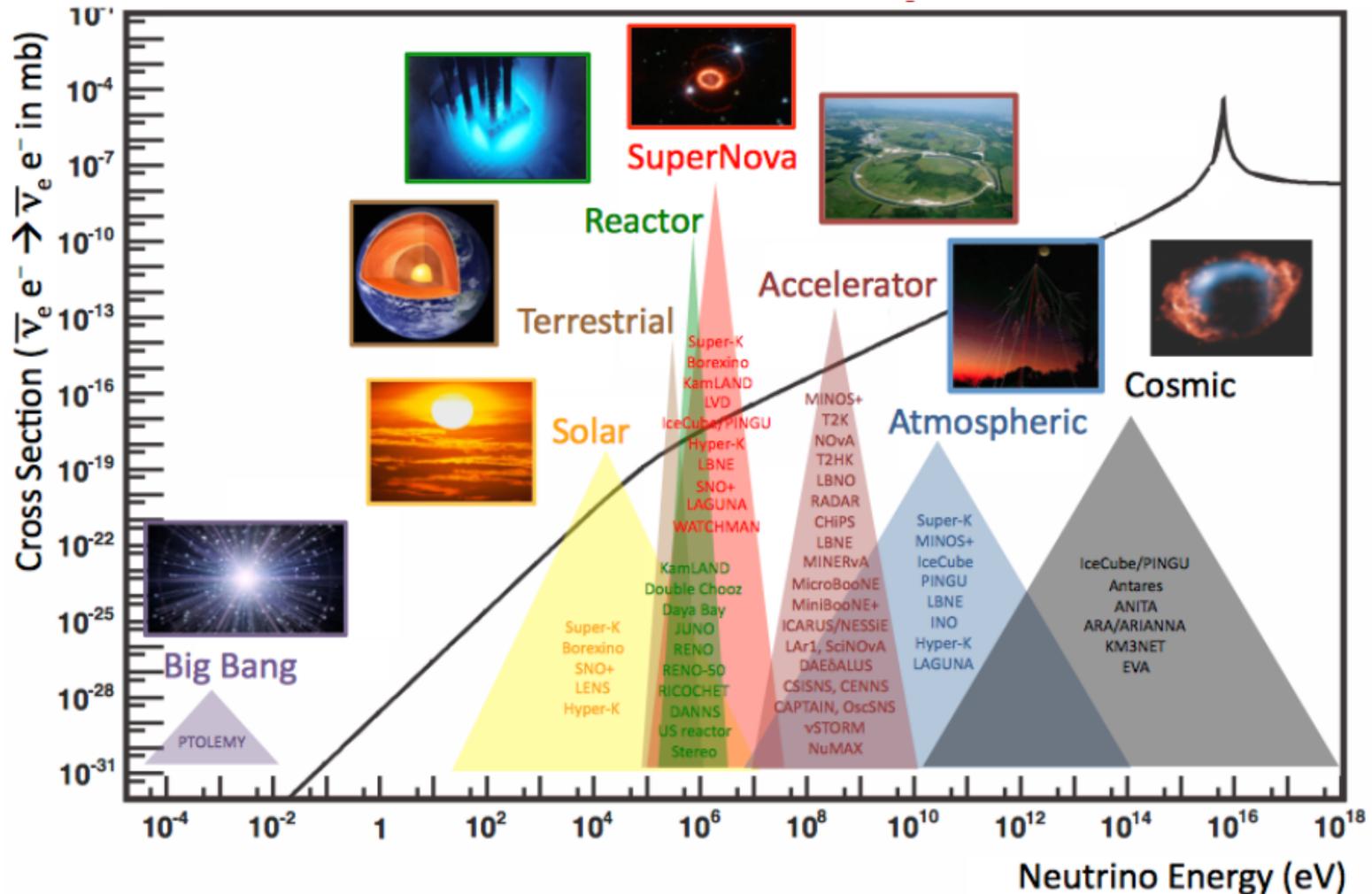
$$\text{T2K, NOvA}$$

$\rightarrow$  New phenomena?

# Neutrino physics experiments

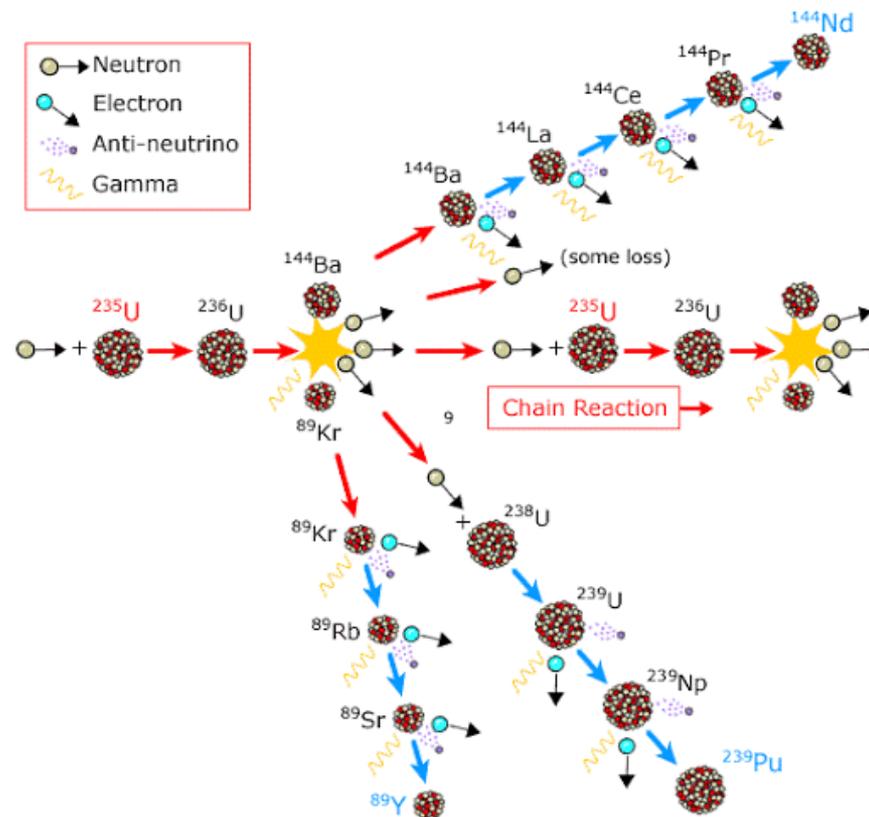
# Sources of neutrinos

- Neutrinos are everywhere:
  - Energy spectrum covers 20 orders of magnitude
  - Second most abundant particles in the universe

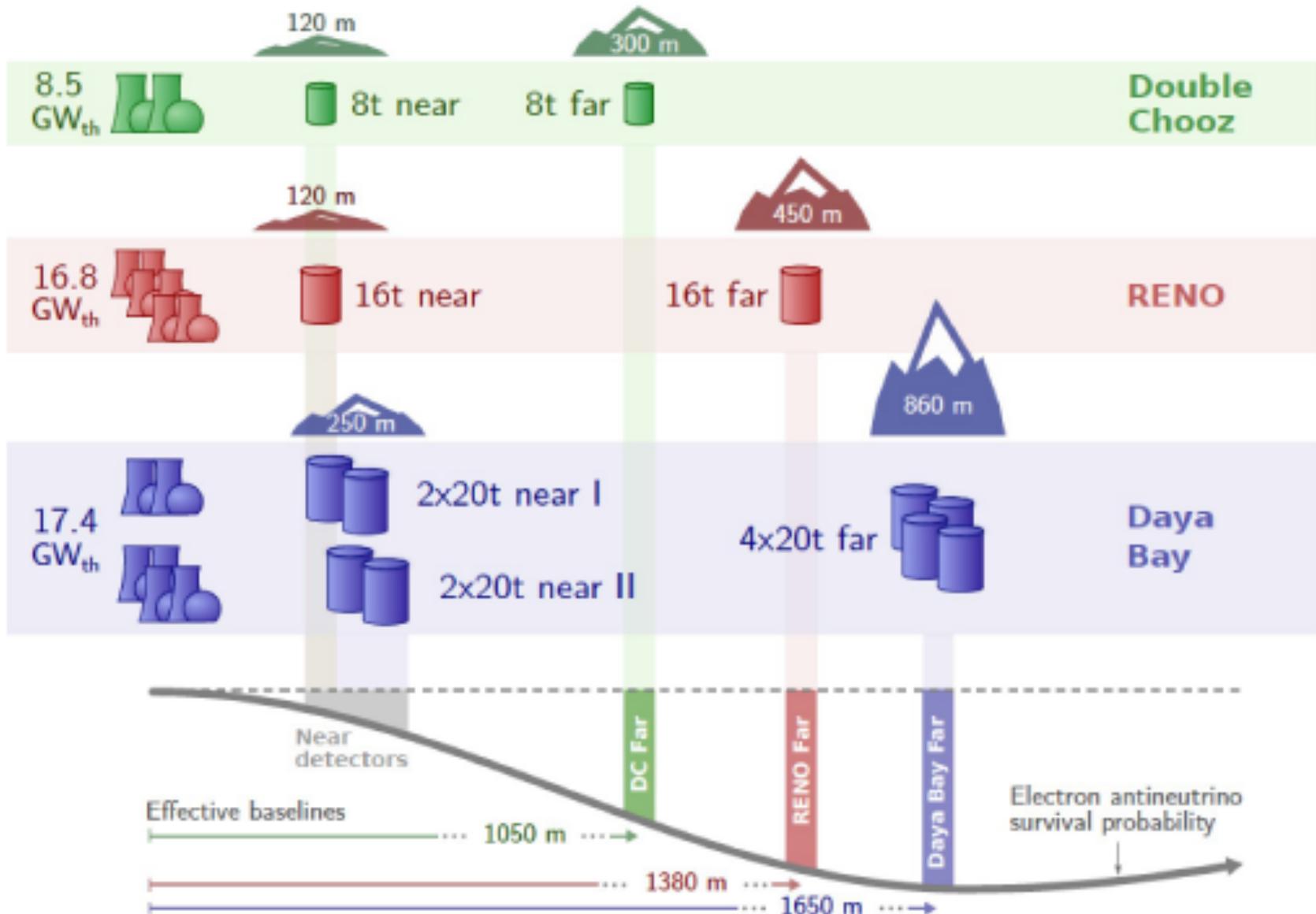


# Artificial sources: Reactor neutrinos

- Intense flux of anti- $\nu_e$ , produced “for free” by nuclear power plants  $E_\nu \sim \text{MeV}$ 
  - Used for first observations of neutrinos (Reines & Cowan)
  - anti- $\nu$  from  $\beta$ -decay of fission products, flux estimated by the fraction of isotopes that are fissioning at a given time and the reactor power
  - Average flux  $10^{20}$  anti- $\nu_e$  per second

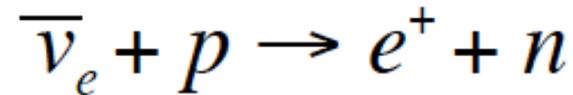


# Reactor neutrino experiments



# Detectors for reactor neutrino experiments

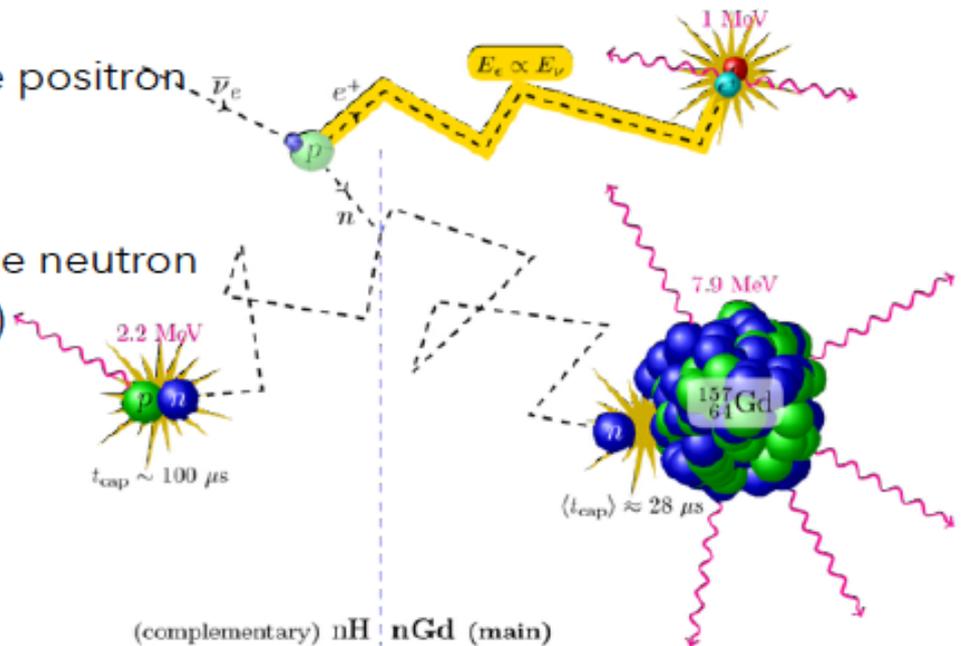
- ▶ Anti-neutrinos detected via inverse  $\beta$ - decay (IBD)



