Course overview

Crystal lattice phenomena's

- -- Crystal structures (Real and reciprocal space)
- -- Scattering theory (Bragg's law, Form Factor, Structure factor)
- -- Crystal bindings (Equilibrium lattice constants, binding energies)
- -- Lattice vibrations (Phonon dispersions, density of state, heat capacity)

Electronic phenomena's

- -- Free electron gas (Fermi Dirac distribution, density of states)
- -- Band structure (electronic masses, Fermi surfaces)
- -- Electronic measurements (Heat capacity, resistivity, Hall effect, quantum oscillations)
- -- Electronic phases (metals, semi-metals, semi-condductors, band insulators)

Exam Structure

10 min – Presentation:

Topics: (1) Crystal structures, (2) Crystal Bindings, (3) Reciprocal lattice+ scattering theory,
(4) Crystal vibrations (Phonons), (5) Heat capacity (6) Band structure
(7) Semiconductors

20 min – Discussion:

- (a) Questions to the lecture material
- (b) Questions to the exercises

- End Exam

5 min - evaluation

5 min – Results: Passed / failed, grade will be known at a later point.

MY AVAILABILITY BEFORE EXAM:

30th-31th May 1st and 6th of June

johan.chang@physik.uzh.ch

Exercise 5 Sphere packings

Calculate the ratio c/a of an ideal hexagonal dense sphere packing (hcp) and its packing density. Compare the packing density to that of an fcc lattice and explain your findings.

http://quiz.thefullwiki.org/Solid-state_physics

Question 1: Here, the electrons are modelled as a <u>Fermi gas, a gas</u> of particles which obey the quantum mechanical _____.

- (1) Dirac delta function
- (2) Fermi–Dirac statistics
- (3) Boltzmann distribution
- (4) Maxwell–Boltzmann distribution

Question 2: This structure can be investigated using a range of <u>crystallographic techniques, including</u>, <u>neutron diffraction</u> <u>and electron diffraction.</u>

- (1) X-ray crystallography
- (2) Atom
- (3) Protein
- (4) Protein structure

Question 5: Phonons are also necessary for understanding the lattice <u>heat capacity of a solid, as in the Einstein model</u> and the later .

- (1) Copper
- (2) Debye model
- (3) Zinc
- (4) Carbon

https://www.crcpress.com/downloads/IP662/IP662_Questions.pdf

- 2.5 The cohesive energy of a solid is 9 eV/atom. What does this tell you about the solid?
- 2.6 What types of bonding are present in a graphite crystal?
- **2.10** Calculate the packing fraction of the face-centered cubic structure.

4.10(a) What are alloys of copper and zinc commonly known as?

- 5.1(a) State the Bragg law.
- 5.4(a) What types of radiation other than X-rays are commonly used to obtain diffraction patterns?
- 6.6(a) Does the resistivity of a metal increase or decrease with temperature?
- **6.8(a)** Which principle do electrons in a Fermi gas obey?

Today's program

Physics 481: Condensed Matter Physics - Midsemester test

Friday, March 4, 2011

Problem 1: Structure determination (70 points)

X-ray diffraction is used to study a powder specimen of a monoatomic substance that is known to crystallize in a cubic lattice structure with primitive vectors $\vec{a}_1 = (a, 0, 0)$, $\vec{a}_2 = (0, a, 0)$ and $\vec{a}_3 = (0, 0, a)$. The wavelength of the X-rays is 1.4 Å.

a) Find the primitive vectors of the reciprocal lattice. (15 points)

Problem 2: One-dimensional Morse solid (80 points points)

Consider N identical atoms of mass M whose motion is restricted to the x-axis. Nearest neighbor atoms are coupled by the so-called Morse potential

$$V_M(r) = D \left(1 - e^{-\alpha(r-r_0)} \right)^2 - D$$

where r is the distance between them and D, α , and r_0 are positive constants.

a) Calculate $V_M(0)$, $V_M(\infty)$ and qualitatively sketch the Morse potential. (10 points)

Problem 3: Phonons of a square lattice (50 points)

Consider a two-dimensional solid of identical atoms of mass M on a square lattice of lattice constant a. In this problem, we investigate vibrations perpendicular to the lattice plane. The equations of motion for the displacements $u_{j,l}$ read

$$M\ddot{u}_{j,l} = K(u_{j+1,l} - u_{j,l}) + K(u_{j-1,l} - u_{j,l}) + K(u_{j,l+1} - u_{j,l}) + K(u_{j,l-1} - u_{j,l})$$

Here, j and l index the atom position in the x and y directions, respectively.

- a) Determine the dispersion relation (ω as a function of \vec{q}) of the phonons for a wave with a wave vector $\vec{q} = (q_x, q_y)$. (30 points)
- b) Calculate the speed of sound in terms of K and M. Does it depend on the direction of \vec{q} ? (20 points).

Dispersions (Dispersion relations)



Phonon Density of States



Van Hove Singularity

Exercise 3 Singularity in density of states

(a) From the dispersion relation derived in the lecture for a monoatomic linear lattice of N atoms with nearest neighbour interactions, show that the density of modes is

$$D(\omega) = \frac{2N}{\pi} \cdot \frac{1}{\sqrt{\omega_{\rm m}^2 - \omega^2}},\tag{4}$$

where $\omega_{\rm m}$ is the maximum frequency.

(b) Suppose that an optical phonon branch has the form $\omega(K) = \omega_0 - AK^2$, near K = 0 in three dimensions. Show that $D(\omega) = \left(\frac{L}{2\pi}\right)^3 \left(\frac{2\pi}{A^{3/2}}\right) (\omega_0 - \omega)^{\frac{1}{2}}$ for $\omega < \omega_0$ and $D(\omega) = 0$ for $\omega > \omega_0$. Here the density of modes is discontinuous.

Electronic Density of States



Physics 481: Condensed Matter Physics - Test prep homework

Problem 1: Tightly bound electrons in 1D (10 points)

Consider a one-dimensional electron system with lattice constant a in tight binding approximation. The energy-momentum relation reads

$$\epsilon(k) = -2t\cos(ka) \; .$$

- a) Calculate the electronic density of states $D(\epsilon)$.
- b) Does it have van-Hove singularities? If so, discuss their character!
- c) Calculate the Fermi energy for 0.5, 1, and 2 electrons per unit cell.
- d) For one electron per unit cell, calculate the low-temperature specific heat (per cell)!