- ▶ search for 2 signal coincidence:

- ▶ instantaneous annihilation of the positron  
(**prompt signal**)

- ▶ thermalisation and capture of the neutron  
after some time (**delayed signal**)

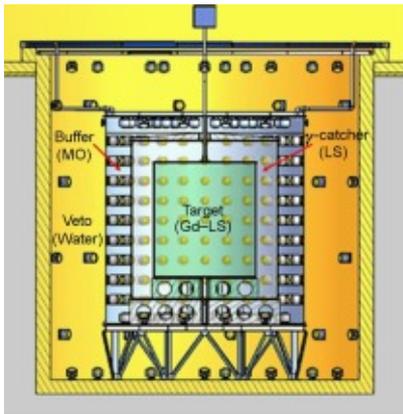


$E_{\text{Thr}}$  for anti-neutrinos 1.8 MeV

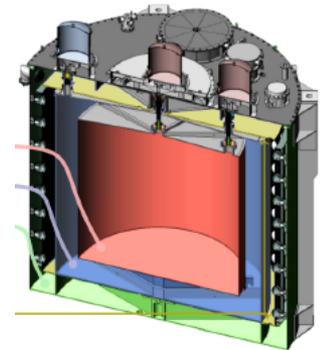
# Detectors for reactor neutrino experiments

- Reactor experiments (Daya-Bay, RENO and Double Chooz) have similar design and strategy: detection of inverse  $\beta$ -decay in liquid scintillator doped with Gd

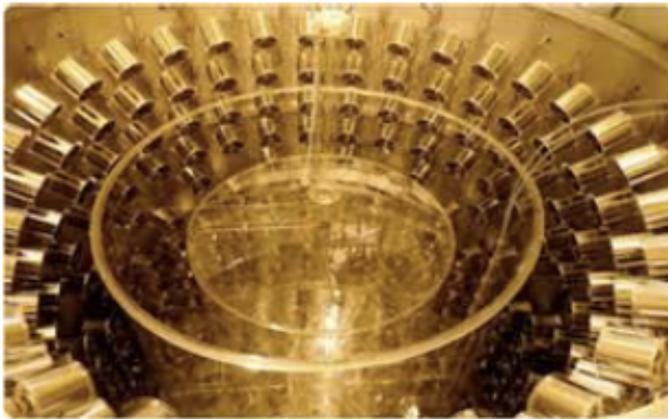
RENO



Daya Bay



Double Chooz detector

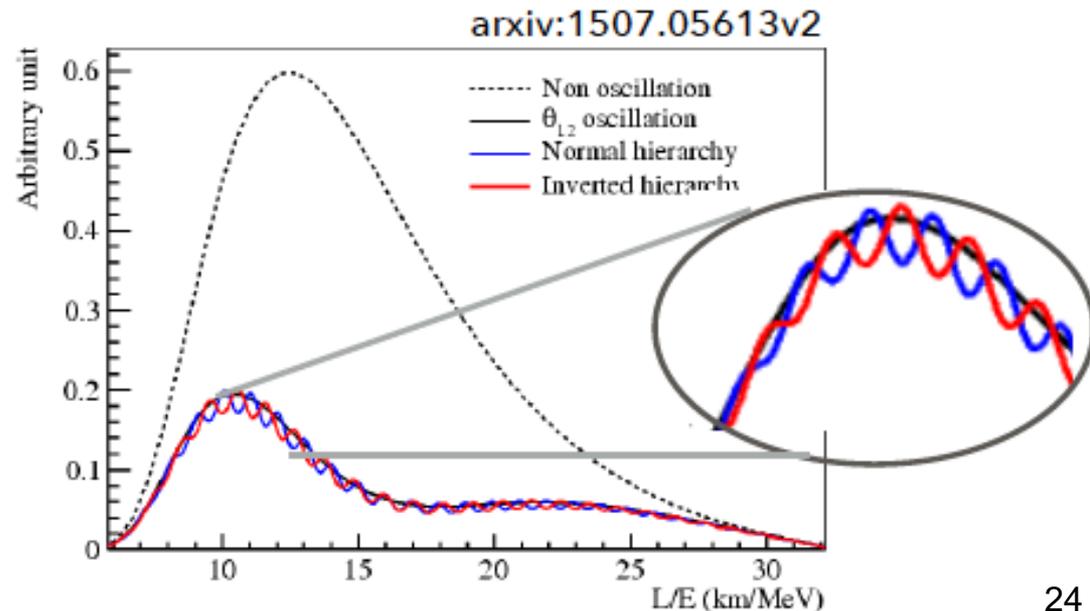
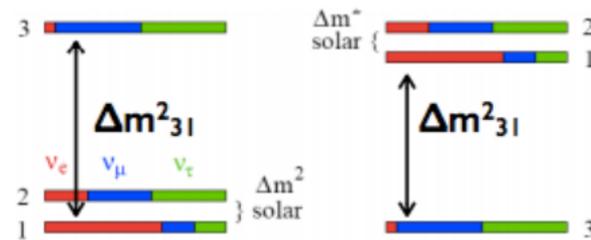


# Measurements with reactor neutrinos

- Measurement of anti- $\bar{\nu}_e$  disappearance

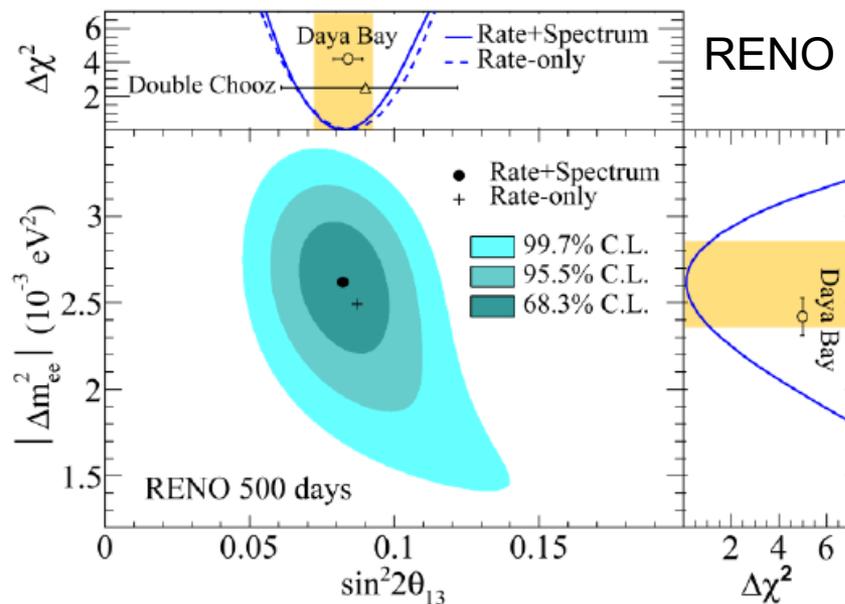
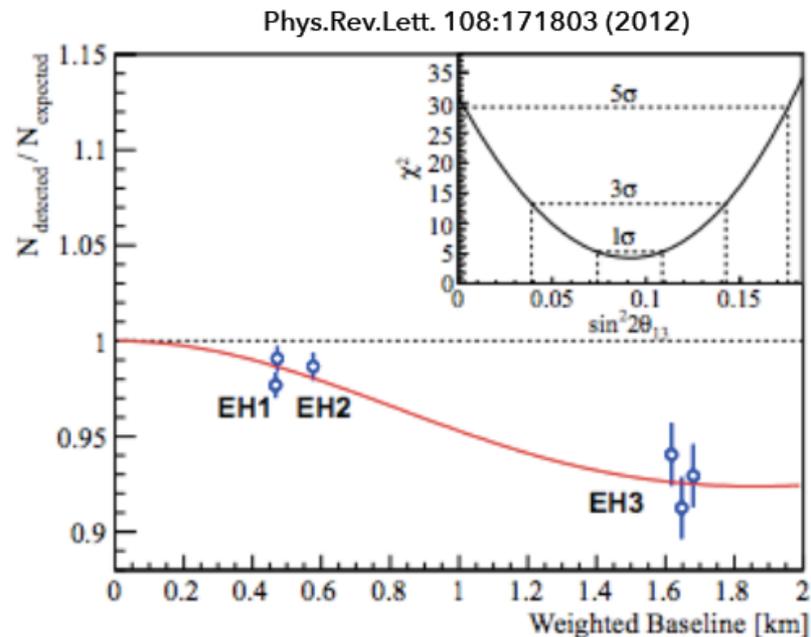
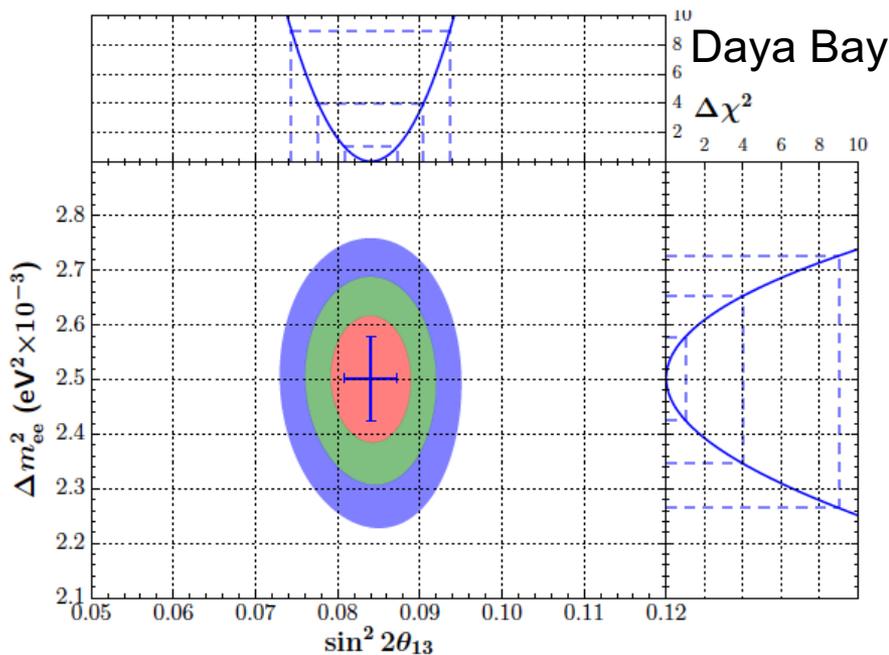
$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \Delta_{21} - \sin^2 2\theta_{13} (\cos^2 \theta_{12} \sin^2 \Delta_{31} + \sin^2 \theta_{12} \sin^2 \Delta_{32})$$

- Sensitivity to  $\theta_{13}$
- No sensitivity to  $\delta_{CP}$
- Sensitivity to mass hierarchy through oscillation interference  $\rightarrow$  spectral distortion (3% effect for medium baseline experiments)

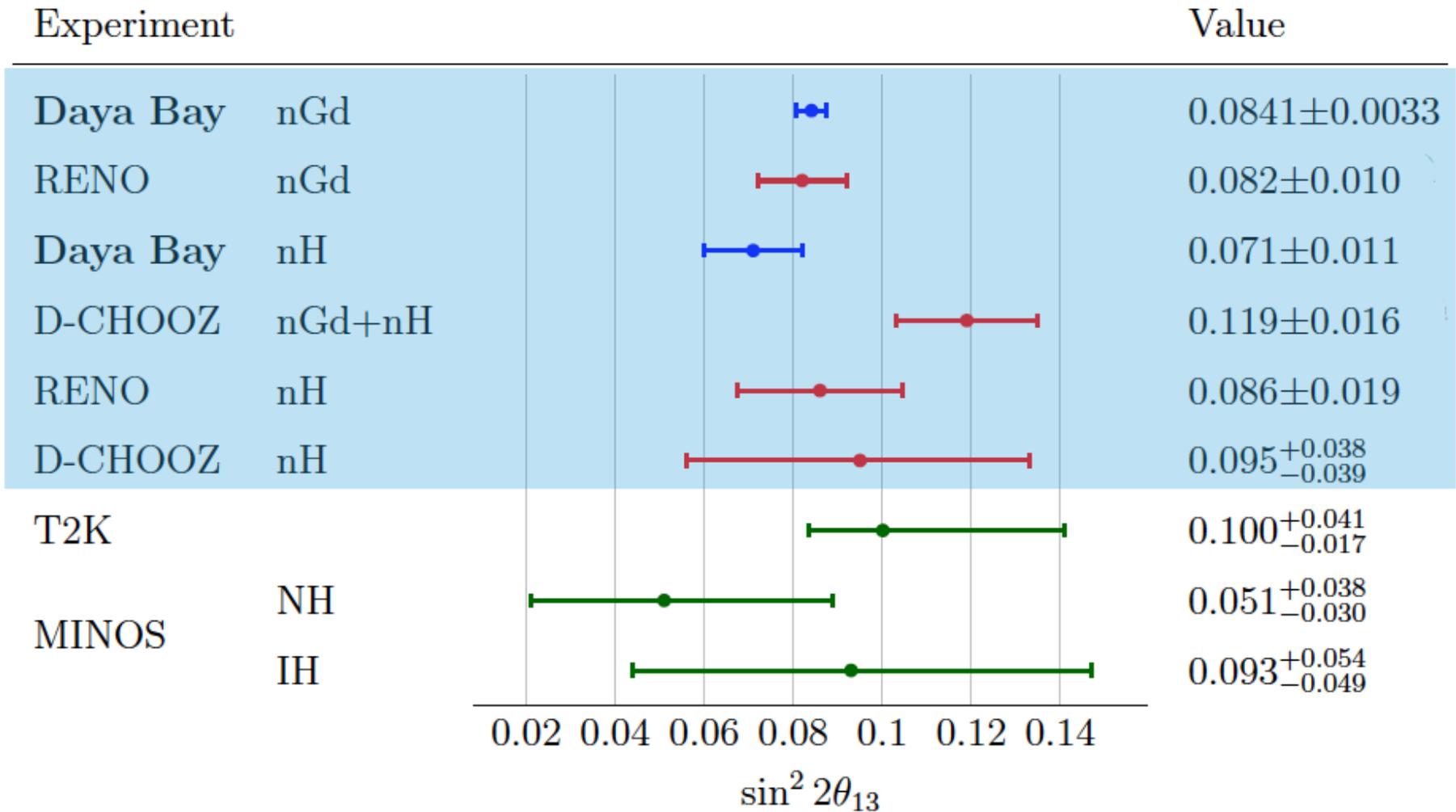


# Measurements of $\theta_{13}$

- Daya Bay (March 2012):  
 $\theta_{13} \neq 0$  with a significance of  $5.2\sigma$
- Since then more precise measurement and measurements by RENO and Double Chooz



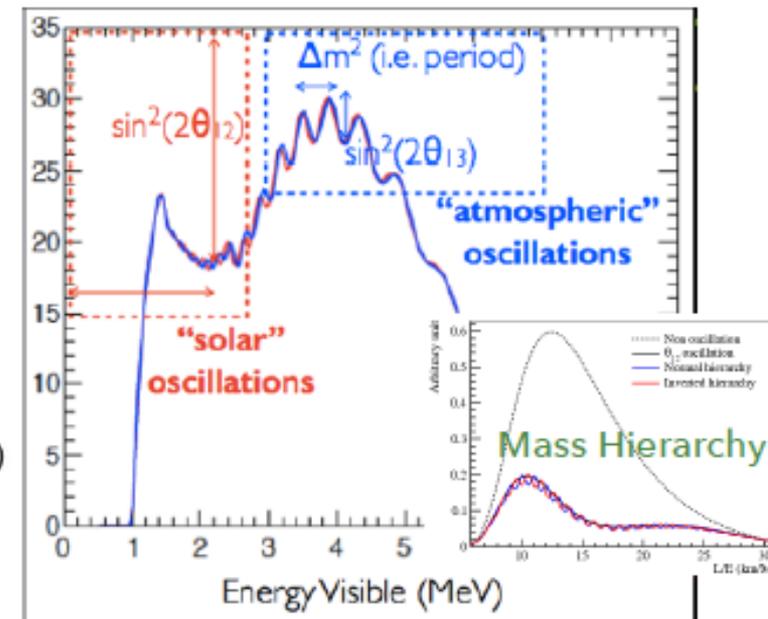
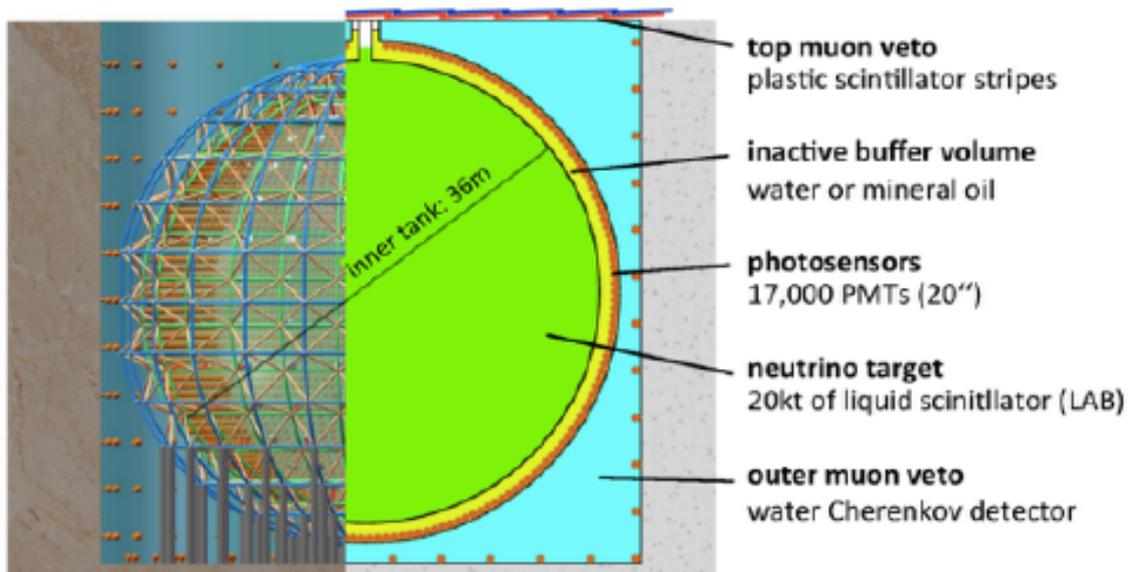
# Summary of measurements of $\theta_{13}$



# JUNO

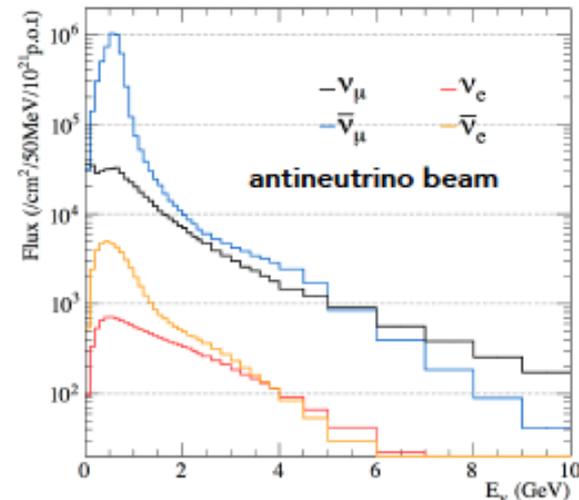
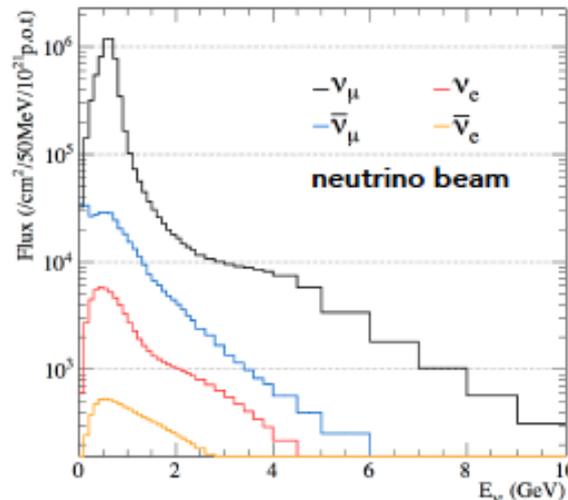
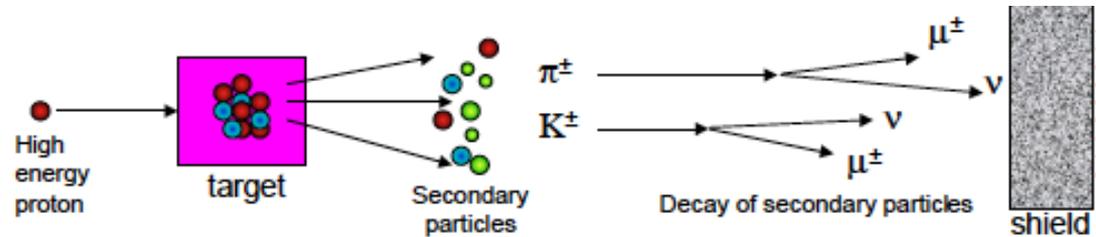


- ▶ JUNO: New reactor experiment in China: anti- $\nu_e$  from Daya Bay power plant
- ▶ 20 kton of liquid scintillator with wide physics program
- ▶ MH determination towards oscillation interference
  - ▶ big challenge in calorimetry! Need energy resolution better than 3% ( $\delta m^2/\Delta m^2 \sim 3\%$ )
- ▶ Data taking foreseen for > 2021



# Artificial sources: Accelerator neutrinos

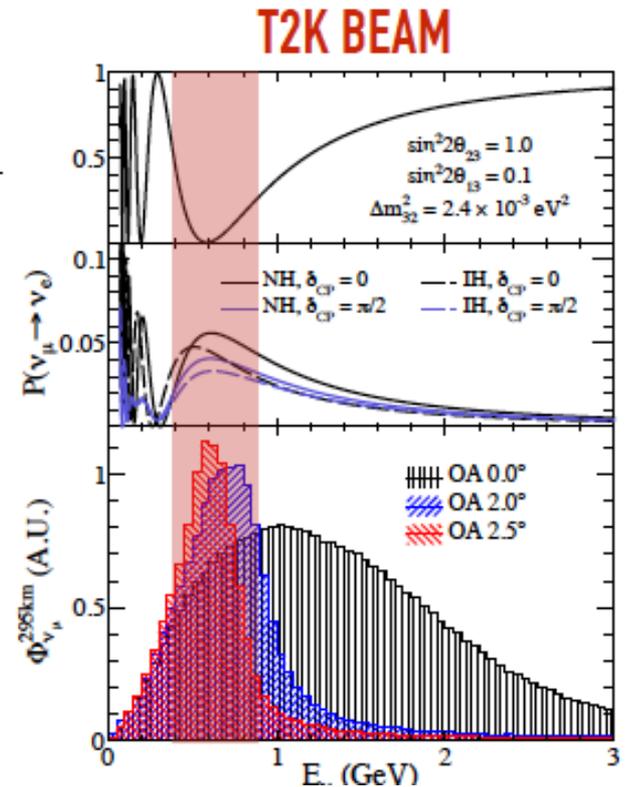
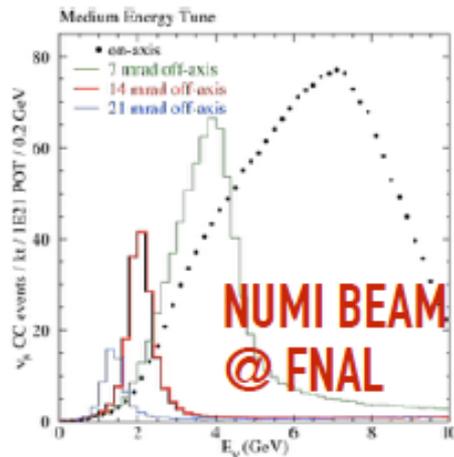
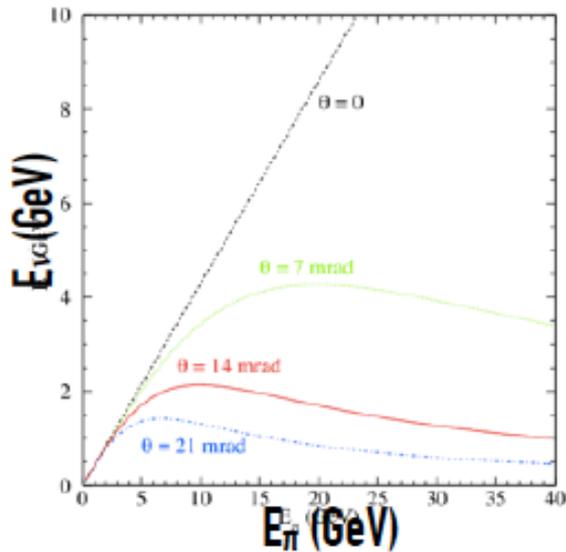
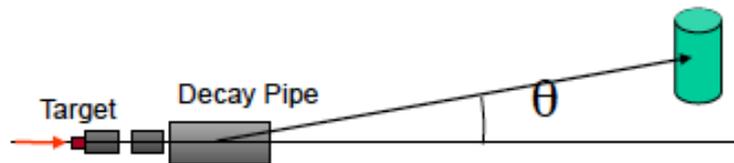
- First accelerator neutrinos by Lederman, Schwartz and Steinberger (1962) with  $E_\nu \sim 1$  GeV
- Same principle in modern experiments, better technique (focusing magnets)
- Possibility to produce both  $\nu_\mu$  and anti- $\nu_\mu$  beams
  - with some contamination of other  $\nu$  and anti- $\nu$  flavors



T2K flux at Super-Kamiokande  
PRL 116, 181801 (2016)

# Accelerator neutrinos: Off-axis technique

- Off-axis technique foresees detectors not aligned with the center of the neutrino flux, but shifted by some degrees
- Narrower energy spectrum at “low” energies
- Dependency from parent hadron energy removed
- Technique adopted by T2K and NOvA

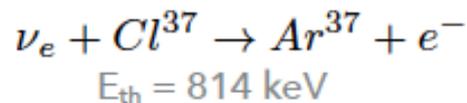
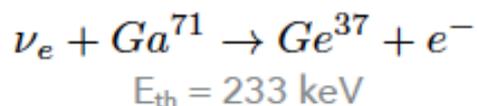


# Desirable features for neutrino detectors

- Low energy threshold
    - Low-energy neutrinos or secondary particles can be detected and studied
  - Good angular resolution
    - Particles direction accurately reconstructed – direction of neutrinos inferred from measured direction of charged leptons
  - Good particle identification
    - Discrimination of flavors  $e/\mu/\tau$  crucial for oscillation measurements
  - Good energy resolution
    - Measurement of neutrino energy crucial for extraction of oscillation parameters
  - Good time resolution
    - Time evolution of transient signals important for background rejection
  - Charge identification
    - Discrimination between leptons and anti-leptons important for oscillation measurements, in particular  $\delta_{CP}$
- Not possible to have all of these features in one detector
- Need to select most appropriate technology according to the aim of the experiment

# Detection of $\nu_e$ with radiochemical sources

- Very first approach to study solar neutrinos (Davis-Pontecervo)
- Production of radioactive isotopes
- $^{37}\text{Ar}$  and  $^{71}\text{Ga}$  are extracted chemically and counted by their decay products
  - No information about neutrino energy or direction



GALLEX (1991-1997)  
LNGS Italy

615 tons of cleaning fluid  $\text{C}_2\text{Cl}_4$   
Expected 1.5 Ar atoms/day

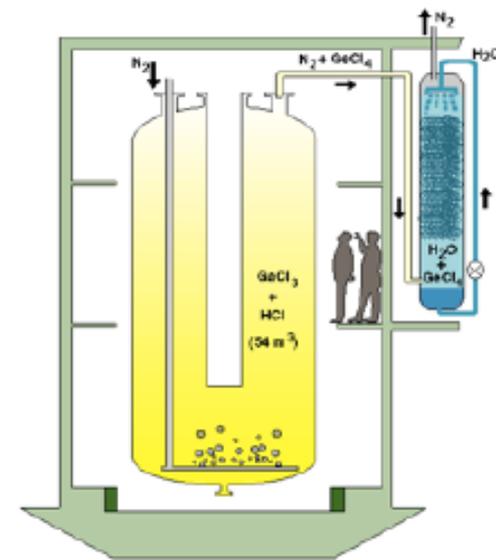


image courtesy of BNL



Davis experiment (1960's)  
Homestake mine, South Dakota  
*(same as DUNE!)*

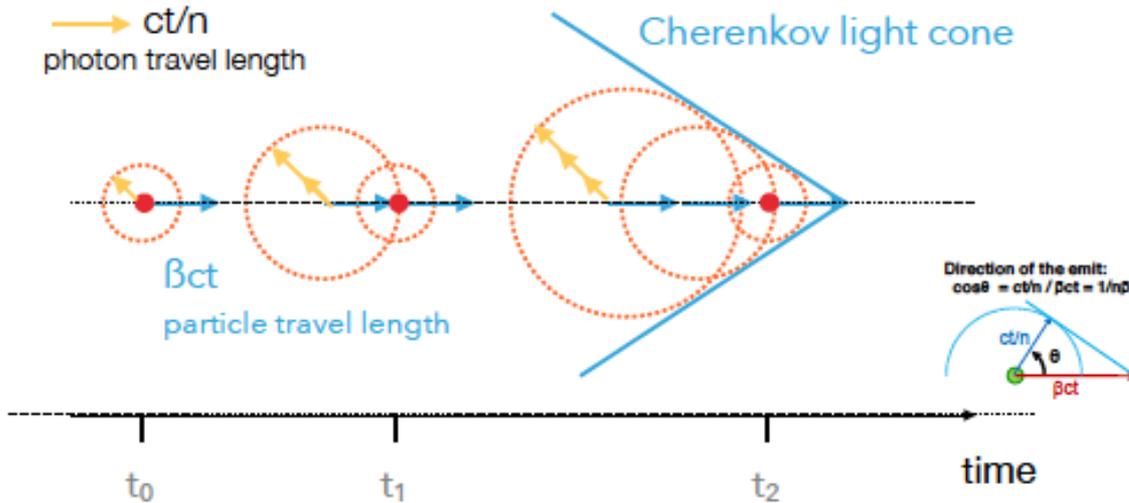
615 tons of cleaning fluid  $\text{C}_2\text{Cl}_4$   
Expected 1.5 Ar atoms/day

# Cherenkov radiation

- Presence of neutrino inferred from presence of charged lepton
  - Coherent emission of light from passage of charged particle through medium, if speed of particle is larger than the speed of light in the medium
- Threshold for emitting Cherenkov radiation depends on mass of the particle

  $\beta ct$   
 particle travel length

  $ct/n$   
 photon travel length



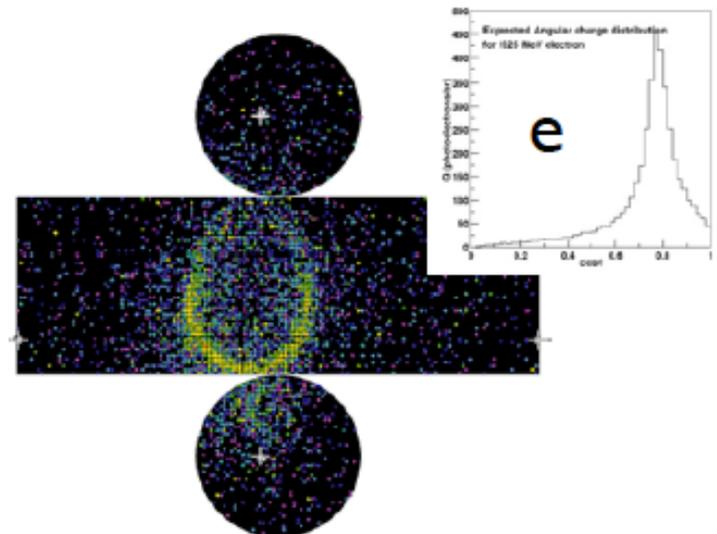
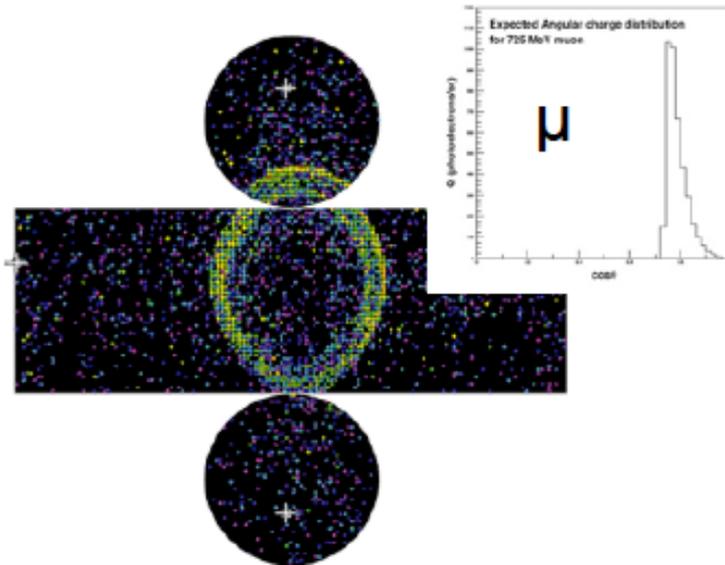
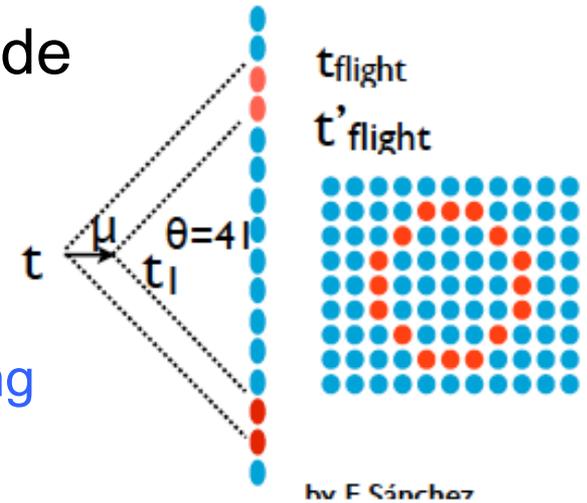
$$\beta > 1/n \simeq 0.75 \quad \gamma = \frac{1}{\sqrt{1-\beta^2}} \simeq 1.5$$

$$E_{Thr} = \gamma mc^2$$

particle	$E_{thr}$
electrons	0.755 MeV
muons	160.3 MeV
pions	211.7 MeV
protons	1407 MeV

# Particle identification

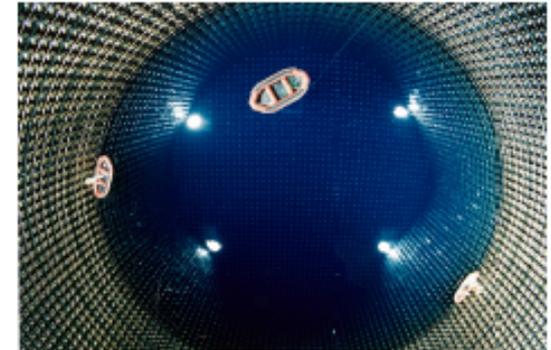
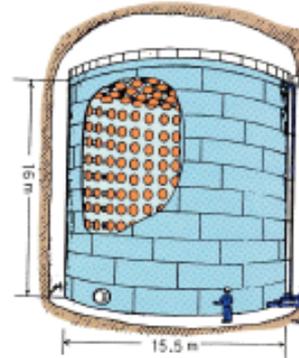
- Angular distribution of Cherenkov photons along the primary particle direction provide key to particle identification
- $e/\mu$  discrimination
  - Muons: sharp and clear ring
  - Electrons: fuzzy ring due to multiple scattering and showering



# Examples of Cherenkov detectors

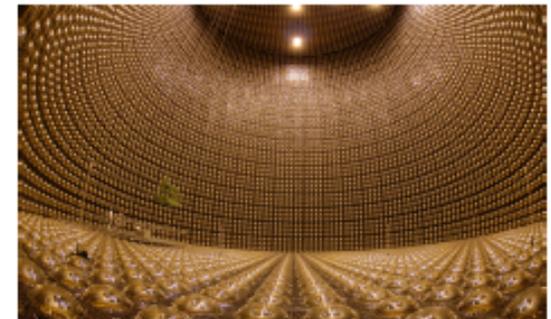
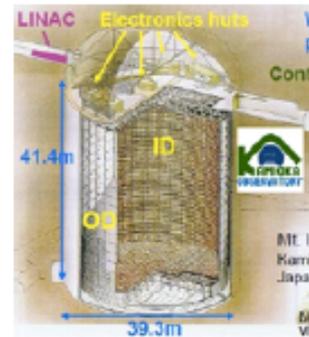
## Kamiokande (1983-1996)

- Nucleon decay experiment
- 4.5ktons of ultra pure water
- 984 (ID) + 123 (OD) PMTs (20-25% coverage)
- **discovery of oscillations with atmospheric neutrinos**



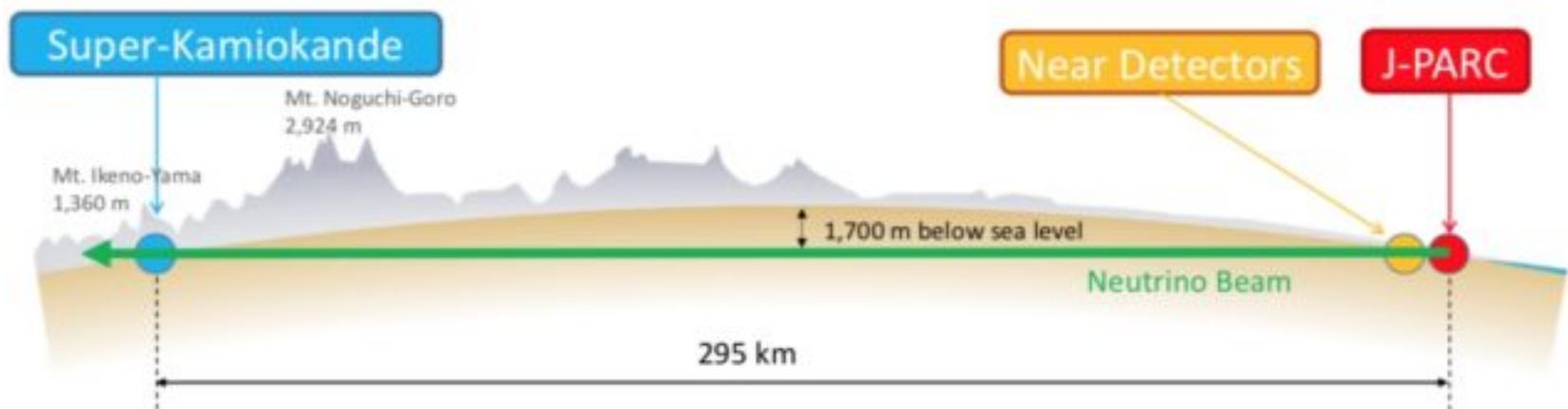
## Super-Kamiokande (1996-today)

- atmospheric neutrinos experiment + FD for the T2K experiment
- 50ktons of ultra pure water
- 11k (ID) + 2k (OD) PMTs (40% coverage)



# T2K: Accelerator neutrinos (since 2010)

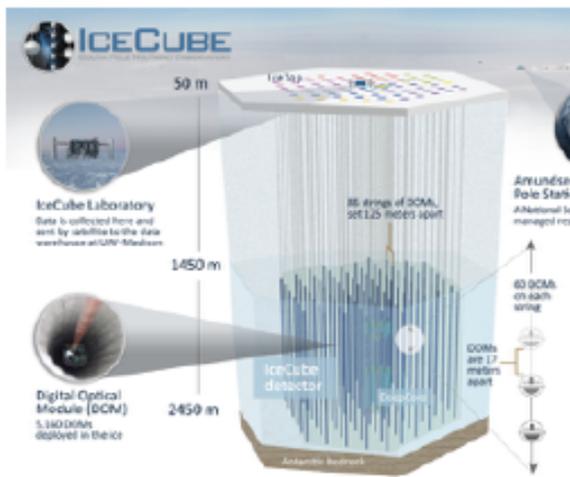
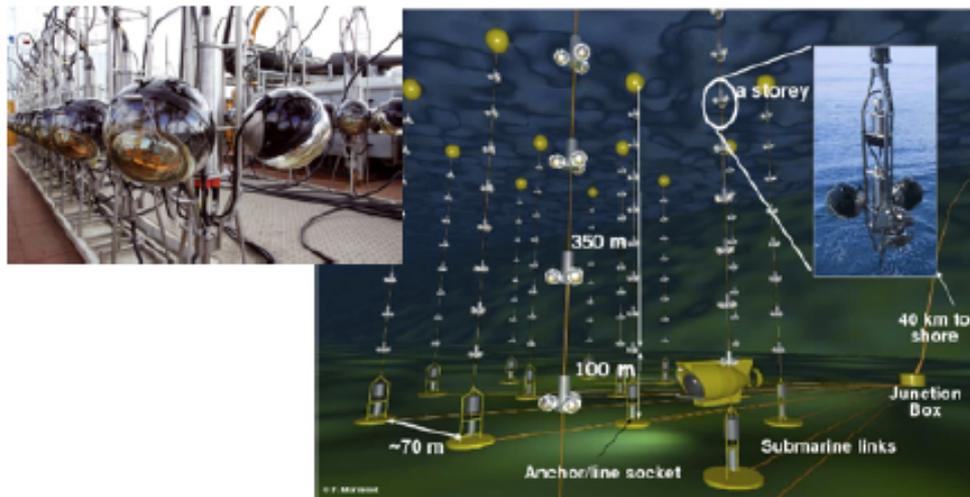
- T2K (Tokai to Kamioka): neutrino beams produced at JPARC
- Two near detectors at 280m from target
  - One to measure beam direction and intensity
  - Other (off-axis) to measured cross section, flux and flavor composition
- Then beam reaches SuperKamiokande after 295km
- Measurements of  $\nu_{\mu}$  disappearance
- First measurement of  $\nu_{e}$  appearance



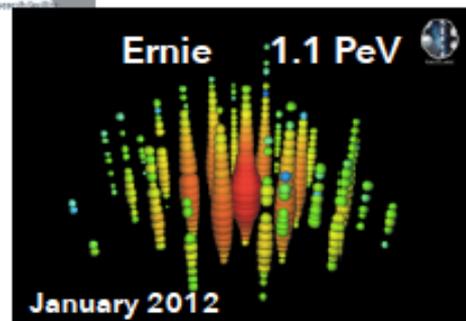
# Examples of Cherenkov detectors

## Antares (2008-2017)

- 12 separate vertical strings 350m long
- 75 optical modules each
- $E_\nu 10^{10} - 10^{14}$  eV
- astro-particle physics



Amundsen-Scott South Pole Station, Antarctica  
A National Science Foundation managed research station

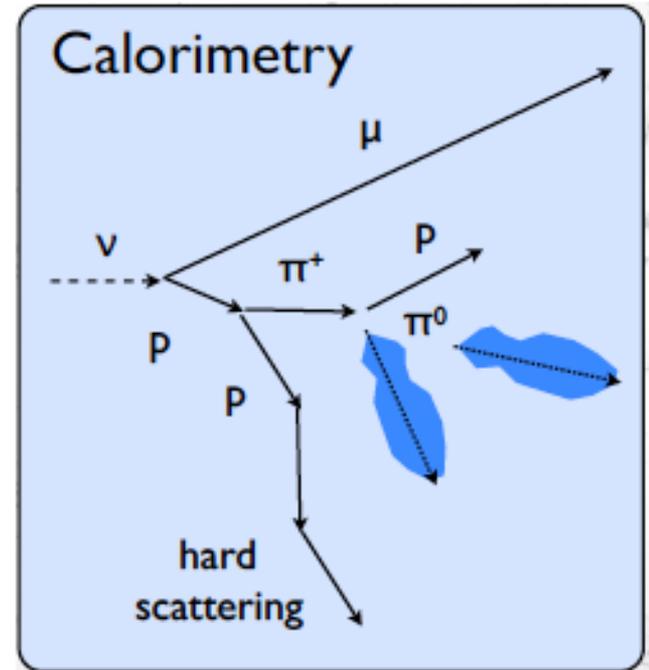


## IceCube (2011 - today)

- ▶ cubic-kilometer particle detector made of Antarctic Ice
- ▶ 5,160 digital optical modules (DOMs) attached in vertical string frozen in 86 boreholes (in-ice detector)
- ▶ beginning of searches for cosmogenic neutrino interactions

# Tracking Calorimetry

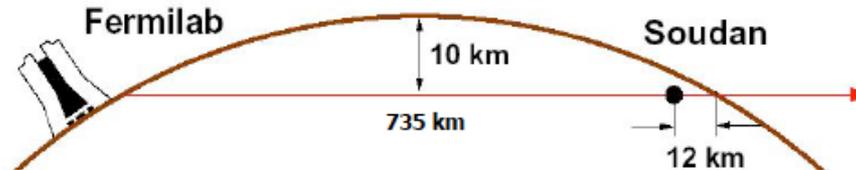
- Aim to detect and reconstruct all particles from neutrino interaction
- Two main types
  - Alternating detector layers
  - Monolithic (single volume detector)
- If magnetized
  - Charge determination  $\rightarrow$   $\nu$  or anti- $\nu$
  - Momentum from curvature of charged particle tracks



$$E_\nu = E_{lepton} + E_{had}$$

# Tracking Calorimetry: MINOS (2003-2016)

- 120 GeV proton beam at Fermilab,  $\langle E_\nu \rangle \sim 3$  GeV
- Near detector at 1km, far detector at Soudan mine at 735km



First measurement of  $\nu_\mu$  disappearance

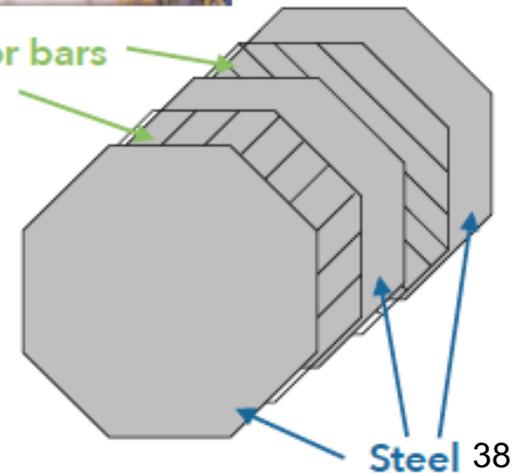
1kton



5.4kton

- Magnetized (1.3T) steel/scintillator sampling calorimeter/tracking
  - 2.54cm steel absorbers  $\sim 1.4X_0$
  - 1 cm thick plastic scintillator bars with orthogonal direction in alternating layers

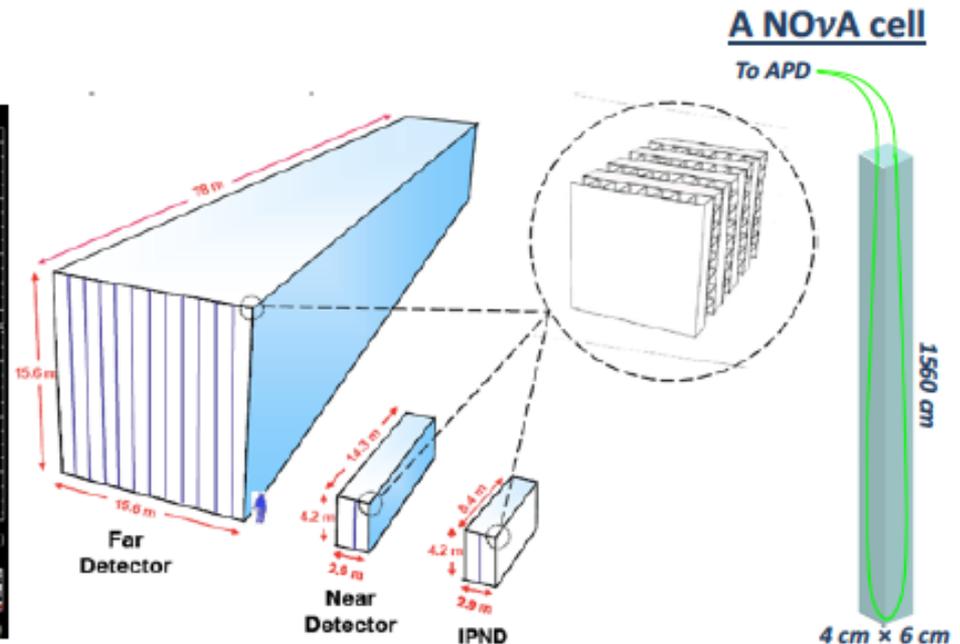
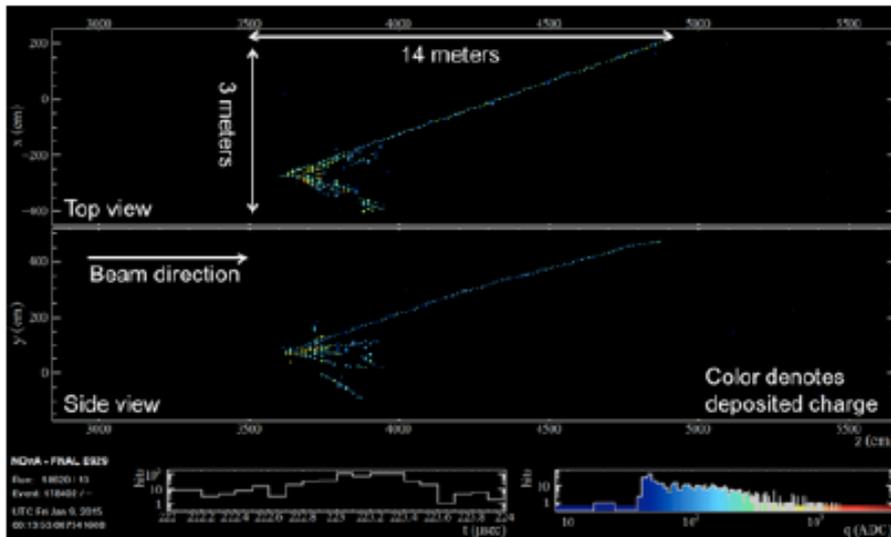
Scintillator bars  
( $\pm 45^\circ$ )



Steel 38

# Tracking Calorimetry: NOvA (since 2014)

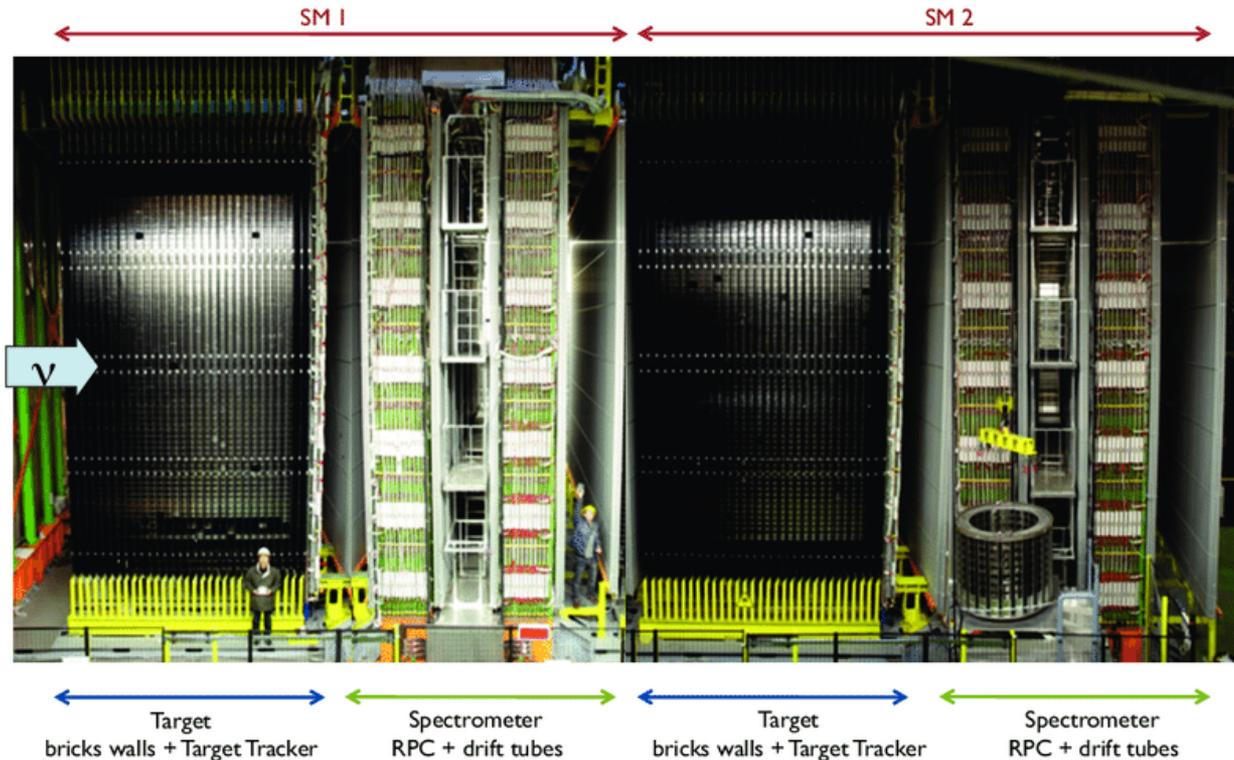
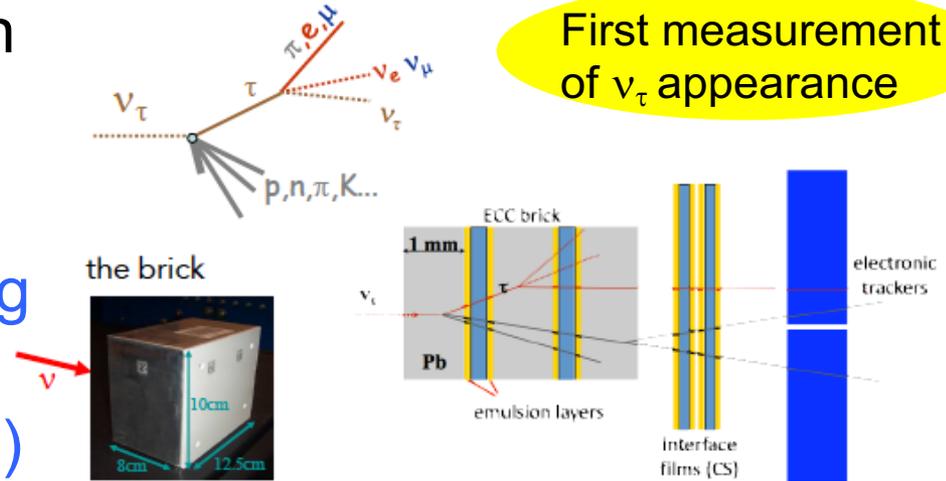
- 120 GeV proton beam at Fermilab,  $\langle E_\nu \rangle \sim 3$  GeV
- Far detector at Soudan mine at 735km
- Uses off-axis technique
- 385'000 high refracting plastic PVC cells filled with liquid scintillators
- Energy deposited by incoming particles collected by wavelength shifting fibers



# Tracking Calorimetry: OPERA (2008-2012)

- Optimized for reconstruction of  $\nu_\tau$  interactions
- $\langle E_\nu \rangle \sim 17$  GeV
- Modular structure alternating lead sheets and emulsion films (1.25 kton target mass)

First measurement of  $\nu_\tau$  appearance



# Measurements at accelerator experiments

$$P(\nu_\mu \rightarrow \nu_e) \sim \boxed{\sin^2 2\theta_{13}} \times \boxed{\sin^2 \theta_{23}} \times \boxed{\frac{\sin^2[(1-x)\Delta]}{(1-x)^2}} \\
 \boxed{-\alpha \sin \delta} \times \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \times \sin \Delta \frac{\sin[x\Delta]}{x} \frac{\sin[(1-x)\Delta]}{(1-x)} \\
 + \alpha \cos \delta \times \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \times \cos \Delta \frac{\sin[x\Delta]}{x} \frac{\sin[(1-x)\Delta]}{(1-x)} \\
 + \mathcal{O}(\alpha^2)$$

$$\alpha = \left| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \right| \sim \frac{1}{30} \quad \Delta \equiv \frac{\Delta m_{31}^2 L}{4E} \quad \boxed{x \equiv \frac{2\sqrt{2}G_F N_e E}{\Delta m_{31}^2}}$$

matter effects

M. Freund, Phys.Rev. D64 (2001) 053003

- Sensitivity to  $\theta_{23}$
- Sensitivity to  $\theta_{13}$  as reactor measurement have determined that  $\theta_{13}$  is not too small
- Measurement of  $\delta_{CP}$  only possible at accelerator experiments
- Sensitivity to mass hierarchy due to matter effects

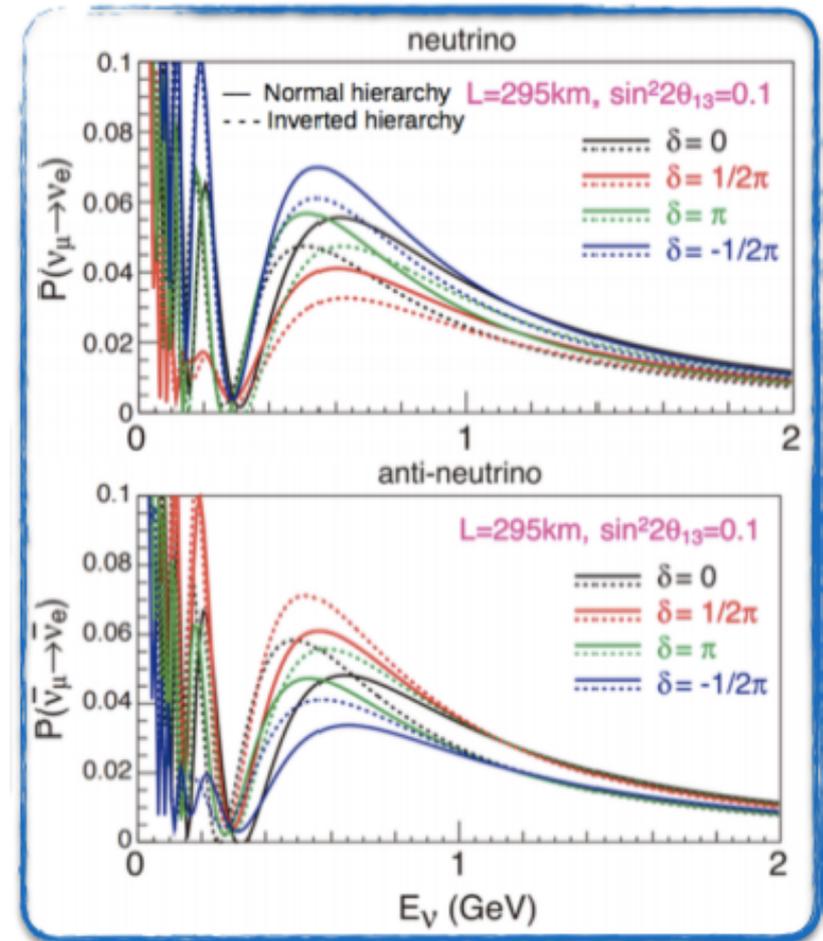
# Measurement of $\delta_{CP}$

- Measurement is (in principle) simple: looking for different behavior between neutrino and anti-neutrino oscillations

e.g. if  $\delta_{CP} = :$

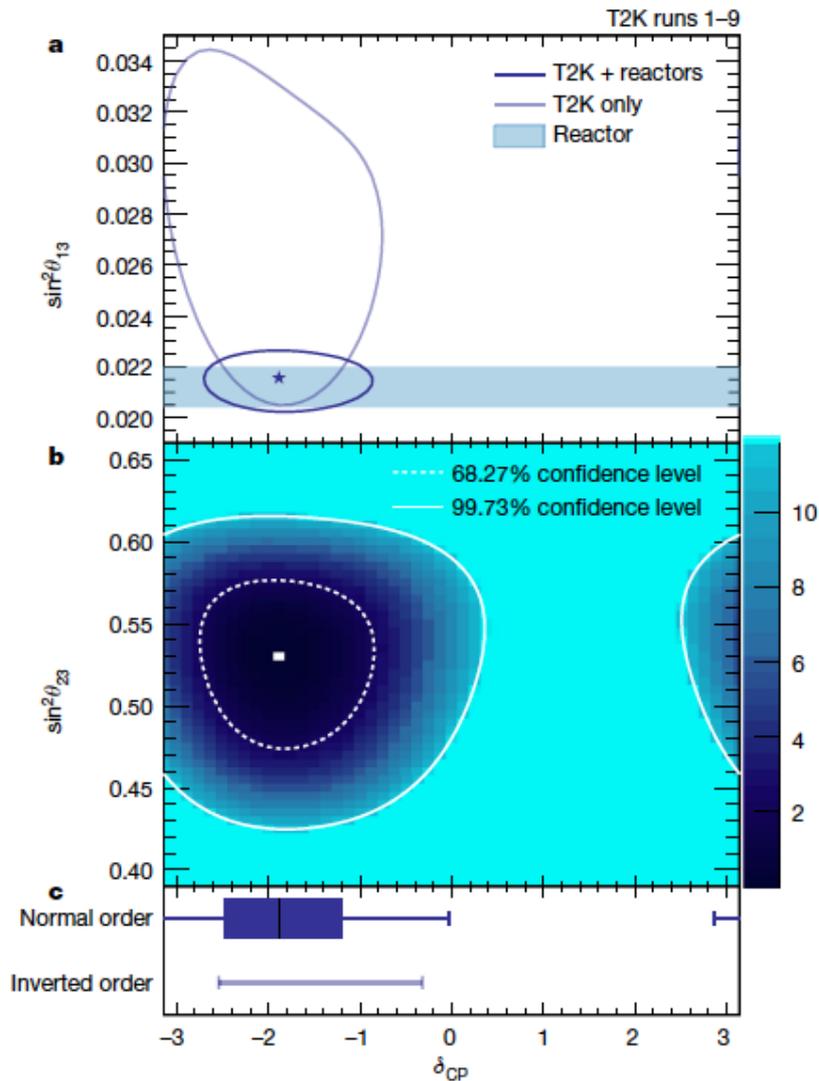
- ▶  $0, \pi$  : no CP violation  $P(\nu_\mu \rightarrow \nu_e) = P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$
- ▶  $-\pi/2$  : enhance  $P(\nu_\mu \rightarrow \nu_e)$  suppress  $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$
- ▶  $+\pi/2$  : suppress  $P(\nu_\mu \rightarrow \nu_e)$  enhance  $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$

- Complicated by matter effects
- Complicated by beam contamination
- Dependence on  $\theta_{13}$



# Measurement of $\delta_{CP}$

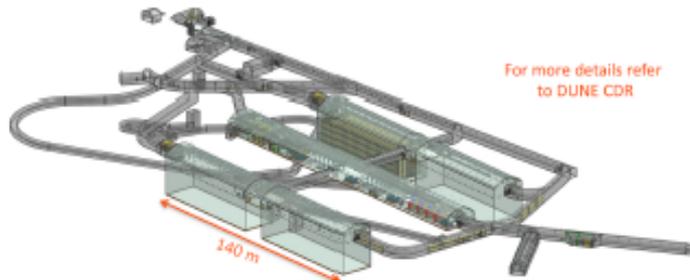
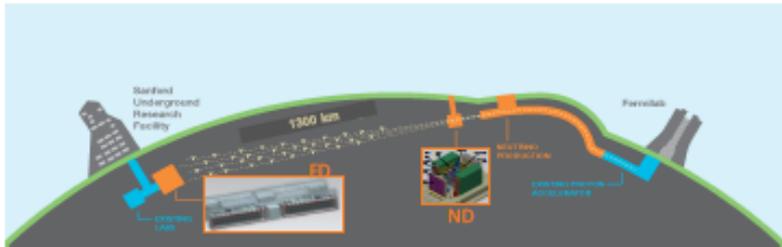
- T2K results published this month exclude CP conservation at 95% confidence level *Nature* volume 580, pages 339–344(2020)



# Future accelerator-based experiments

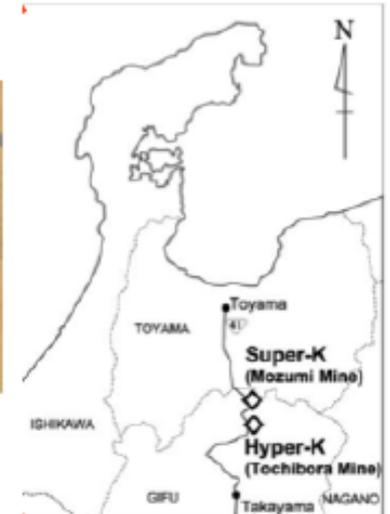
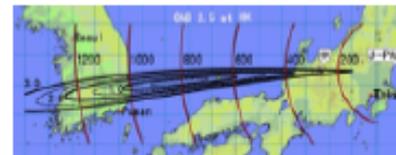
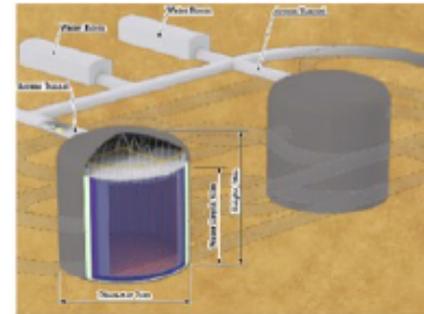
## DUNE

- 4 modules Liquid Ar-TPC ~10kton each
- SURF, Homestake mine (US) ~2400mwe
- On-axis beam from Fermilab (1.2-2.4 MW)
- baseline ~1300km
- $\langle E_\nu \rangle \sim 3\text{GeV}$



## HYPER-KAMIOKANDE

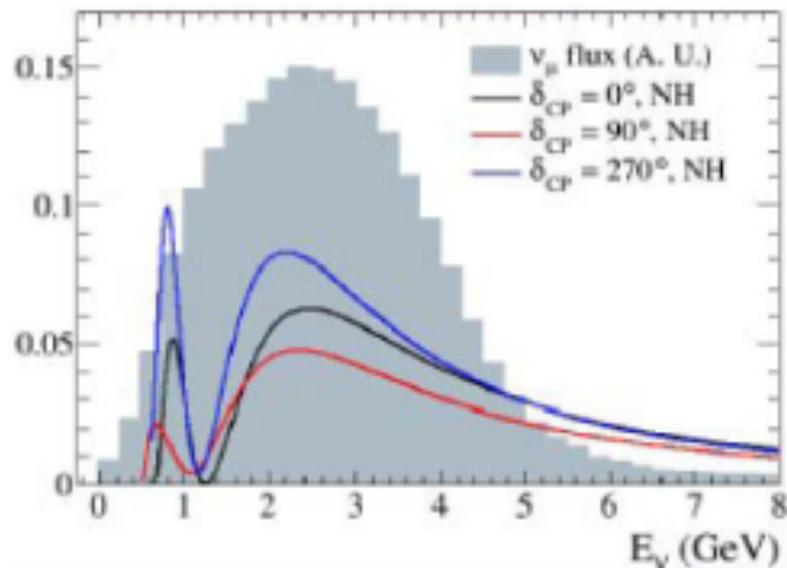
- 2 water Cherenkov of ~260 ton each
- Tochibora, near Kamioka (Japan), ~1750mwe
- Off-axis beam from Tokai (1.3 MW)
- baseline ~300km (1100km if T2HKK)
- $\langle E_\nu \rangle \sim 0.6\text{GeV}$



# Future accelerator-based experiments

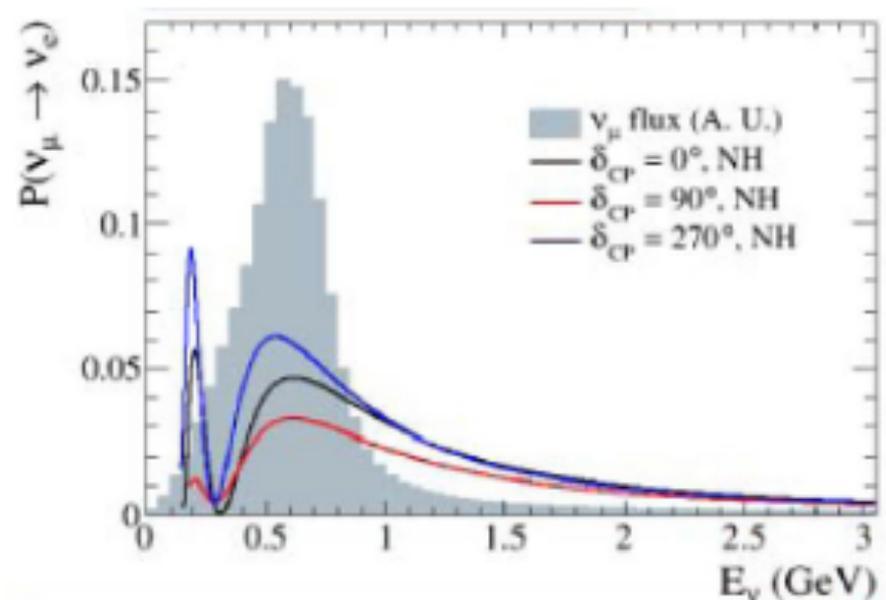
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- 4 modules Liquid Ar-TPC ~10kton each
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- baseline ~1300km
- $\langle E_\nu \rangle \sim 3\text{GeV}$



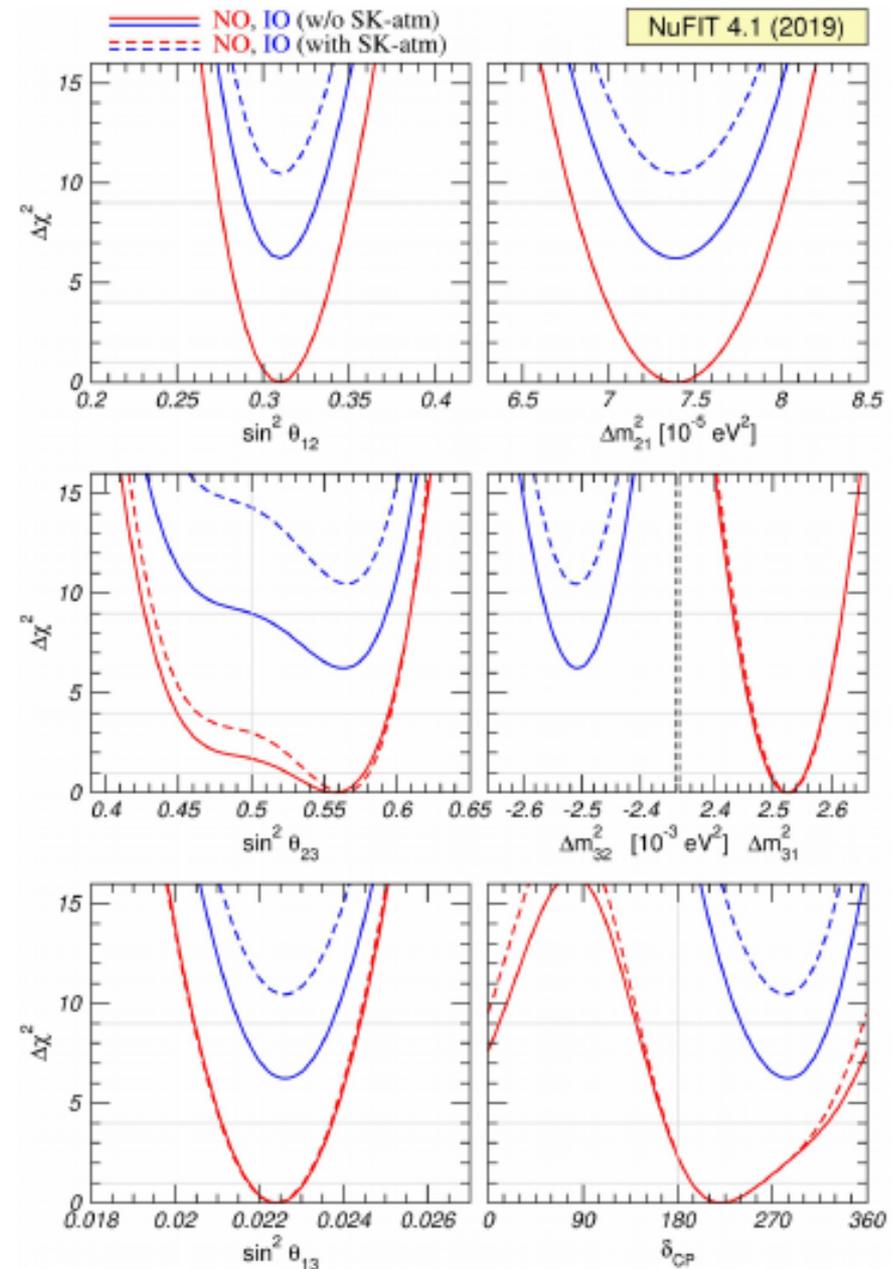
## HYPER-KAMIOKANDE

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- baseline ~300km (1100km if T2HKK)
- $\langle E_\nu \rangle \sim 0.6\text{GeV}$



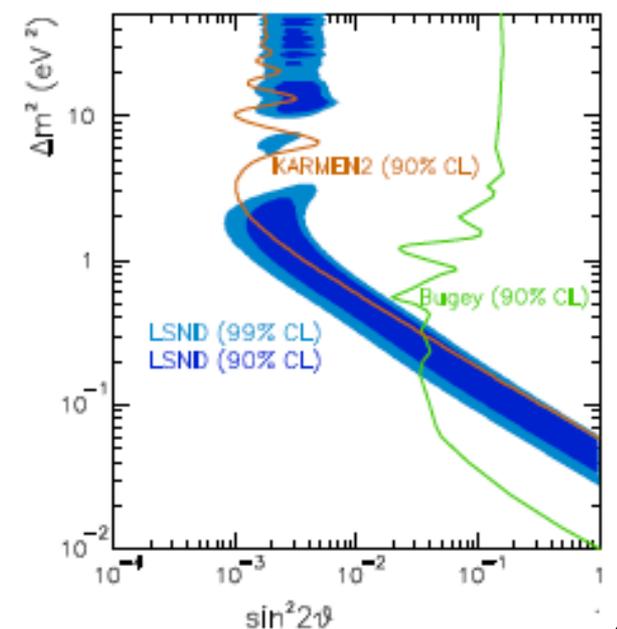
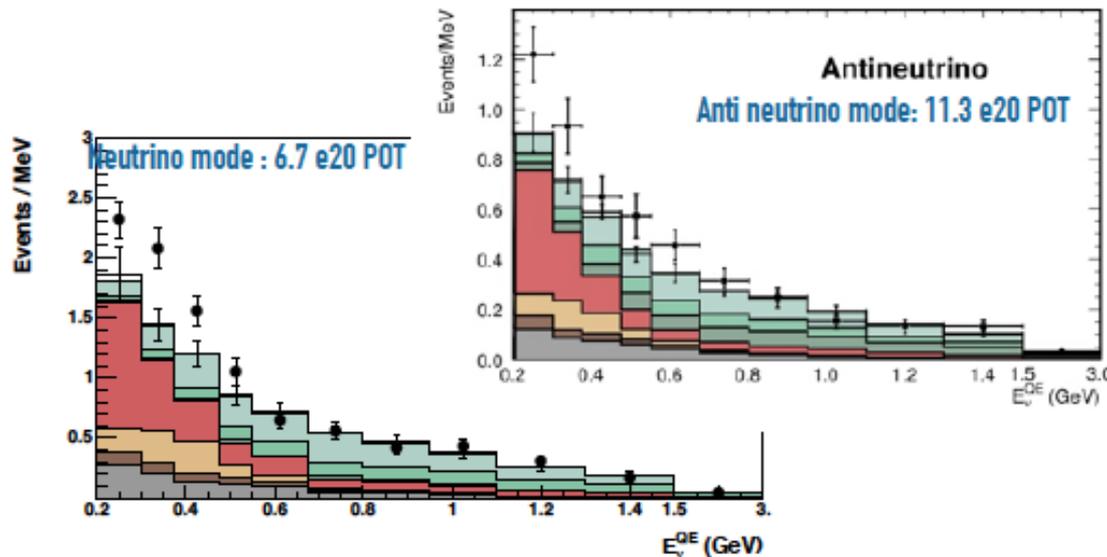
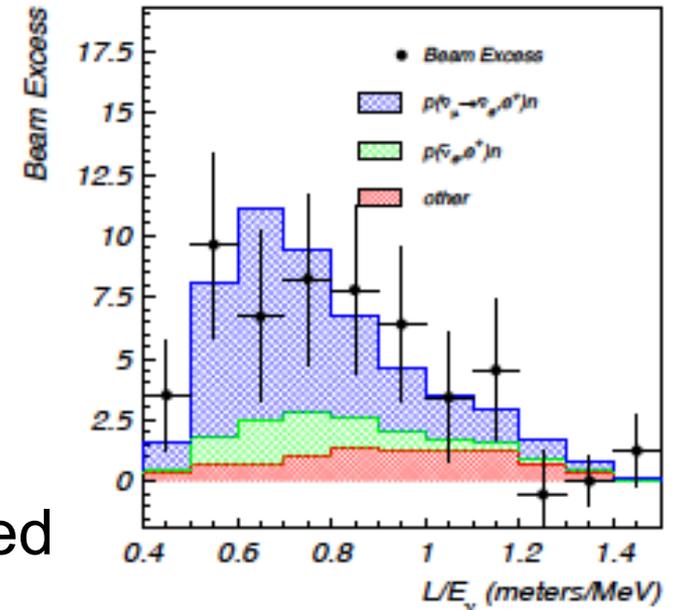
# Summary of 3 flavor neutrino oscillation measurements

- Complementary and consistent measurements of three mixing angles and two mass<sup>2</sup> differences using solar, atmospheric, reactor and accelerator neutrinos
- Improved measurement of  $\theta_{23}$ , determination of mass hierarchy and search for CP violation in lepton sector being addressed by current and future experiments



# LSND anomaly

- LSND (1993-1998) with  $L/E \sim m/\text{MeV}$  observed excess in appearance of  $\bar{\nu}_e$  from  $\bar{\nu}_\mu$  beam
- Compatible with oscillations with  $\Delta m^2 \sim 0.2 \text{ eV}^2$  ( $\gg \Delta m^2_{\text{atmo}}, \Delta m^2_{\text{solar}}$ )
- Large regions of phase space excluded by KARMEN and Bugey
- Excess seen by MiniBooNE



# Interpretation as sterile neutrino

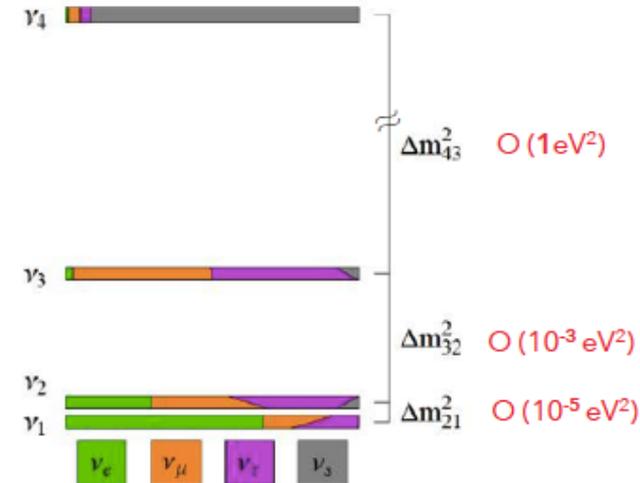
▶ Considering the 3+1 model. Because of the large mass splitting ( $1\text{eV}^2$ ), the other neutrino masses appear degenerate

▶  $\Delta m^2_{41} \approx \Delta m^2_{43} \approx \Delta m^2_{24}$

▶ approximation to 2 neutrino flavour-mixing

$$P_{\nu_{\alpha} \rightarrow \nu_{\beta}}^{SBL(-)} \simeq \sin^2 2\vartheta_{\alpha\beta} \sin^2 \left( \frac{\Delta m^2_{41} L}{4E} \right) \quad \sin^2 2\vartheta_{\alpha\beta} = 4|U_{\alpha 4}|^2 |U_{\beta 4}|^2$$

$$P_{\nu_{\alpha} \rightarrow \nu_{\alpha}}^{SBL(-)} \simeq 1 - \sin^2 2\vartheta_{\alpha\alpha} \sin^2 \left( \frac{\Delta m^2_{41} L}{4E} \right) \quad \sin^2 2\vartheta_{\alpha\alpha} = 4|U_{\alpha 4}|^2 (1 - |U_{\alpha 4}|^2)$$



$\nu_e$  DIS  
 $\sin^2 2\vartheta_{ee} \simeq 4|U_{e4}|^2$

$\nu_{\mu}$  DIS  
 $\sin^2 2\vartheta_{\mu\mu} \simeq 4|U_{\mu 4}|^2$

$\nu_{\mu} \rightarrow \nu_e$  APP  
 $\sin^2 2\vartheta_{e\mu} = 4|U_{e4}|^2 |U_{\mu 4}|^2 \simeq \frac{1}{4} \sin^2 2\vartheta_{ee} \sin^2 2\vartheta_{\mu\mu}$   
 [Okada, Yasuda, IJMPA 12 (1997) 3669; Bilenky, CG, Grimus, EPJC 1 (1998) 247]

# Addressing the anomaly

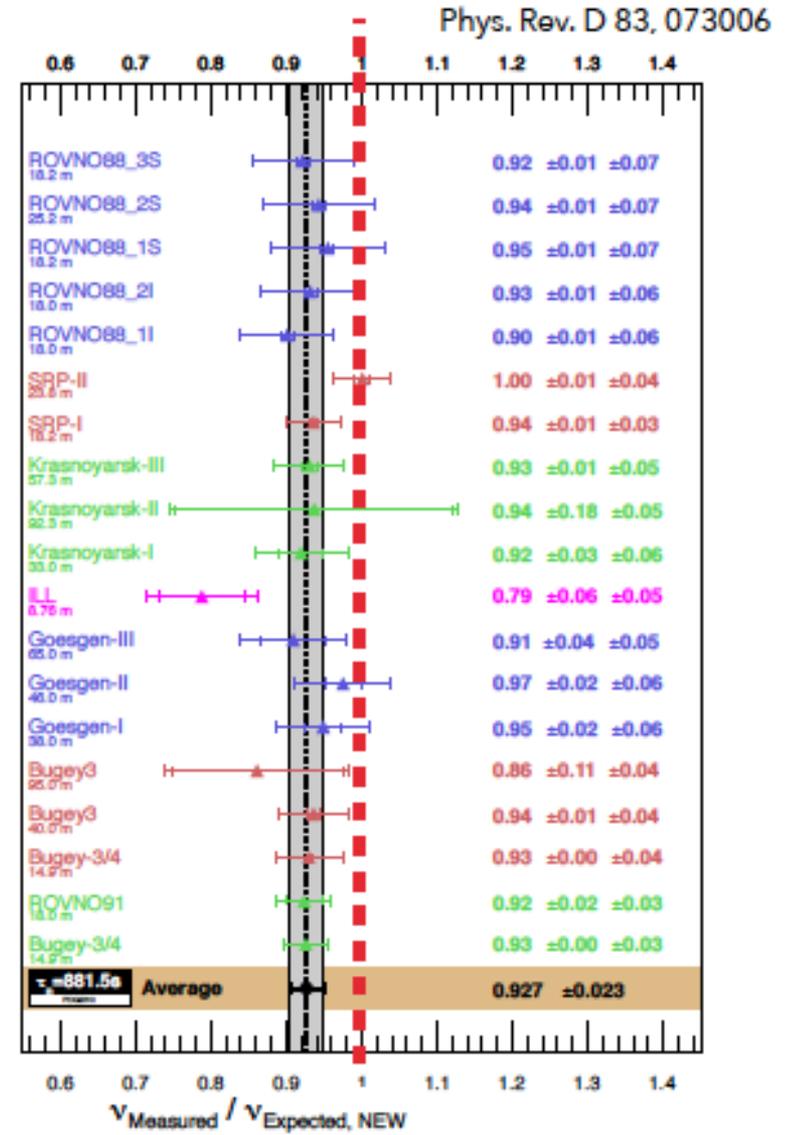
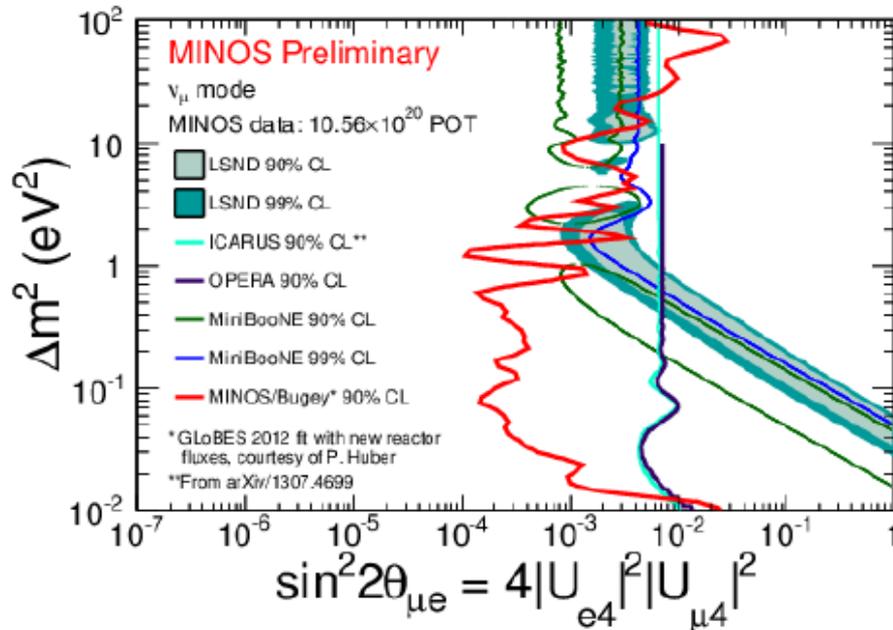
$\nu_e$  DIS:

- Almost all short baseline reactor neutrino experiments show deficits in measured neutrino flux

$\nu_\mu$  DIS:

- No anomaly seen at accelerator experiments

→ To be followed



$$R_{\text{avg}} = 0.927 \pm 0.023$$

# References

- CERN Academic training lectures, "Neutrinos", March 2017:  
Pilar Hernandez and Stefania Bordoni  
<https://indico.cern.ch/event/610409/>
- Lecture notes Pilar Hernandez "Neutrino physics"  
<https://arxiv.org/abs/1708.01046>
- Nico Serra, KTII lecture, 2017
- Stefania Ricciardi, Lecture notes on neutrino oscillations in matter, 2013